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APPENDIX
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**ANALYTICAL
AERIAL TRIANGULATION
ERROR ANALYSIS AND
APPLICATION OF COMPENSATING
EQUATIONS TO
THE GENERAL BLOCK
TRIANGULATION AND
ADJUSTMENT PROGRAM**

MARCH 1960 TO FEBRUARY 1962
DEPARTMENT OF THE ARMY TASK NO. 8T35-11-001-05
CONTRACT NO. DA-44-009 ENG 4420

U.S. Army Engineer
Geodesy, Intelligence, and Mapping
Research and Development Agency

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Final Technical Report
Appendix

MIT

**DEPARTMENT
OF
CIVIL
ENGINEERING**

SCHOOL OF ENGINEERING
MASSACHUSETTS INSTITUTE OF TECHNOLOGY
Cambridge 39, Massachusetts

JUN 26 1962
ILL REG. NO. 8549

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ANALYTICAL AERIAL TRIANGULATION ERROR ANALYSIS

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APPLICATION OF COMPENSATING EQUATIONS

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APPENDIX.

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Geodesy, Intelligence, and Mapping
Research and Development Agency

Ld

CIVIL ENGINEERING SYSTEMS LABORATORY
Department of Civil Engineering
Research Report R62-44
Massachusetts Institute of Technology
Cambridge, Massachusetts

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PREFACE

These investigations were carried out under the authority contained in Contract No. DA-44-009 ENG 4420, "Analytical Aerial Triangulation Error Analysis and Application of Compensating Equations to the General Block Triangulation Adjustment Program."

The investigation was conducted under the direction of Professor Charles L. Miller and Mr. E. Phillip Gladding, Instructor, Department of Civil Engineering. The investigation was conducted, from March 10, 1960 to March 10, 1962, by Messrs. Luis Andrew R., Ziad M. Elias, and Frank S. Greatorex, Research Assistants in the Department of Civil Engineering. Also contributing to the investigation were Messrs. Daniel R. Schurz, Instructor, Armen Gabrielian, Student Assistant, and Lawrence Kalman, Student Assistant.

Glynn

ABSTRACT

The objective of the activities reported is to effect improved accuracy in the supplied General Block Triangulation digital computer program through incorporation in the program means of error adjustment and compensation. ^{is described} ^{and} ^{as follows:} The first volume of the report presents:

- (1) the nature of random and systematic errors and the basic techniques for treating their effects as applicable to the analytical photogrammetric problem;
- (2) the basic least squares method and its incorporation in the computer program;
- (3) complete mathematical description of the program;
- (4) studies of the nature and effects of the important error sources: lens and camera errors, atmospheric refraction, film distortion;
- (5) the study of various techniques for the solution of simultaneous equations;
- (6) operating instructions; and
- (7) the results, conclusions, and resulting recommendations of test runs of the final computer program.

The second volume contains the appendices which consist of the complete flow charts representing the original and final programs.

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TABLE OF CONTENTS

VOLUME II

Title Page	i
Preface	ii
Abstract	iii
Table of Contents	iv
Flow Chart Outline	v
<u>Original IBM 704 Computer Program - Flow Chart</u>	
Segment I - Chain 1	A1
Segment II - Chain 2	A22
Segment III - Chain 3	A99
<u>Additions and Modifications to Original Program - Flow Chart</u>	
Segment 2 - Chain 2	B1
Segment 23 - Chain 23	B41

FLOW CHART OUTLINE

Original IBM 704 Computer Program - Flow Chart

Segment I - Chain 1

START - Initializations	A1
Read Control cards: J,P	A1-A2
FILE - Input card read routine	A3
ECARD - Preliminary processing and storing of E-card data	A4-A9
GCARD - Preliminary processing and storing of G-card data	A10-A18
DEXFR - Normal Matrix Bookkeeping	A19
DEXPR - Termination of Segment I - tape writing for Segment II and print outs.	A20

Segment II - Chain 2

CEQBE - Preliminary initializations	A22
CEQES - General exposure station equation forming routine	A22
ESTYT - Test for type of exposure station and transfer to corresponding equation forming routine	A23
ESTYA, ESTYB, ESTYC, ESTYD, ESTYE, ESTYF, ESTYG, and ESTYH - control for forming of equations by exposure station type	A24-A29
CEQST - Scaling and printing of condition equations	A26-A27
MATFR - Form normal equations	A27
EQ11, EQ12, EQ12A, and EQ13 - Conditional equation forming routine	A30-A34
PHXYZ - Exposure station data processing	A35
CEQFA - General ground point data bookkeeping for equation forming	A36-A43

GPTYB, GPTYC, GPTYD, GPTYE, GPTYF, GPTYG, GPTYH, CEQFJ	A44-A48
- control for forming of equations by ground point type	
SUB1, SUB2, XYZRA - subroutines for computing quantities used in equation forming	A49-A59
TEFCL - Process type A ground point	A59-A61
SUEFX - Process type C ground point	A62
EQ56 - Equation former for ground point equation 56	A62-A65
EQ1 - Equation former for ground point equation 1	A66-A69
EQ2 - Equation former for ground point equation 2	A69-A76
EQ34 - Equation former for ground points equation 34	A77-A80
EQ5 - Equation former for ground point equation 5	A80-A81
EQ6 - Equation former for ground point equation 6	A82-A83
EQ6A - Equation former for ground point equation 6A	A83-A85
EQ7 - Equation former for ground point equation 7	A85-A87
EQ70 - Equation former for ground point equation 70	A87-A91
EQ 101, 102A - Equation former for ground point equations 101, 102, 103	A92-A97
FCVSQ - Compute sum of squares of right hand sides of the normal equations and print normal matrix and constant vector and transfer to Segment III	A98

Segment III - Chain 3

RESEG3 - Initialize for Chebyshev routine	A99-A102
CEBYA, CEBYB, CEBYC, CEBYD, CEBYE, CEBYF, CFBYG - Chebyshev routine for generating initial values for the Steifel iteration method	A103-A104
STEFB, STEFC, STEFD - Steifel solution initial- izations for execution of Steifel iteration cycle STEFL	A104-A105
STEFE, STEFF, STEFG, STEFM, SSDMT, SSDMD, SSDMP - Post Steifelcycle control routines	A105-A107

STEFZ - Non-convergence print out and control routine	A107
SSVAL - Error print out routine	A107
SSEND - Cycle solution print out routine	A108
CHEBY - Routine used in CEBYF	A109-A110
MXV - Routine used in CEBYB	A110-A112
STEFL - Steifel iteration routine used in STEFD	A113-A117
DPMXV - Routine used in STEFL	A118-A120
SEG3B - Initializations for segment 3B	A121
CMRBE - Testing for sufficient convergences of exposure station position vector	A121
CORMR, CORREC, CMPUTE, AYESEE, BEET, BB, DD, FF - Routines using Steifel solution to correct position vectors and orientation matrices of exposure stations	A121-A125
CMTSX+3, ITERC, SEGTX - Print out and store on magnetic tape corrected position vectors and orient- ation matrices of every exposure station, and test for transfer to resection computation or to segment 2.	A125-A127
RESBE - Initializations for resection routine	A127
RESTR, LXYZ, FXMAT, ... , FULLC, PRANG, PREST - Computation, storing, and printing out of exposure station position and orientation parameters	A127-A134
GPRES, GPANL, GPCAL, GBCCB - Print out the given ground point coordinates corresponding to different pairs of photographs. Rewind magnetic tape, halt, and transfer to start a new segment 3 iteration if desired.	A134-A139

Additions and Modifications to Original Program - Flow Chart

Segment 2 - Chain 2

TMX*	- Formation of T matrix associated with each image point	B1-B3
FRBWN	- Write on magnetic tape condition equation and control data	B3-B5
CEQST	- Print out coefficients of unknowns as in original program. Compute control words defining equation type	B5-B8
MFALP	- Equation 70 tape writing routine	B8-B9
SUB1	- Modified to include computations introduced by changes in conditional equations	B9-B10
EQ1	- Additions to original EQ1	B11-B12
EQ2	- Additions to original EQ2	B13-B17
EQ34	- Additions to original EQ34	B18-B20
EQ5	- Additions to original EQ5	B21-B22
EQ6	- Additions to original EQ6	B23-B25
EQ6A	- Additions to original EQ6A	B26-B28
EQ7	- Additions to original EQ7	B29-B30
ESTYA	- Additions to original ESTYA	B30-B32
EQ11	- Additions to original EQ11	B32
EQ12	- Additions to original EQ12	B32-B33
EQ12A	- Additions to original EQ12A	B33-B34
EQ13	- Additions to original EQ13	B34
EQ56	- Additions to original EQ56	B35-B38
EQ101	- Additions to original EQ101	B39-B40

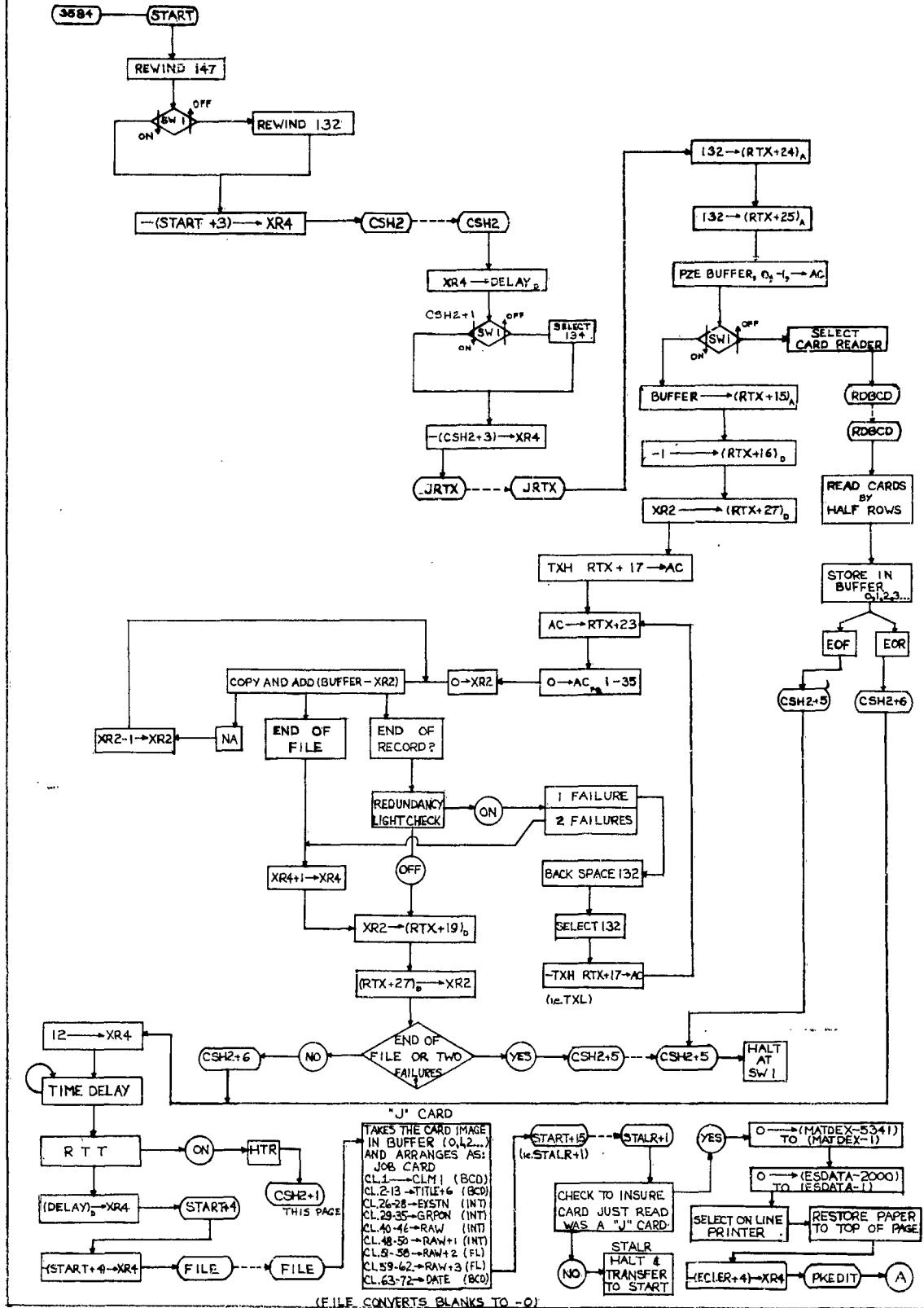
Segment 23 - Chain 23

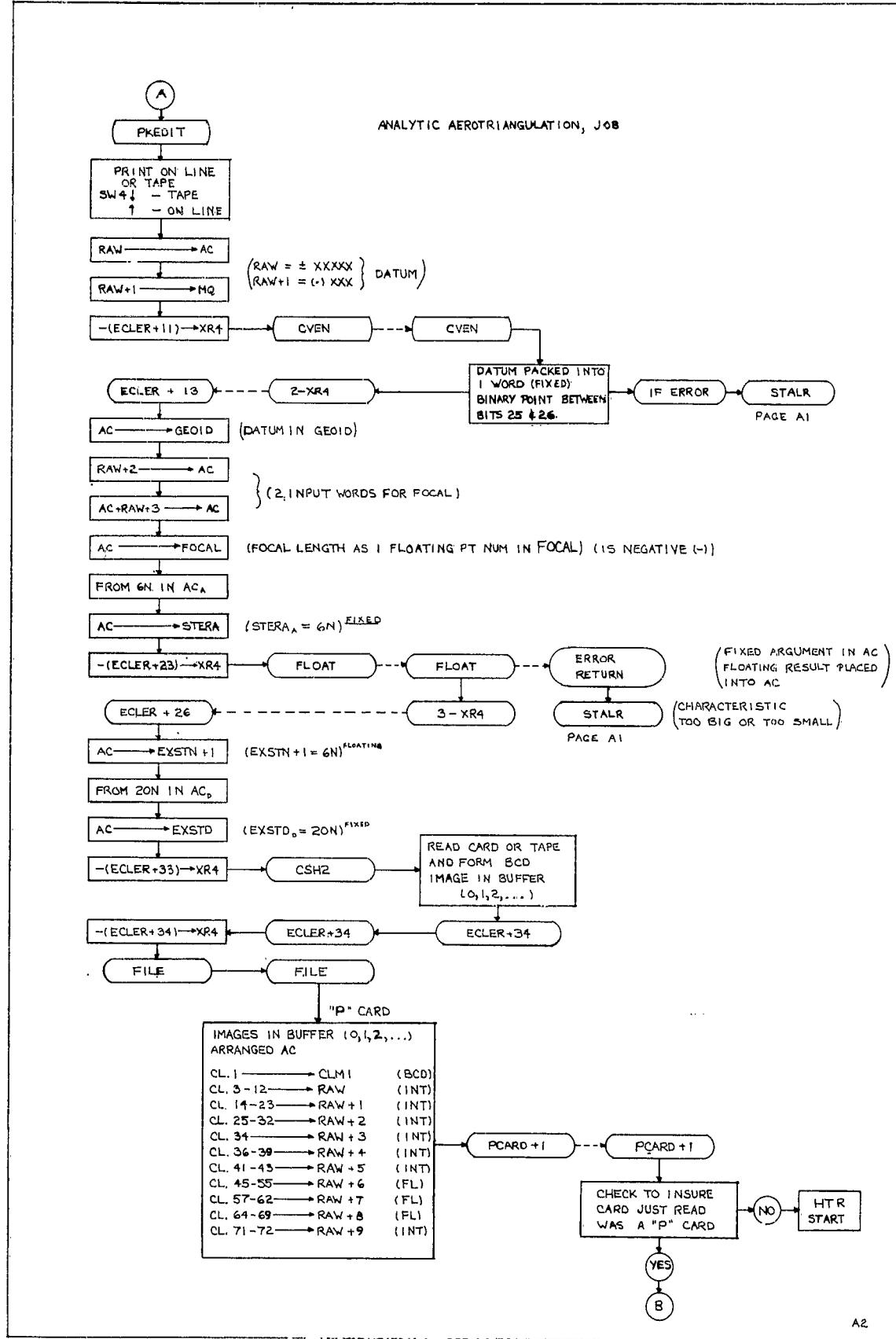
ECHO*	- Read conditional equations from tape	B41-B43
FRBWN*	- Weight matrix and normal equation forming and storing routine	B44-B50

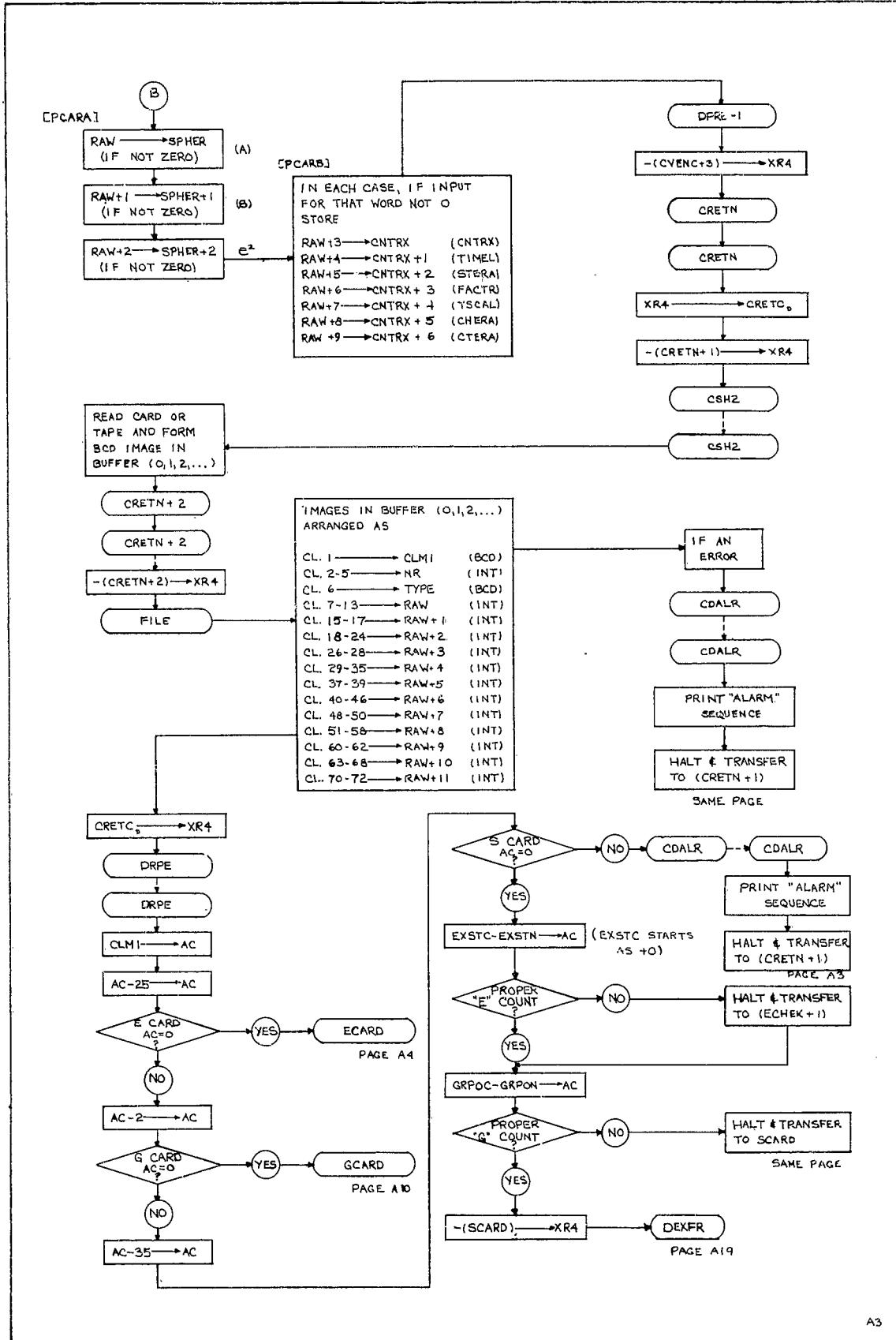
* Additions

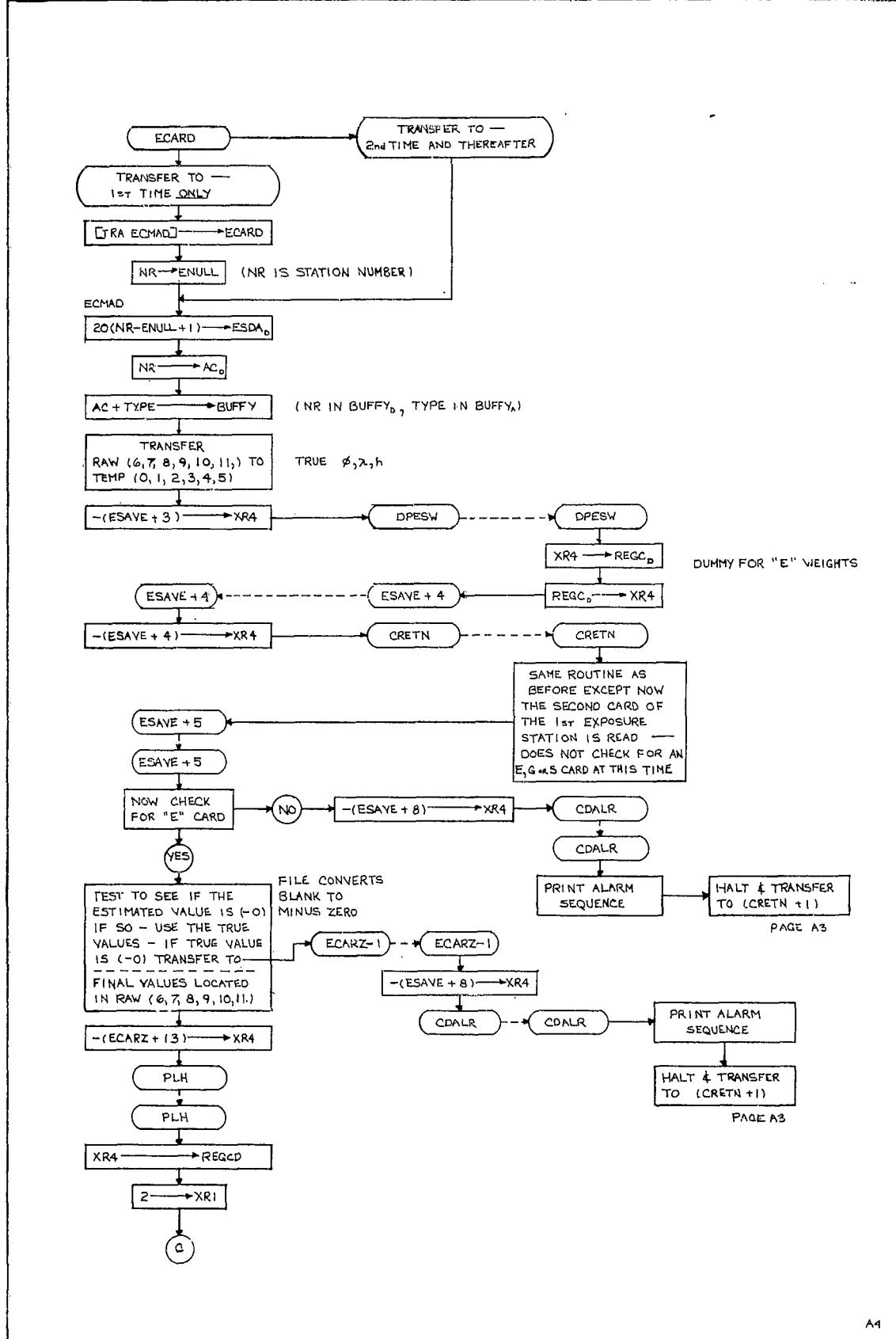
APPENDIX A

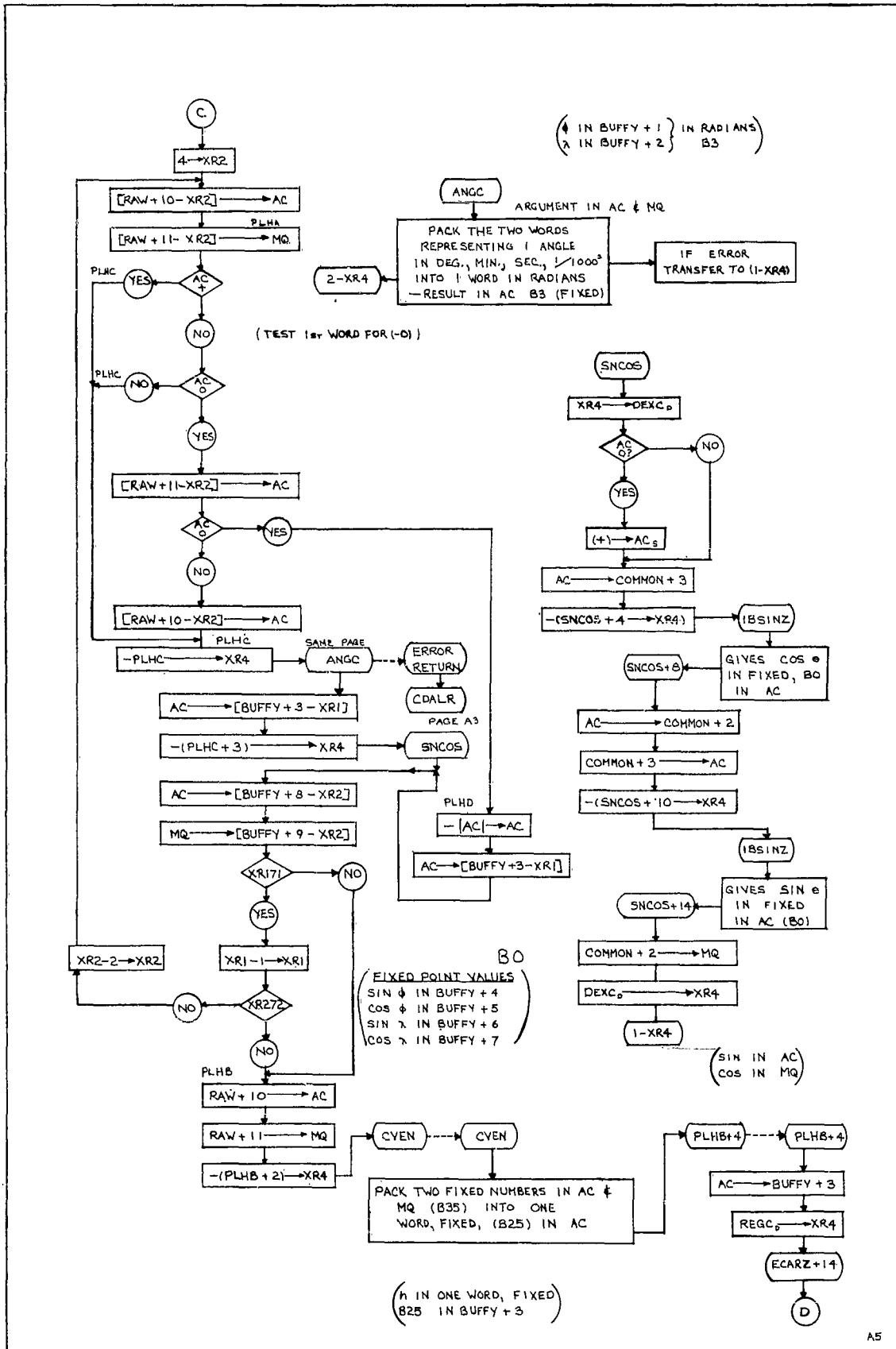
ORIGINAL IBM 704 COMPUTER PROGRAM - FLOW CHART

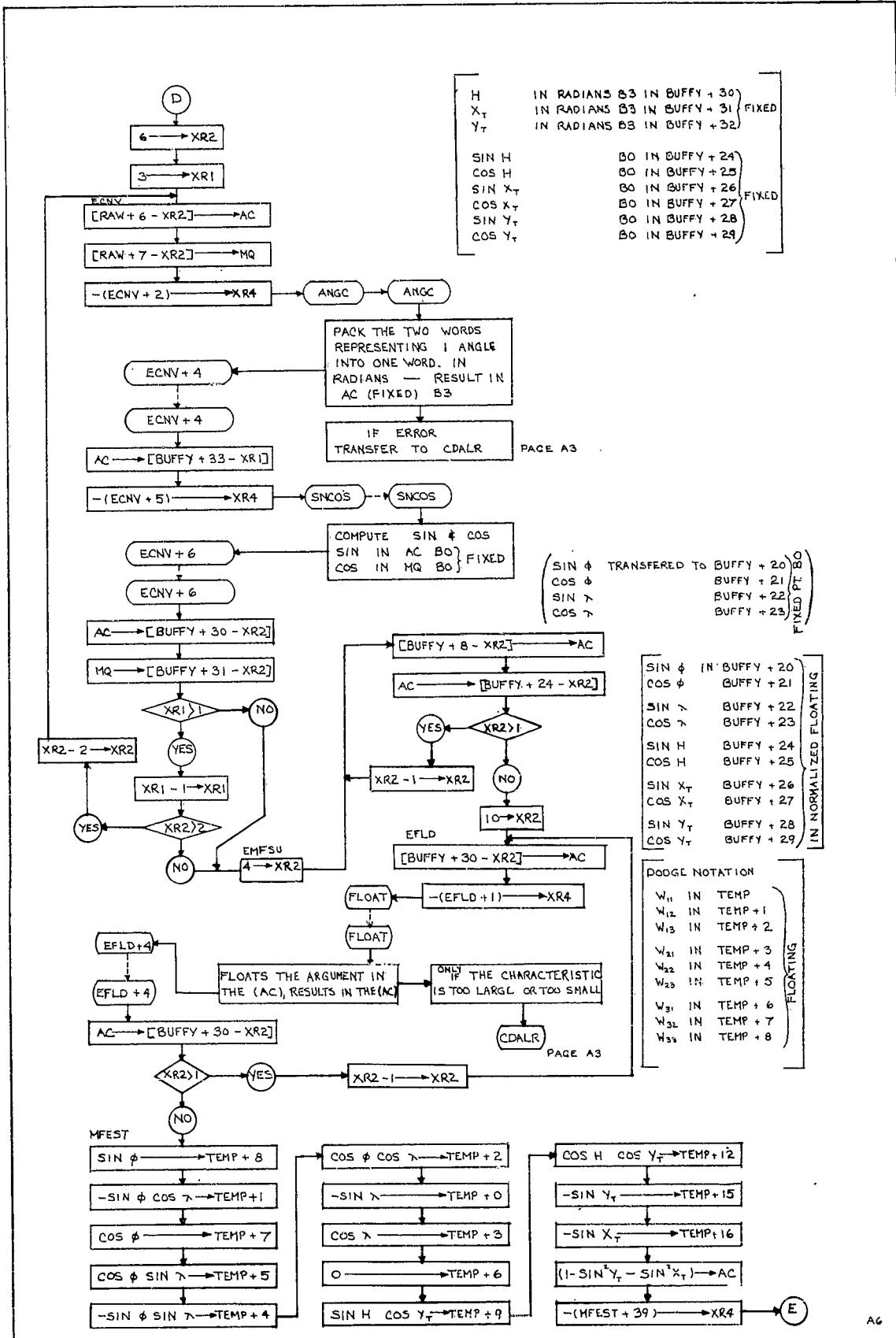


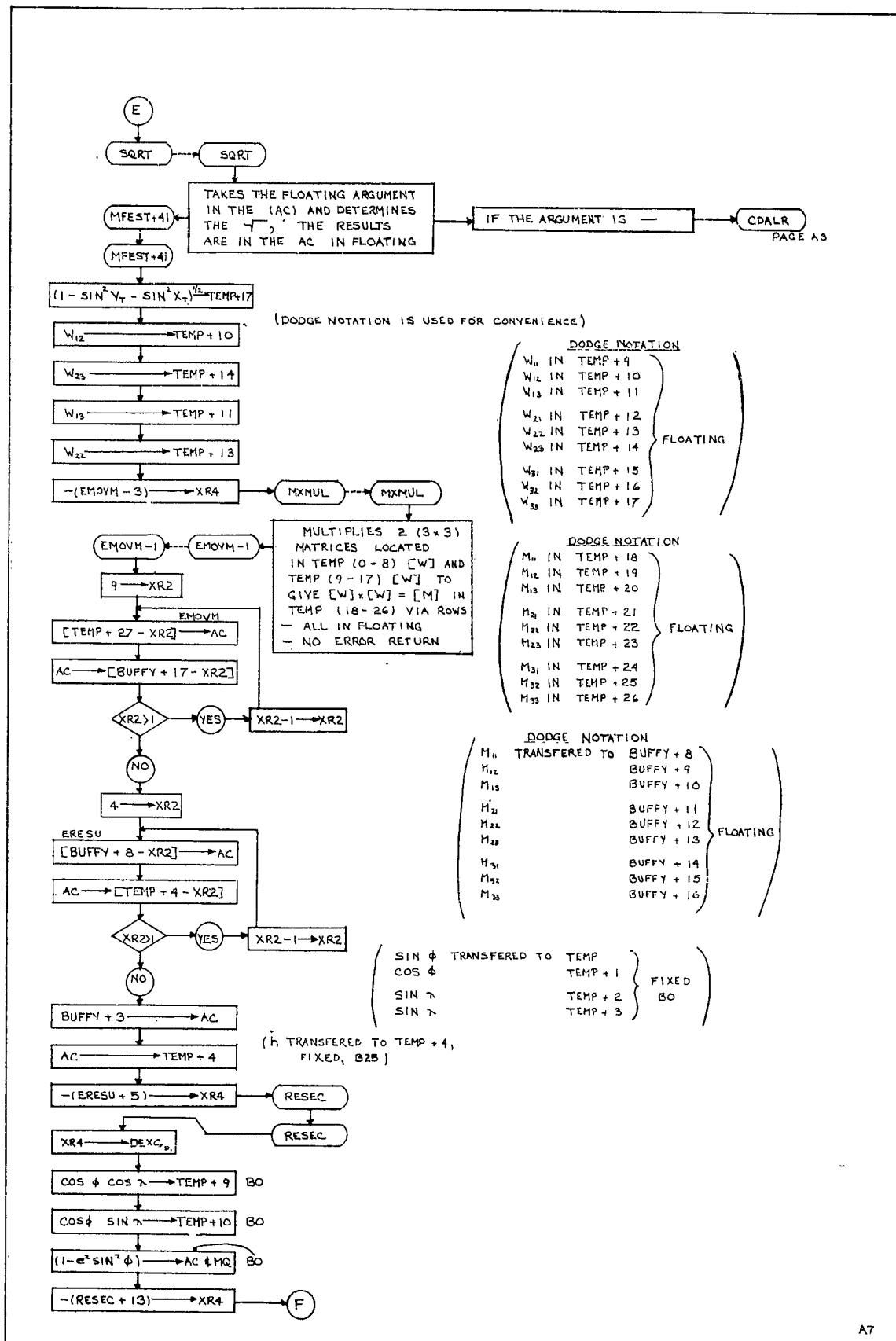


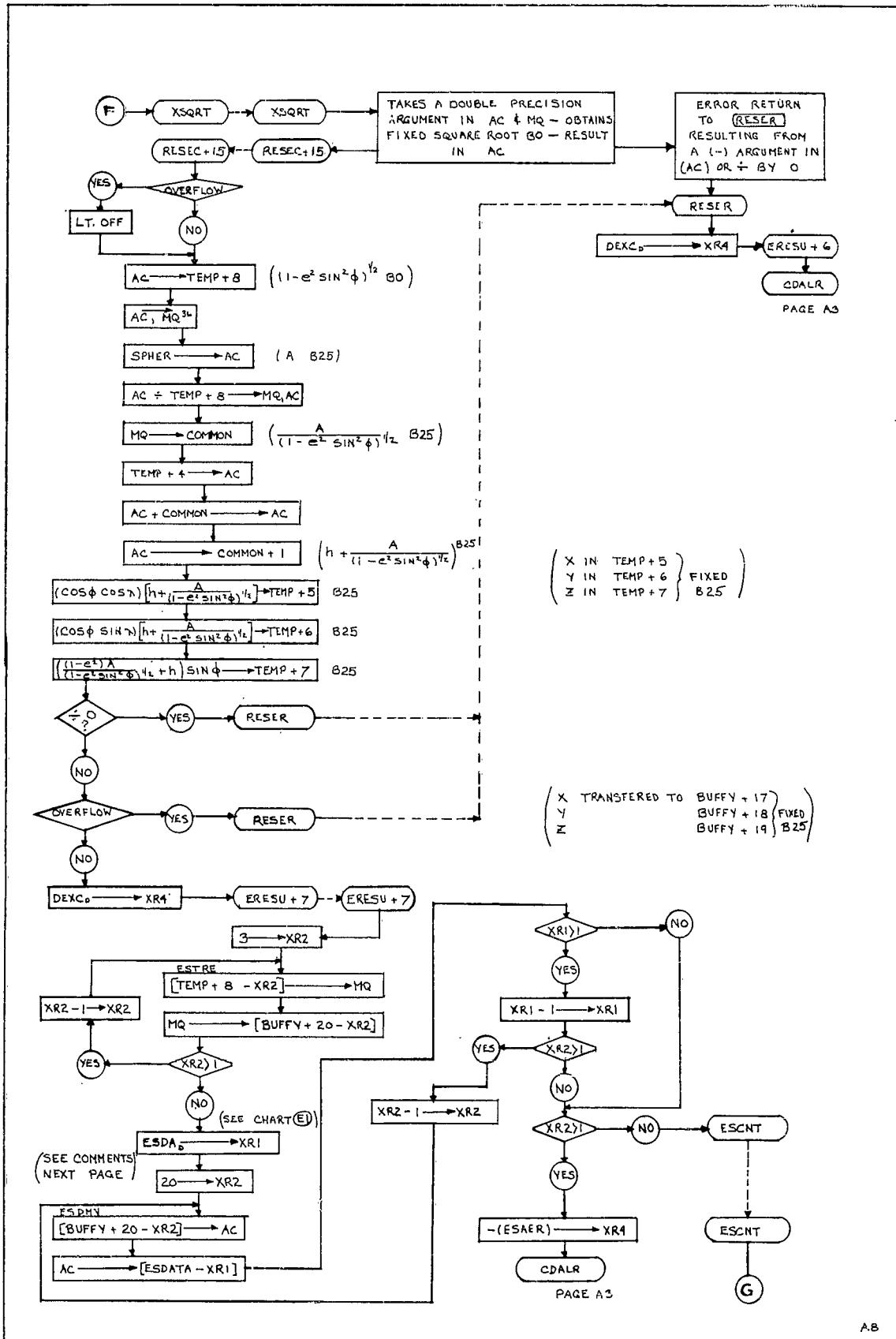


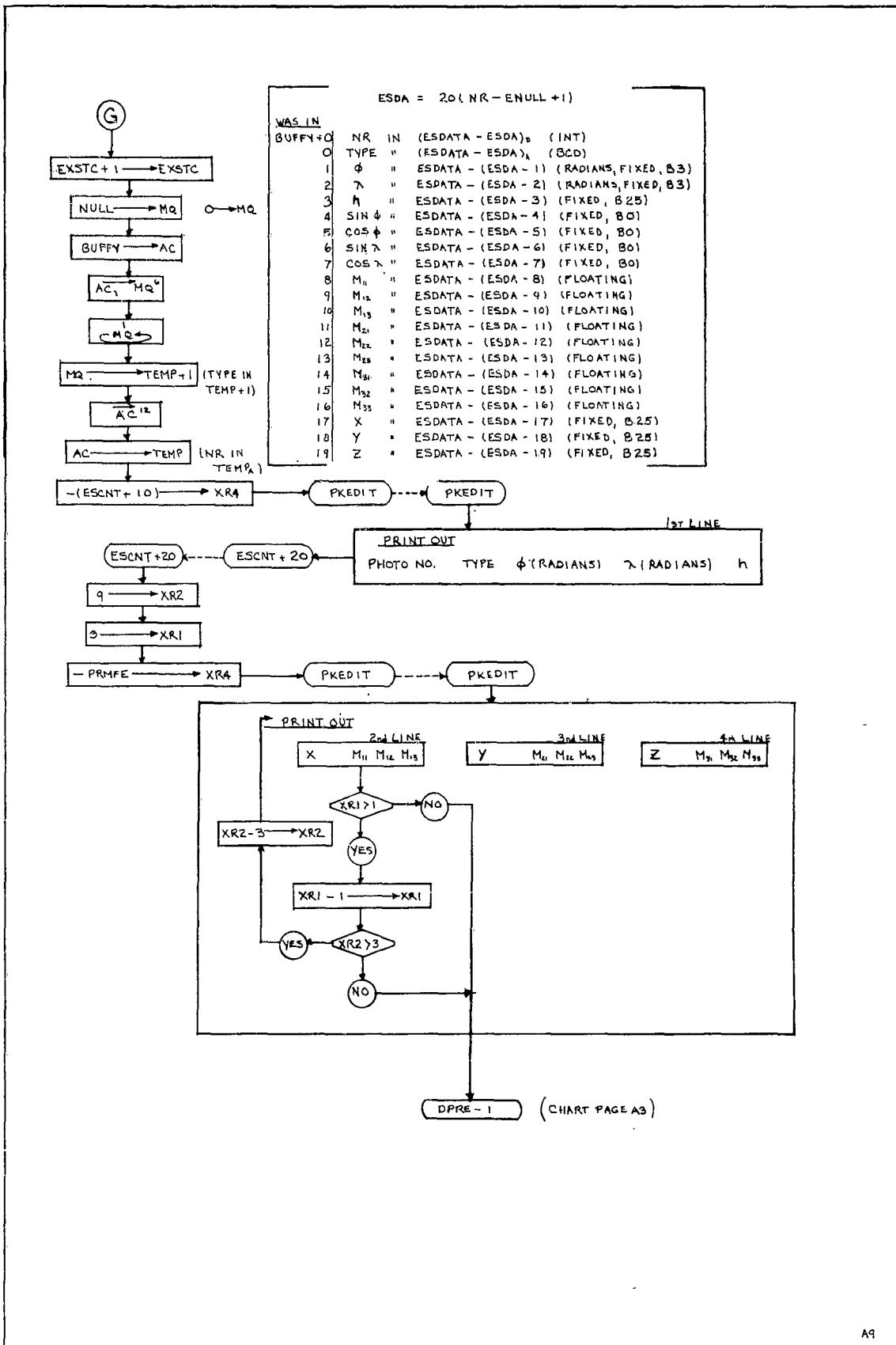


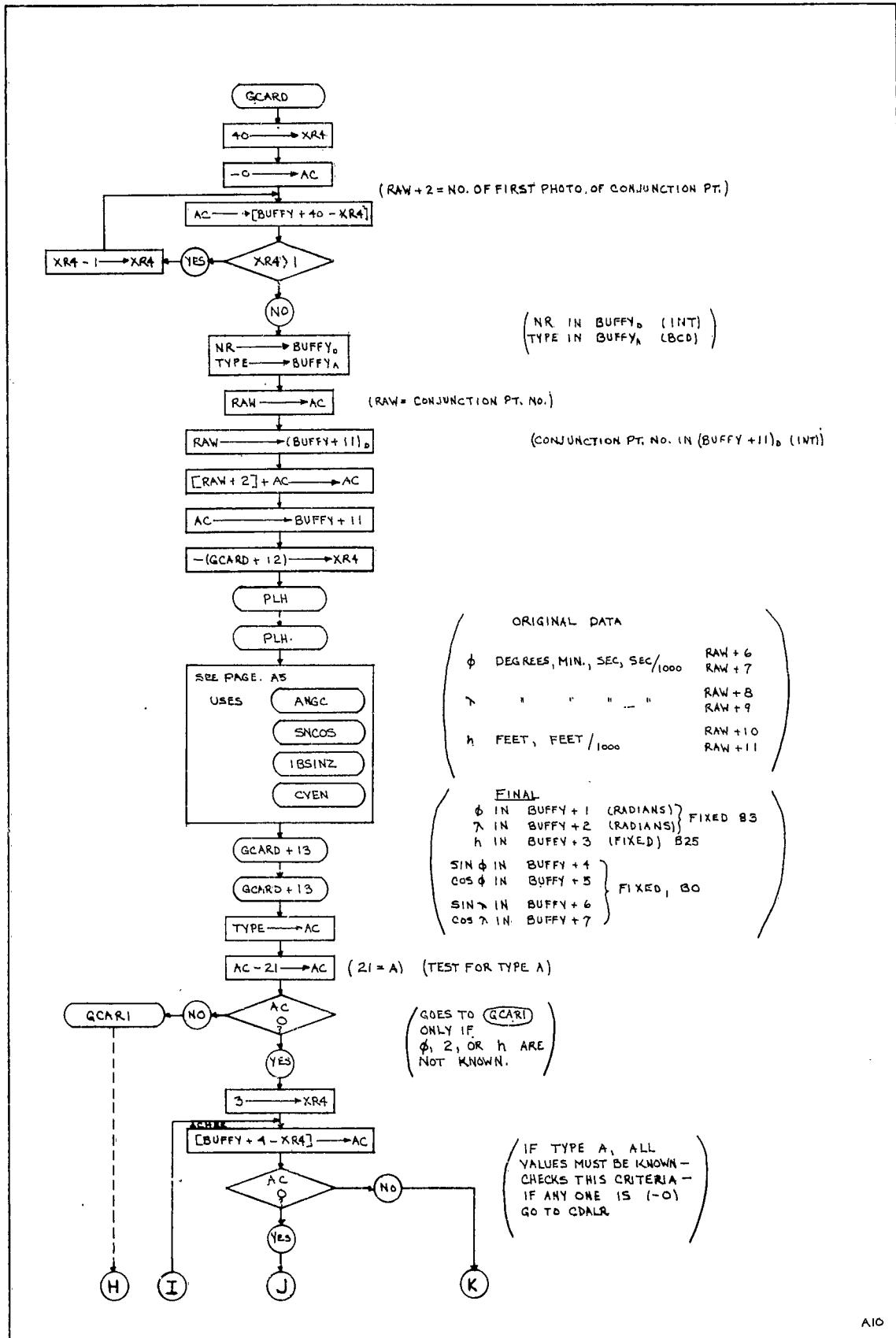


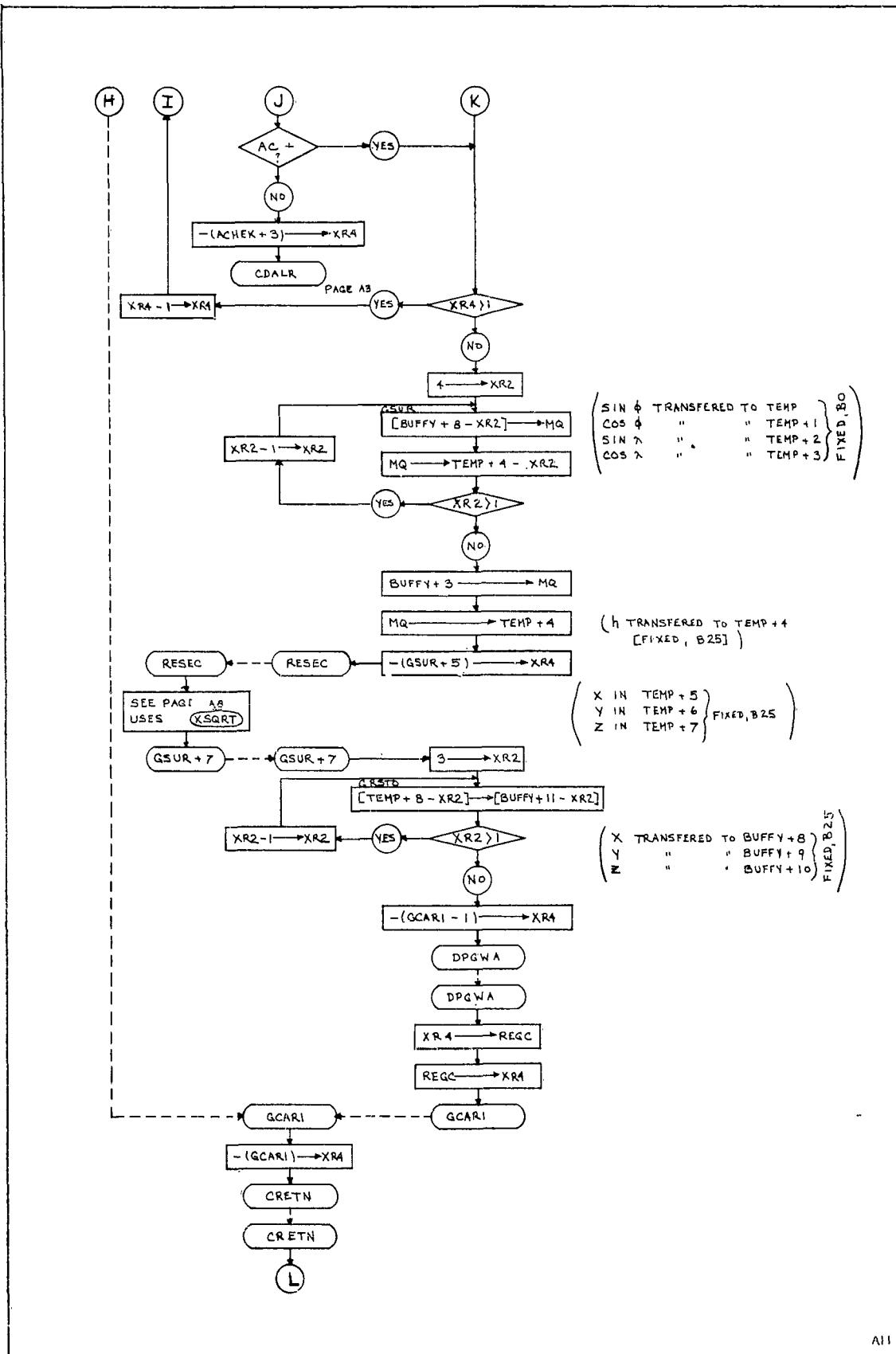


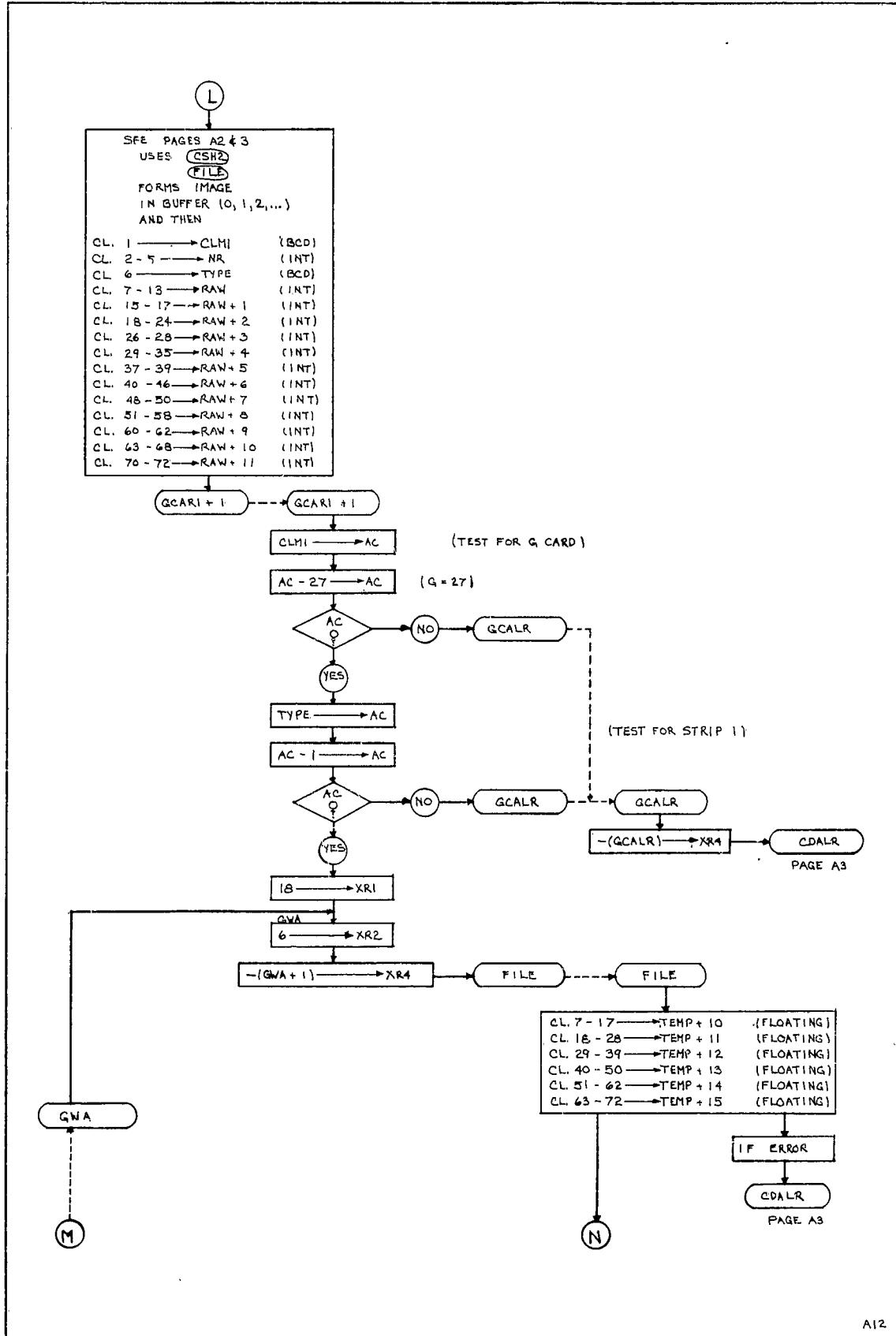


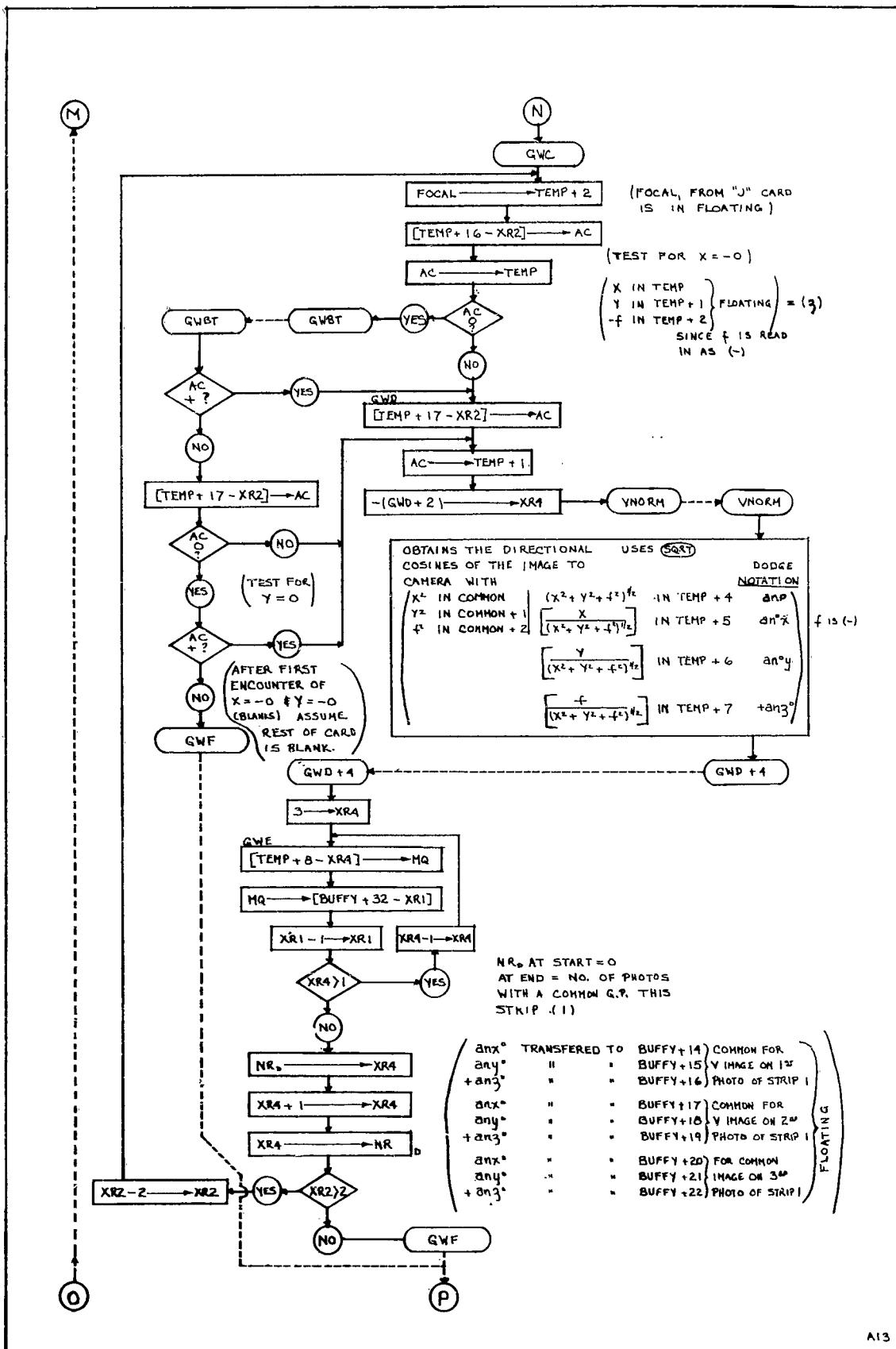


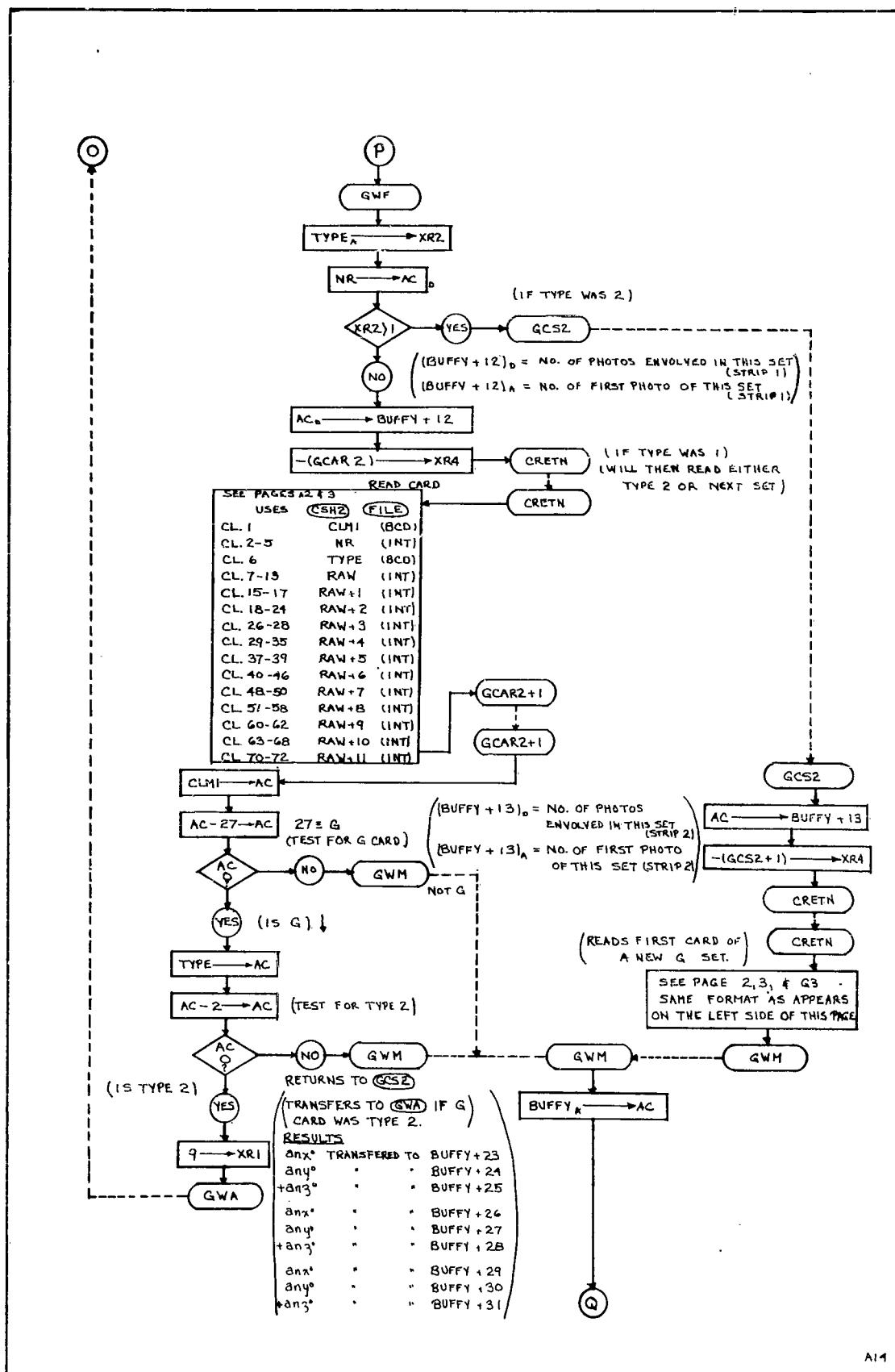


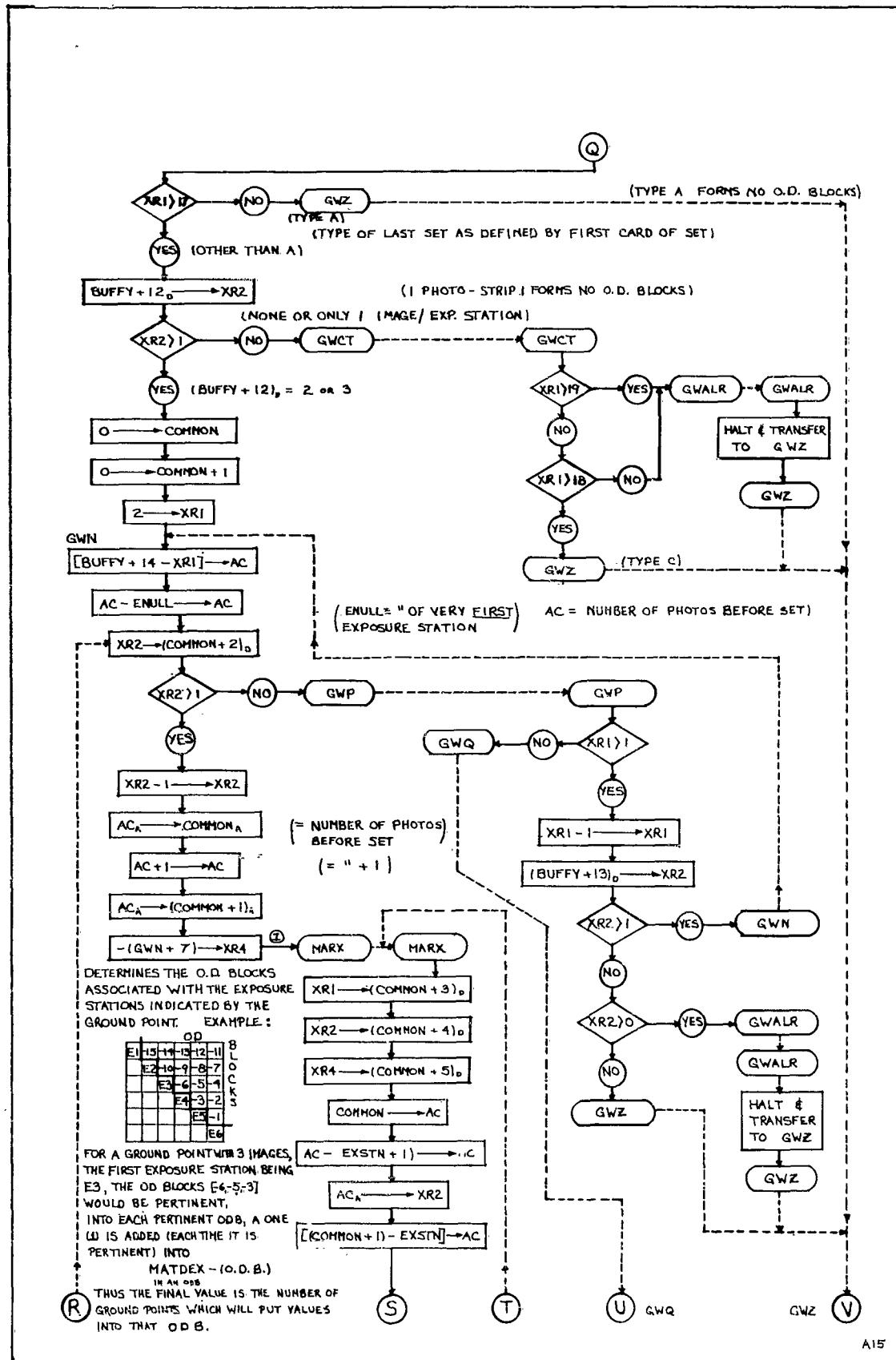


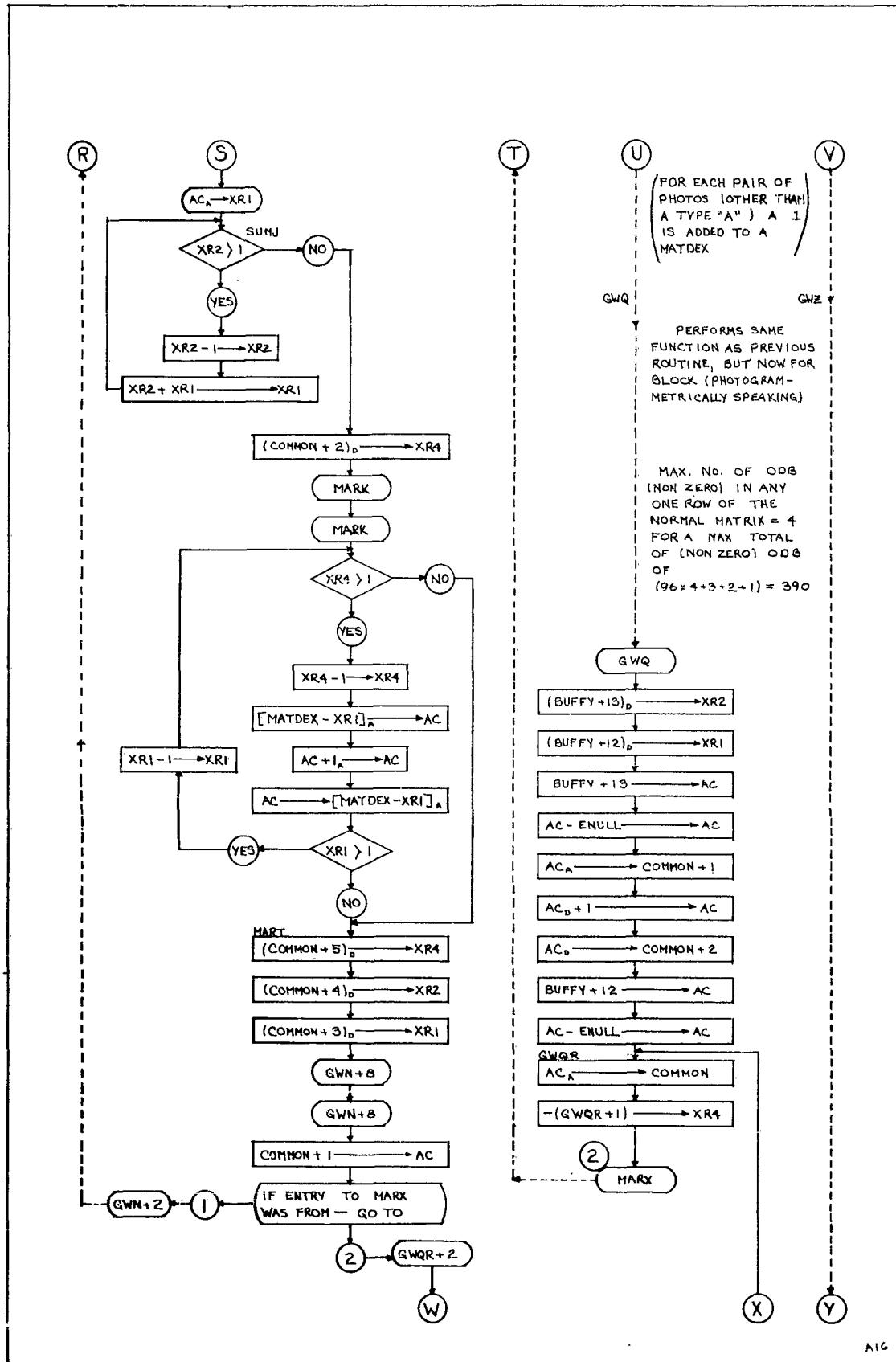


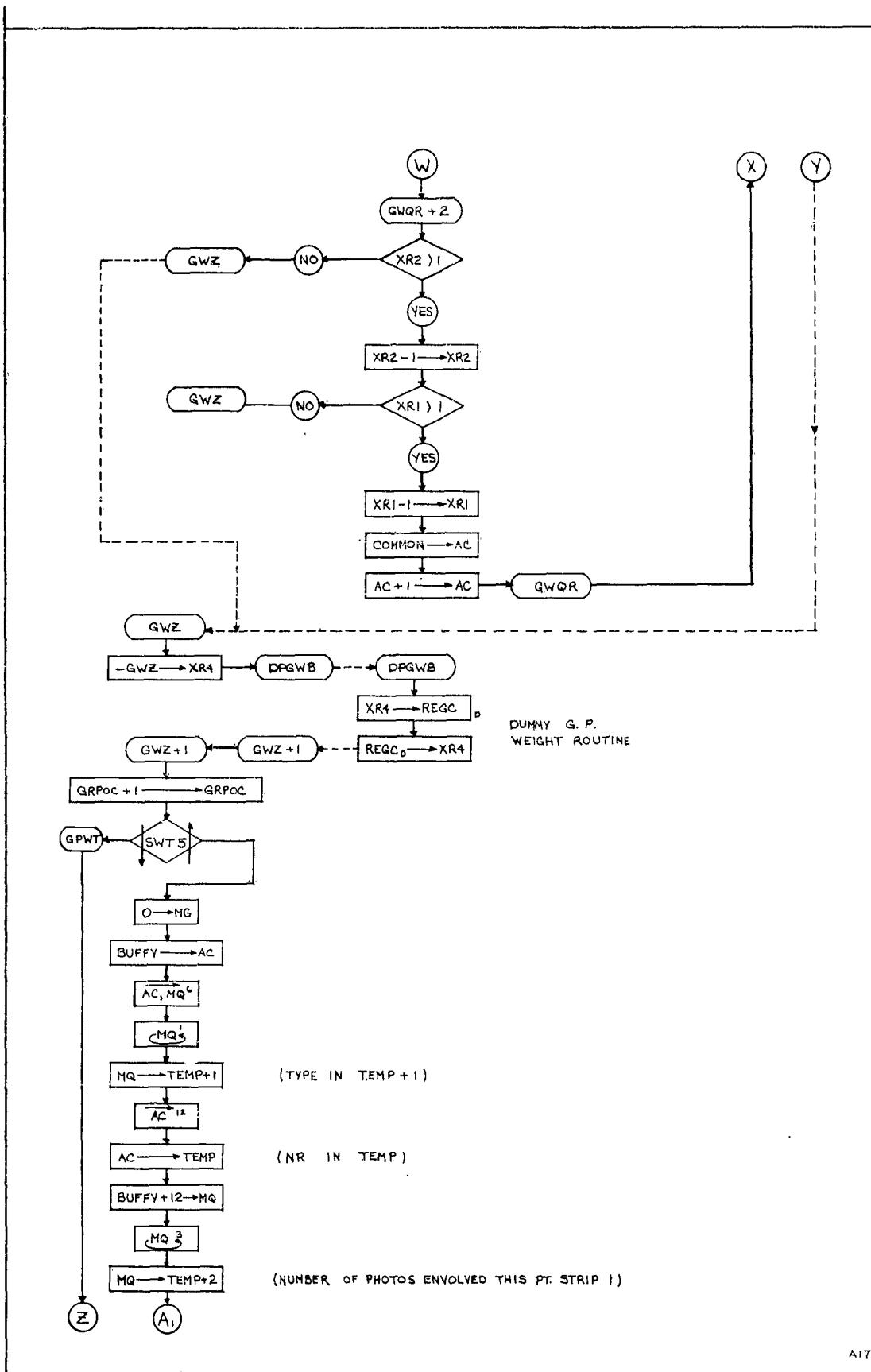


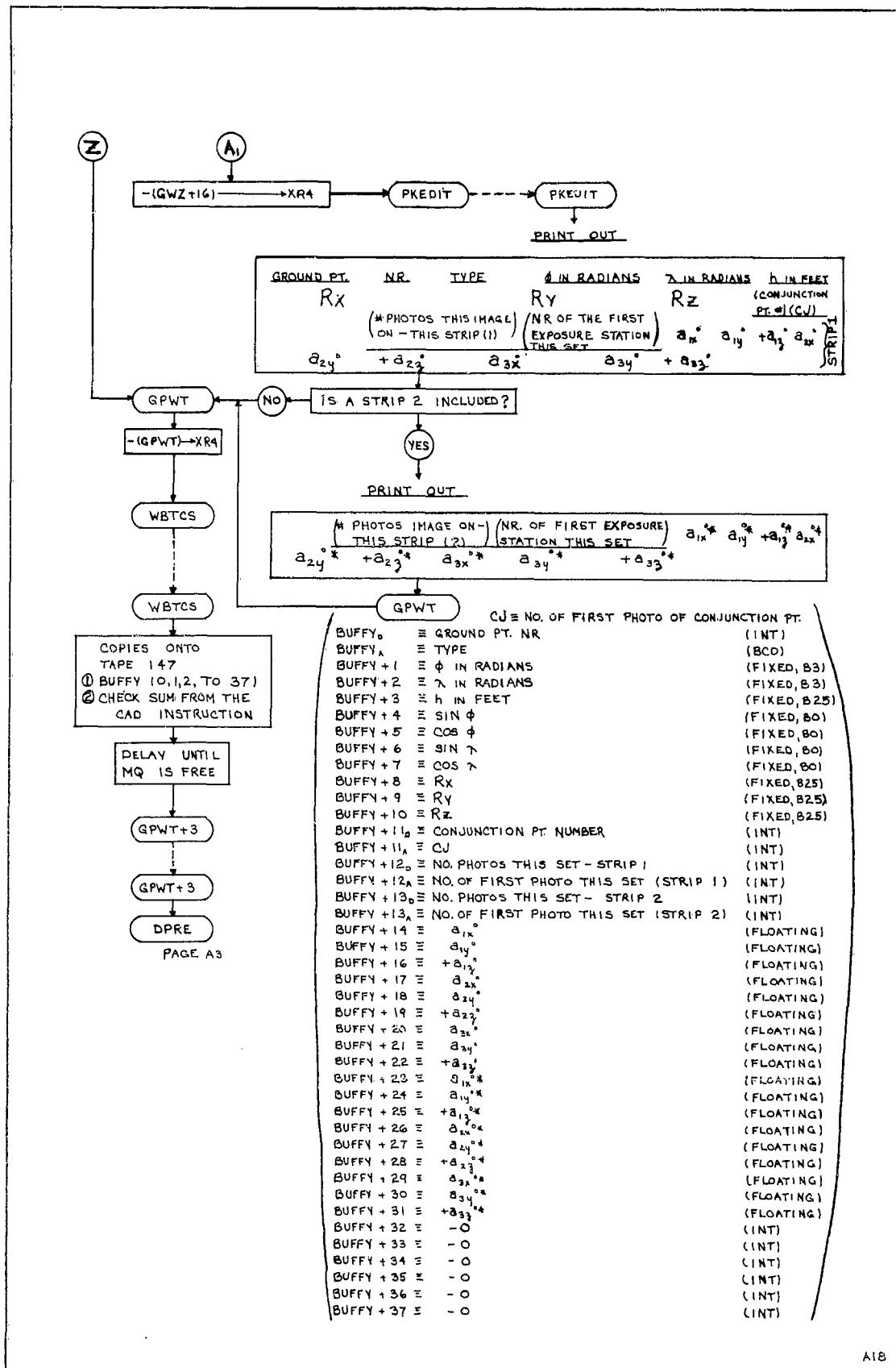


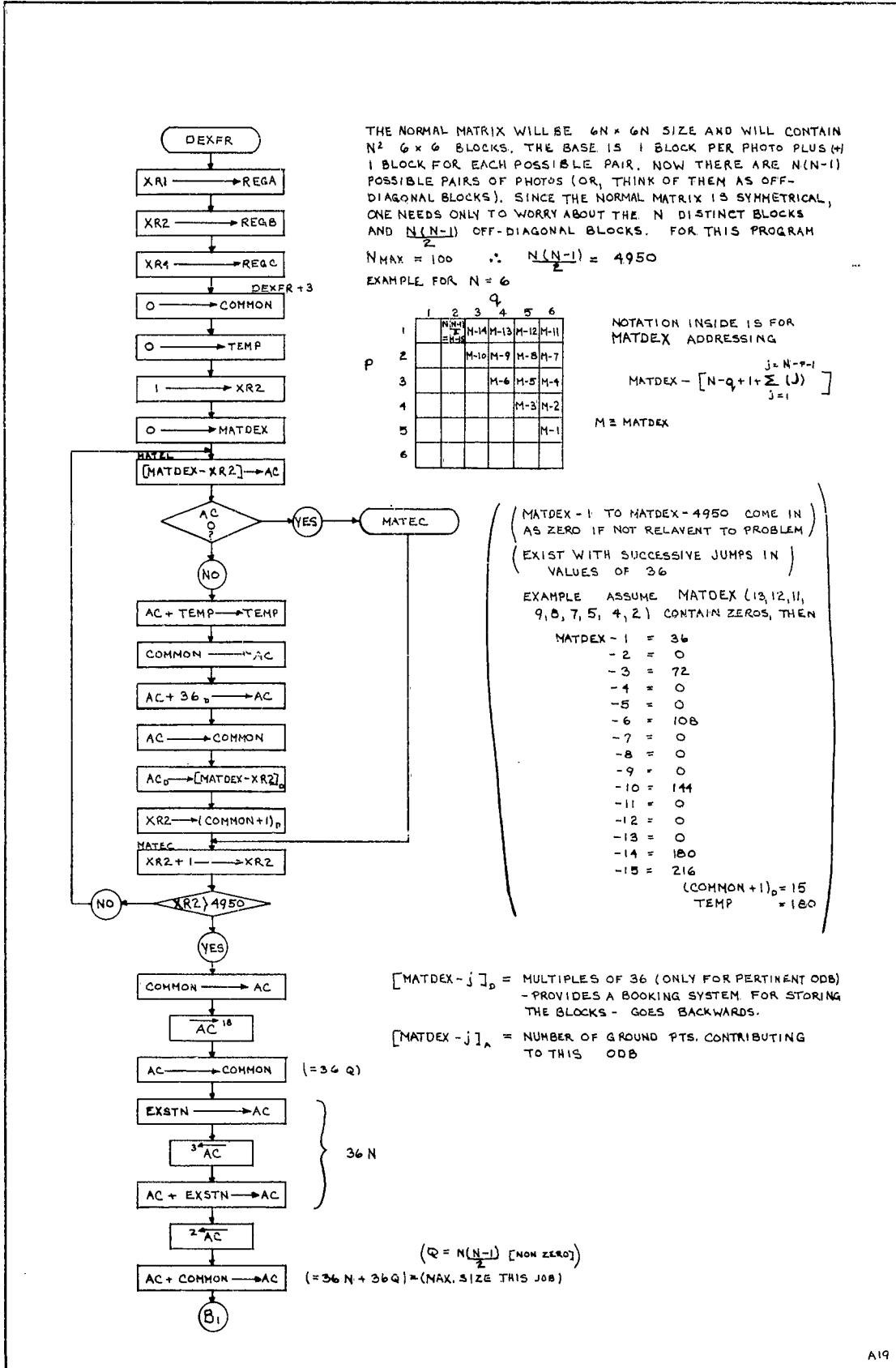


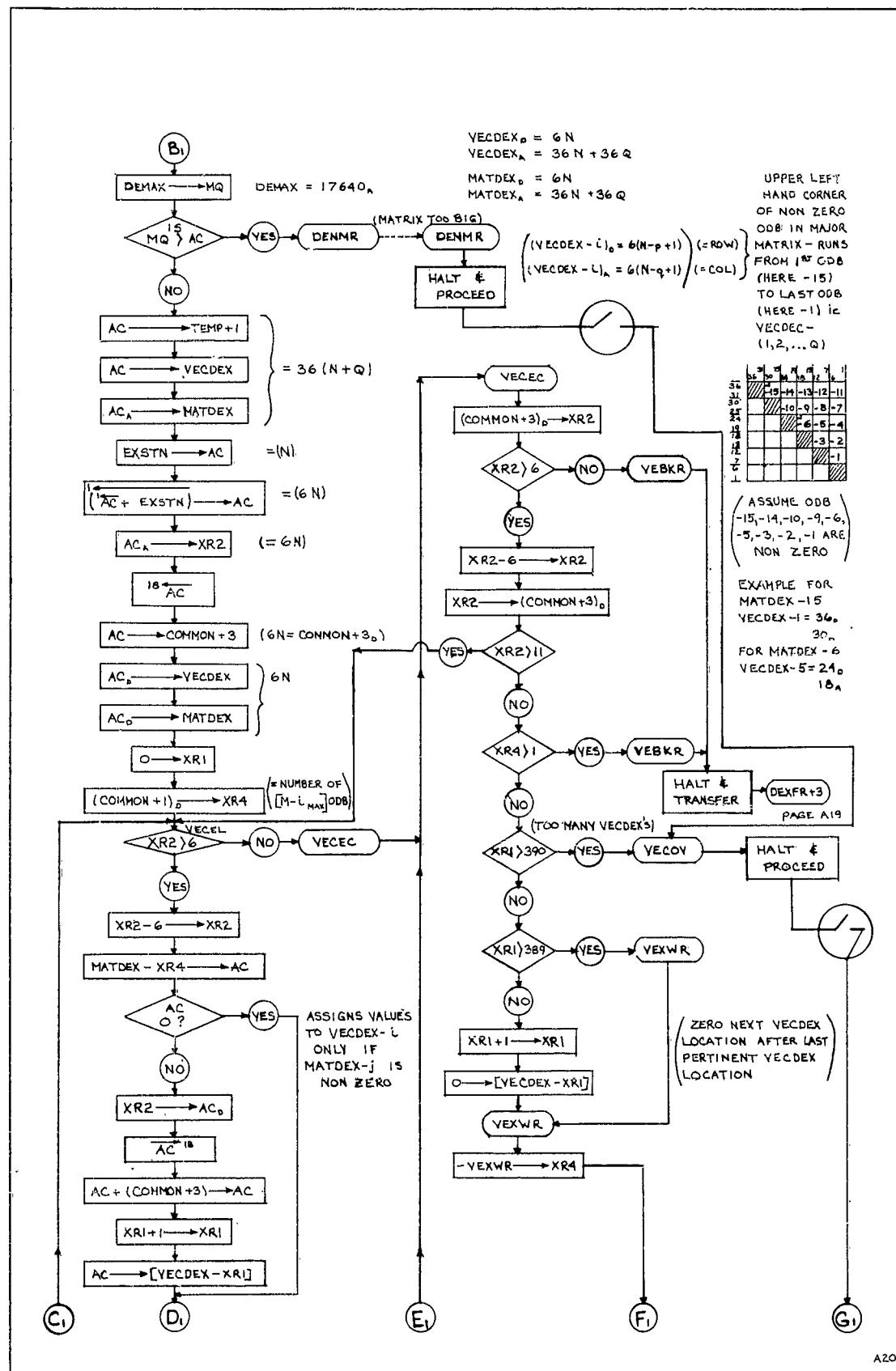


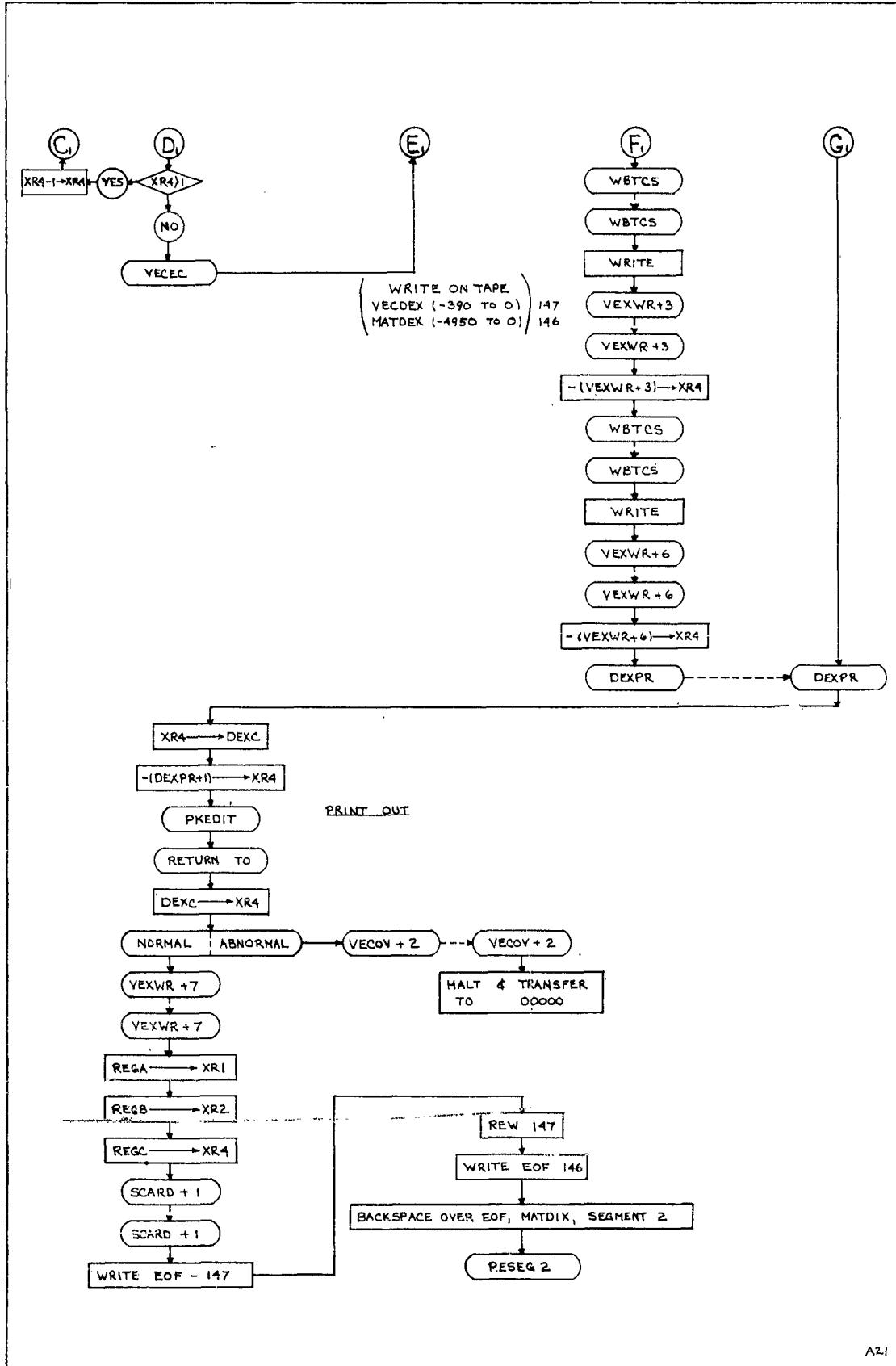


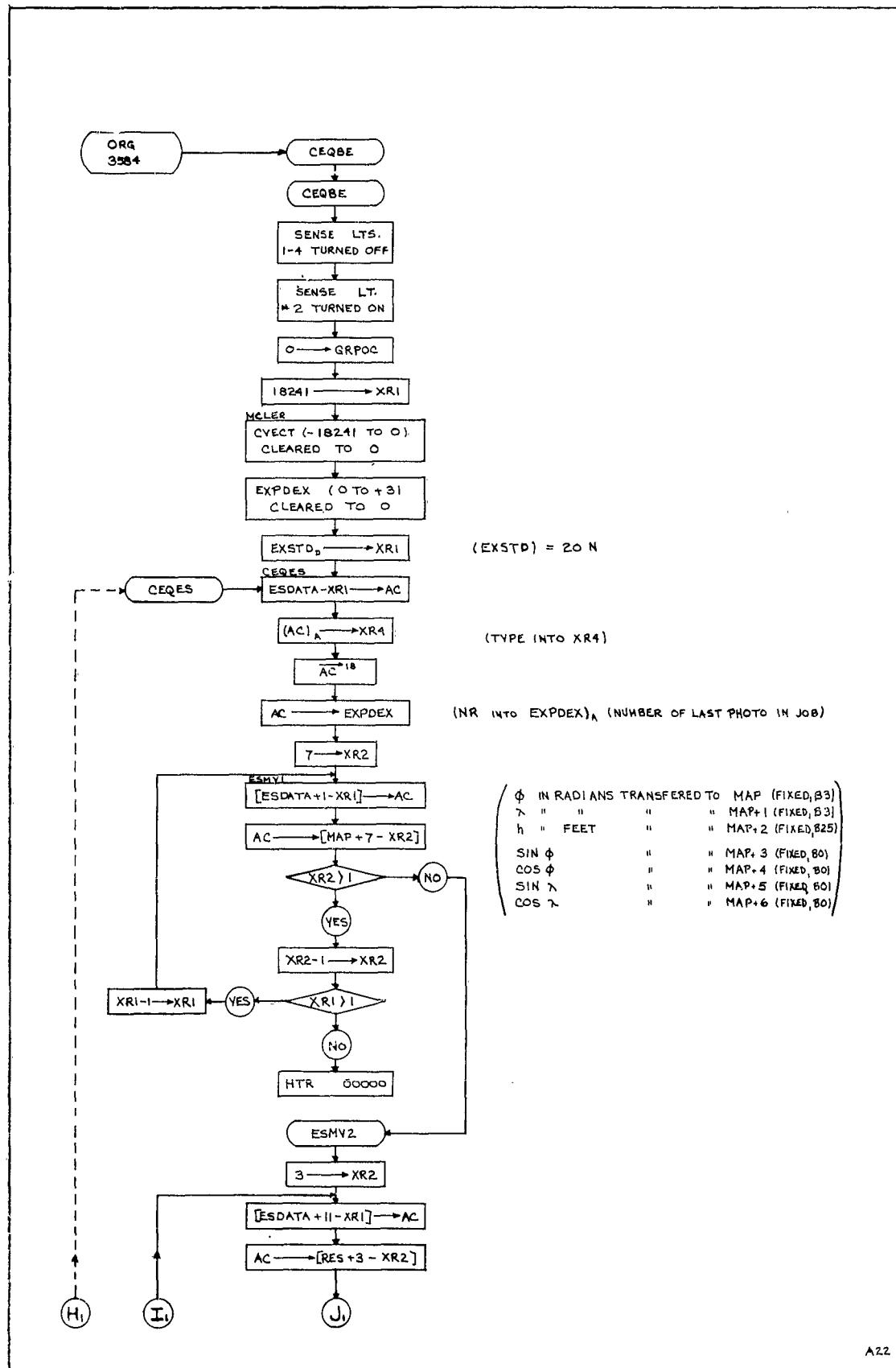


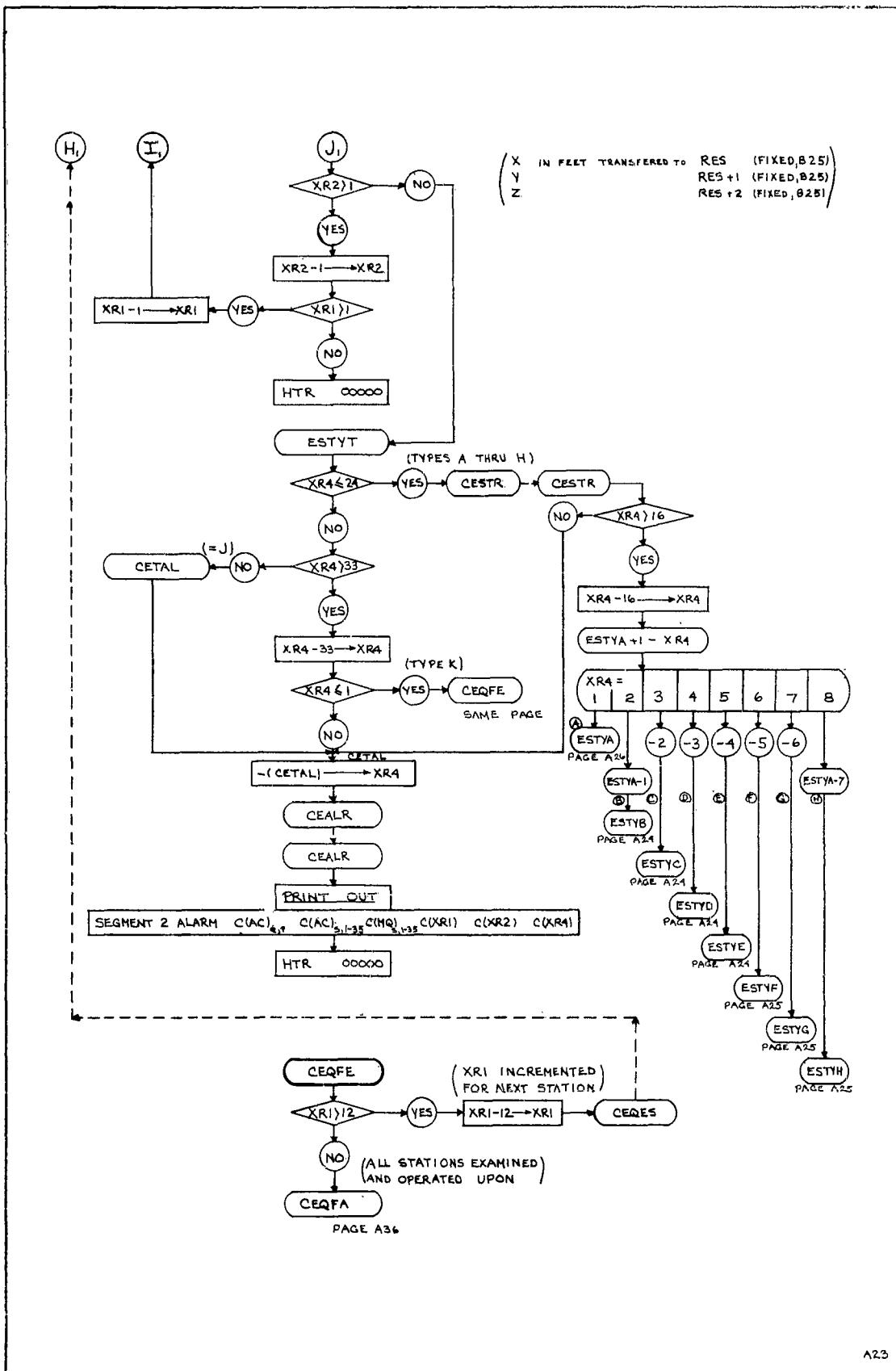


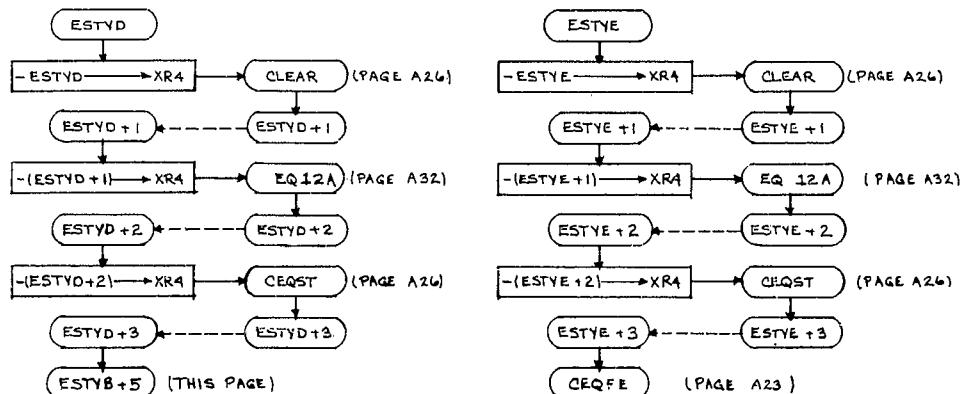
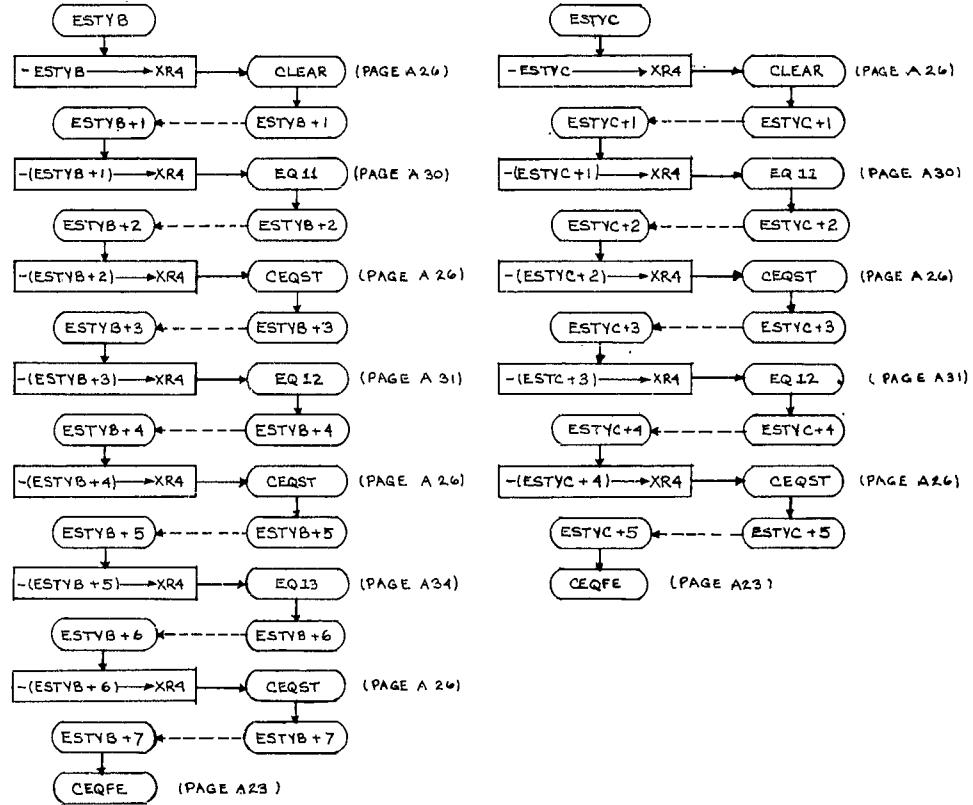


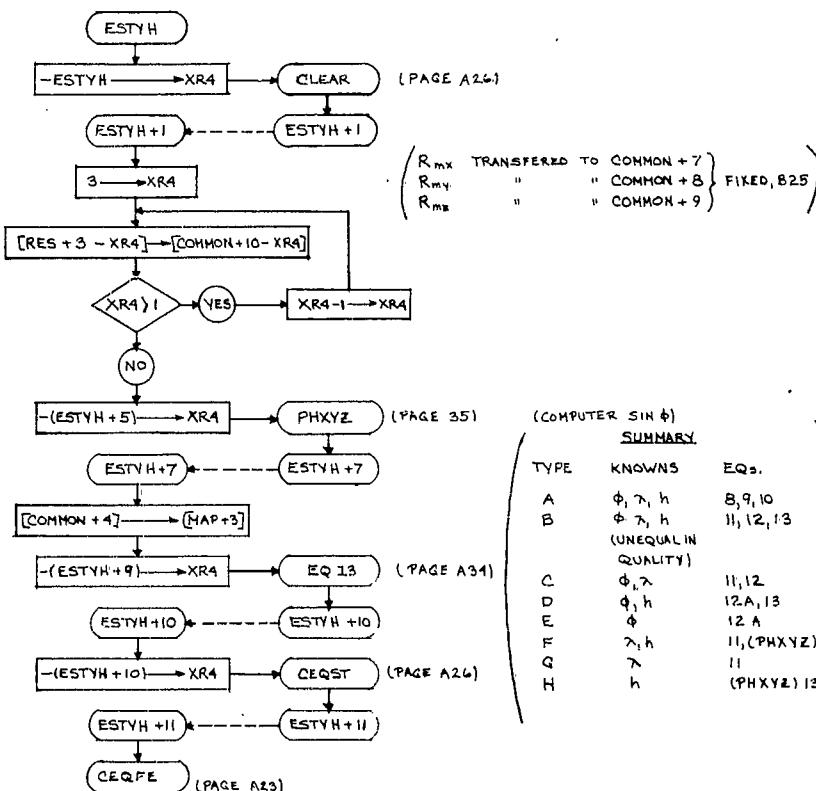
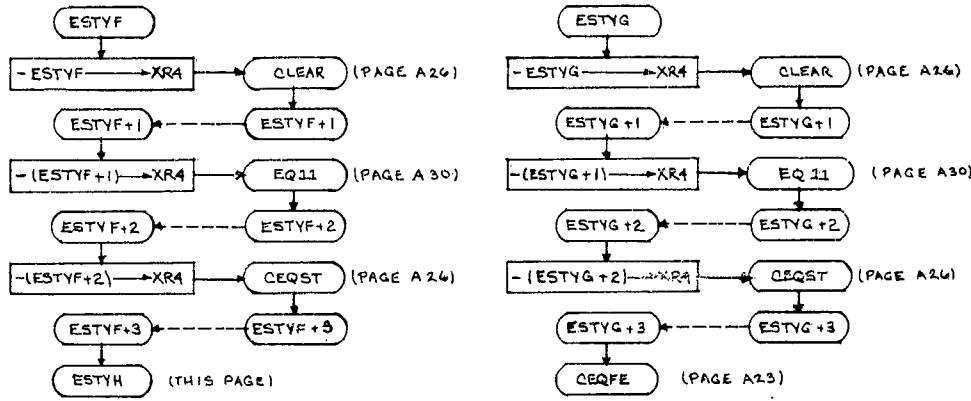


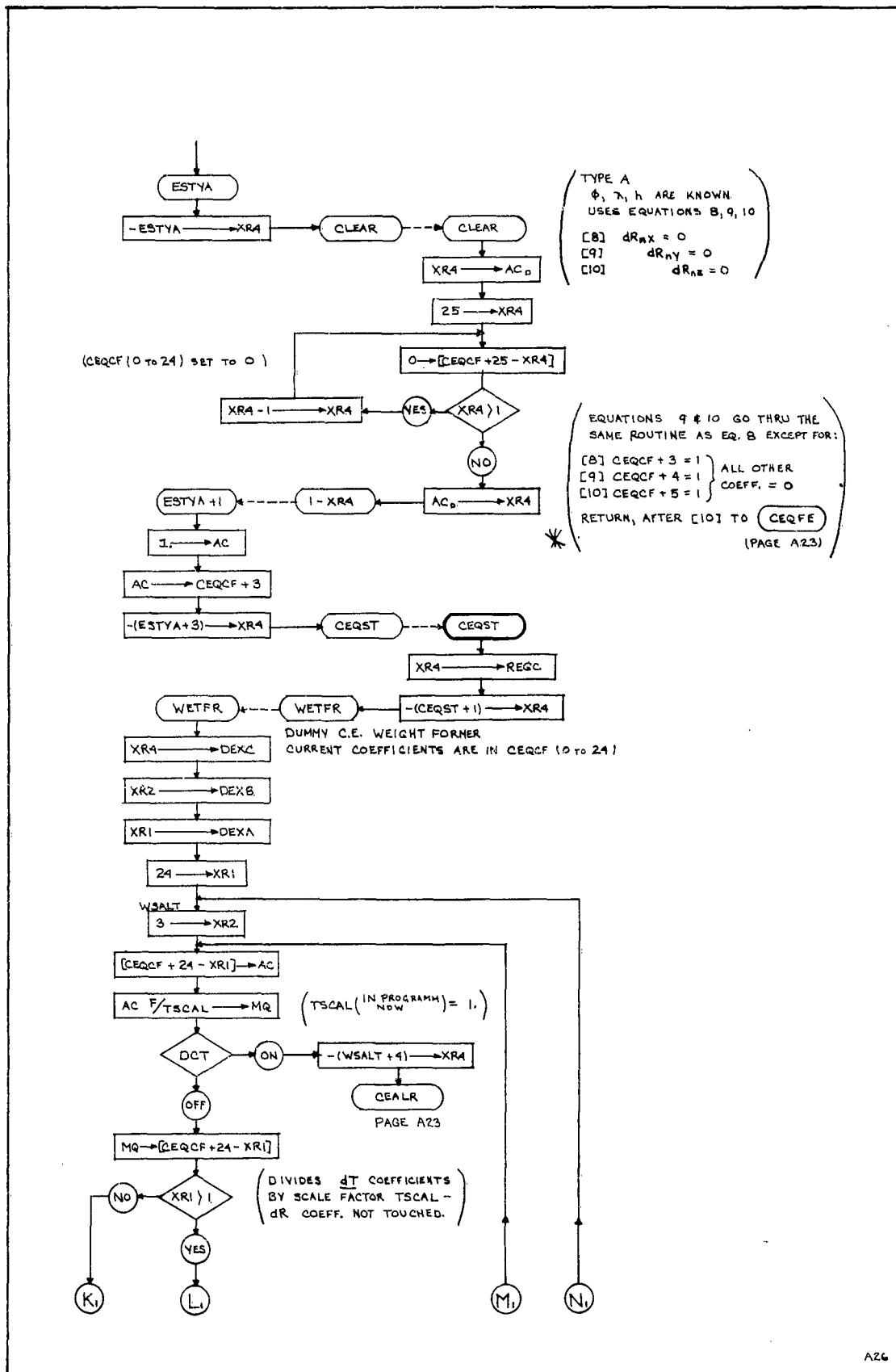


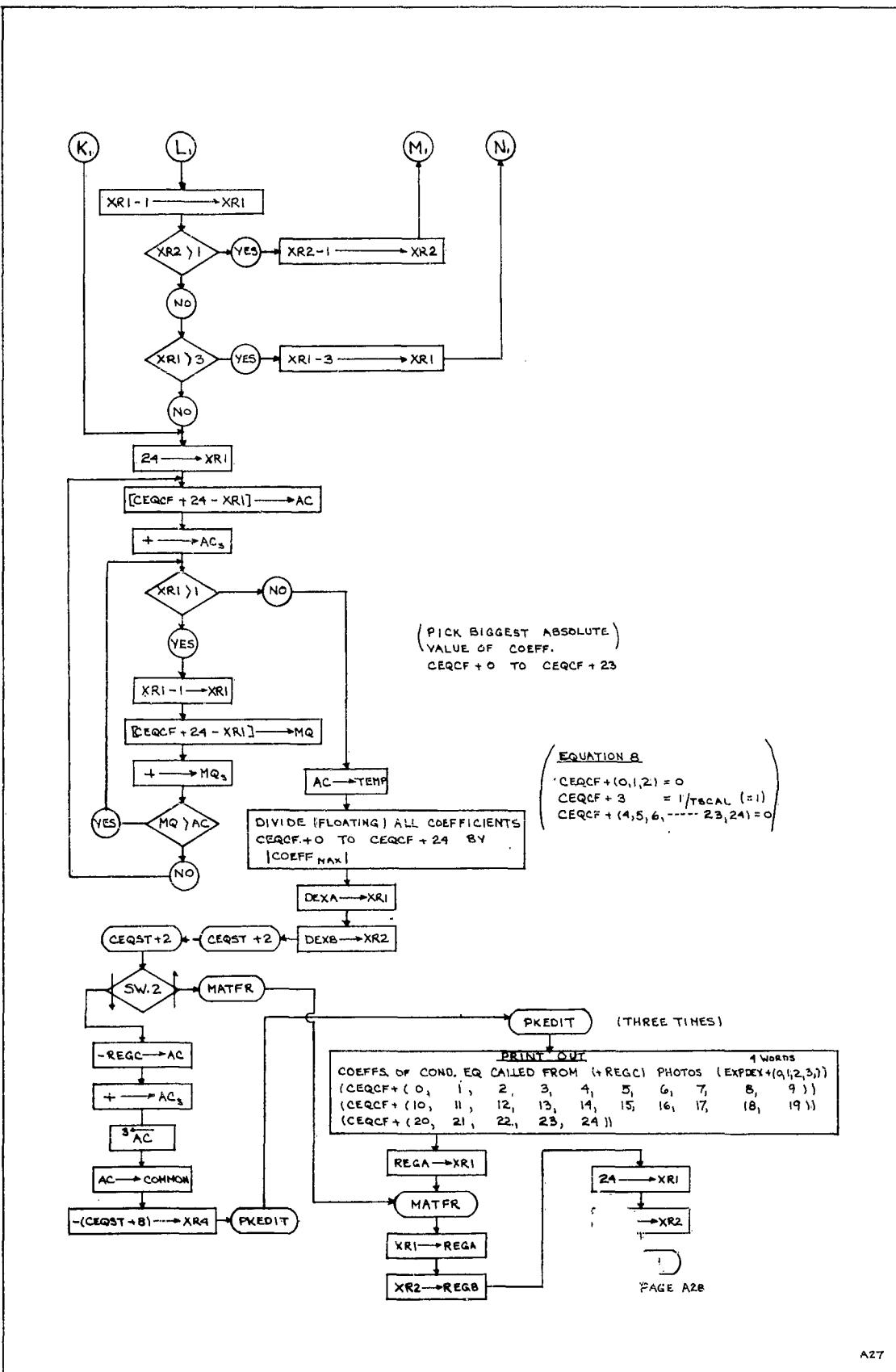


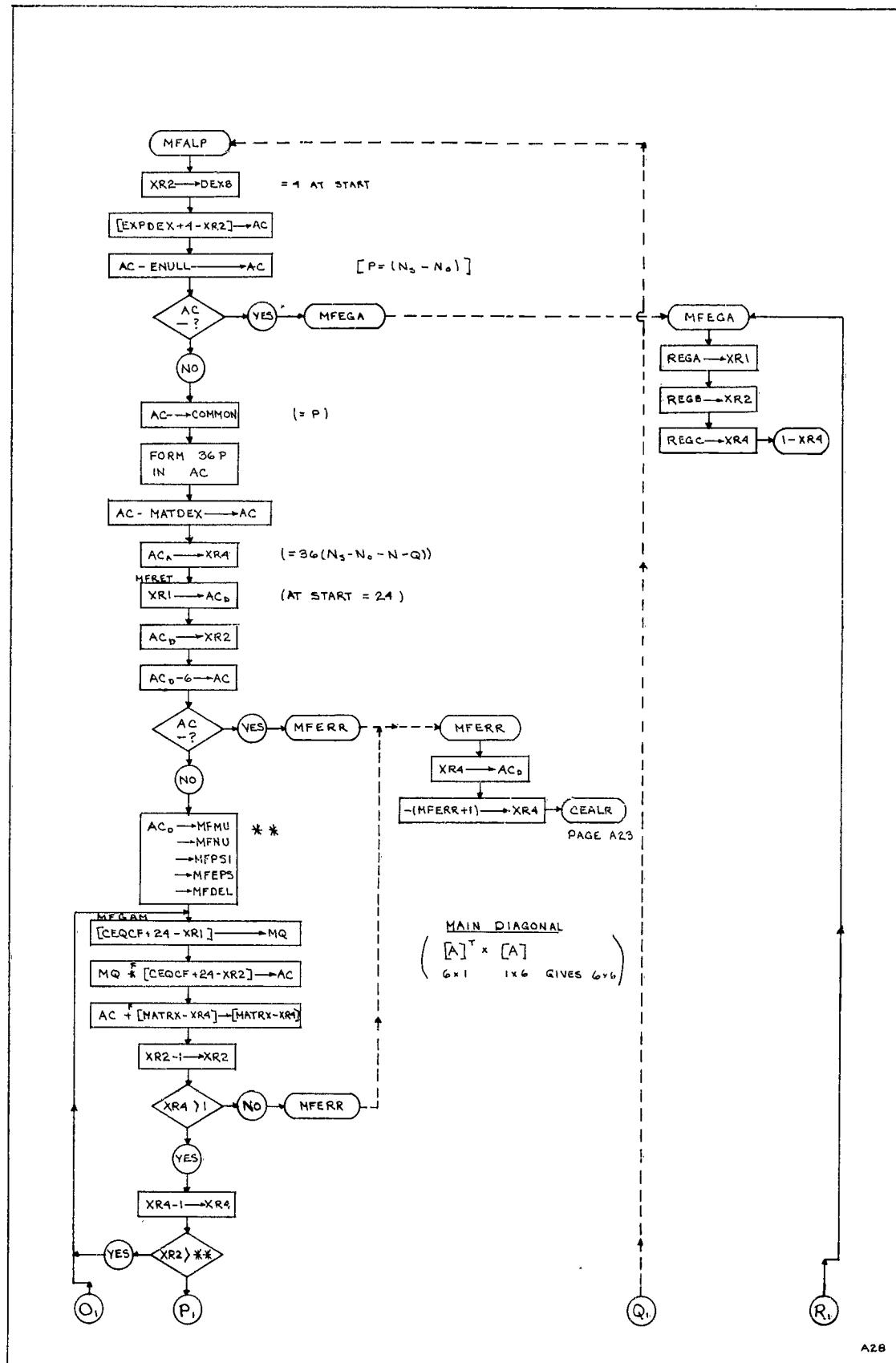


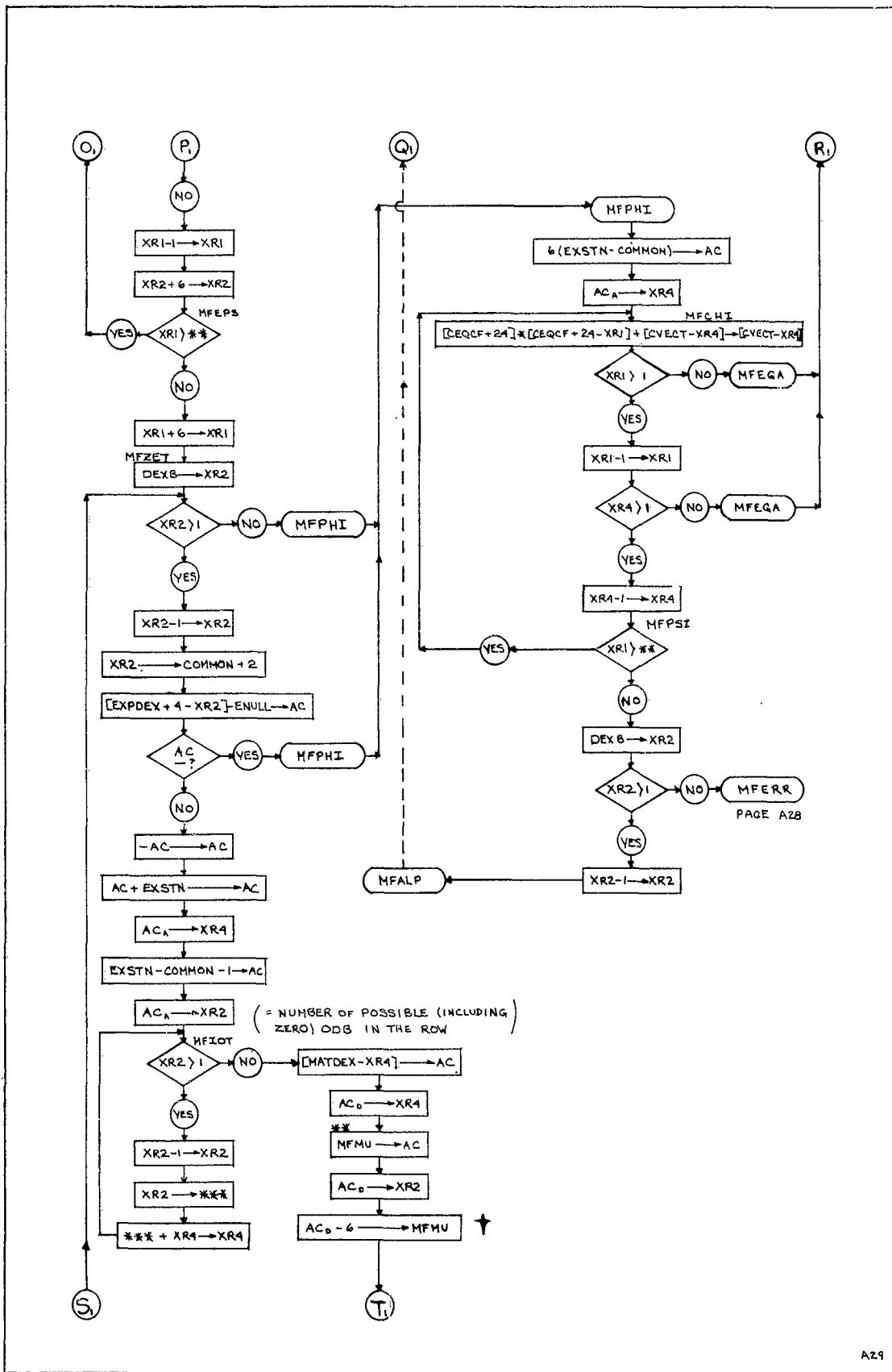


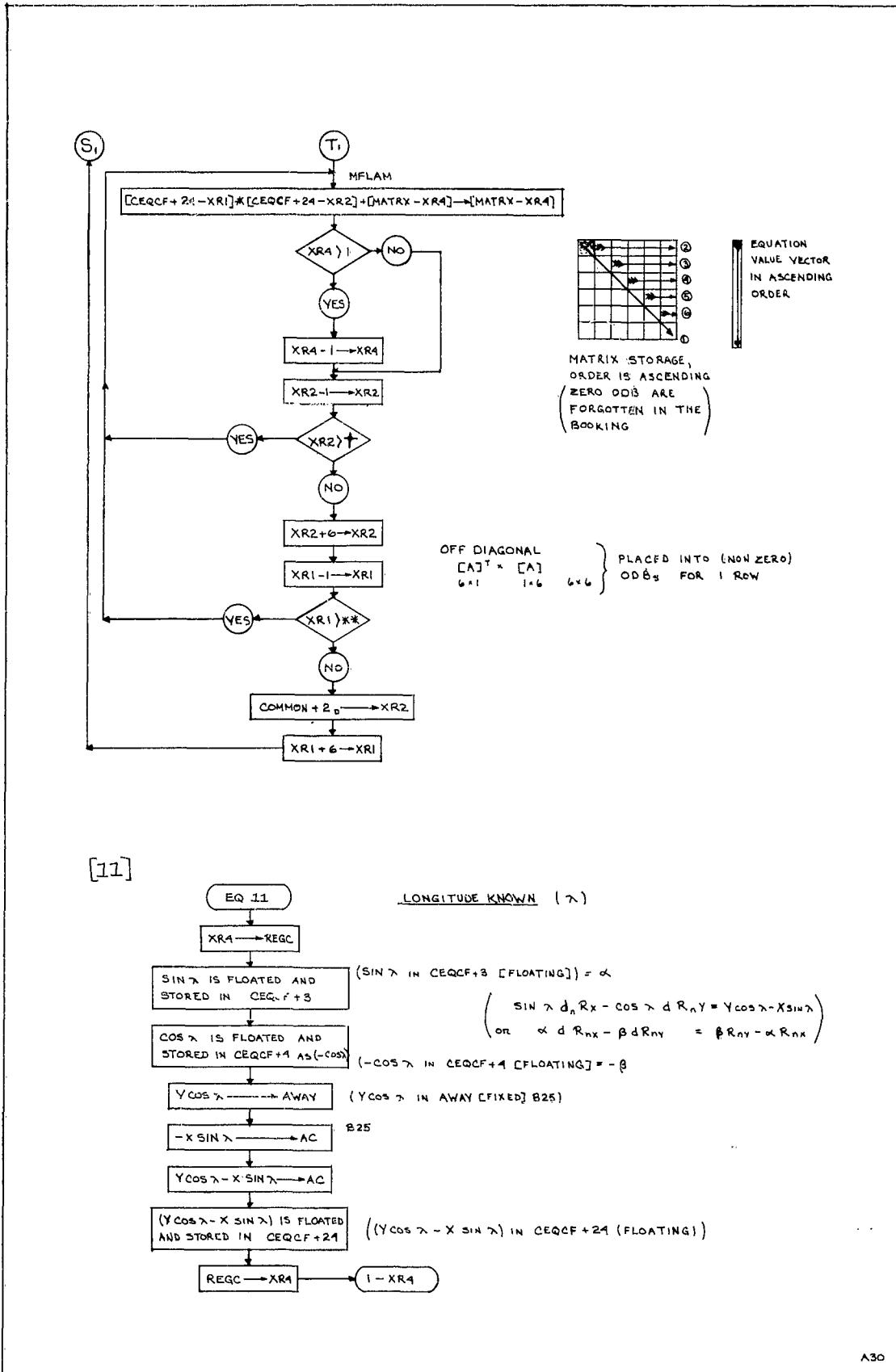




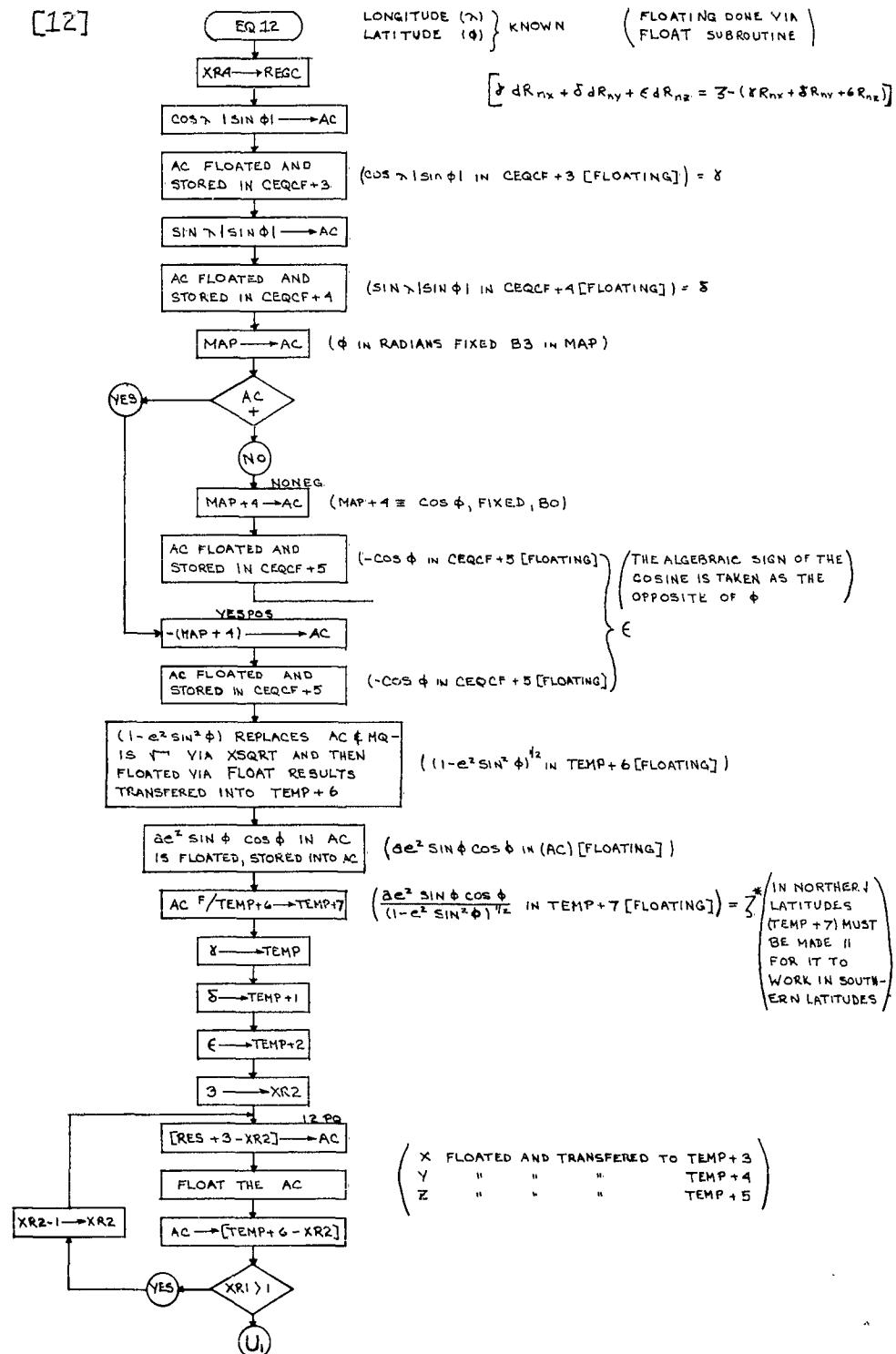


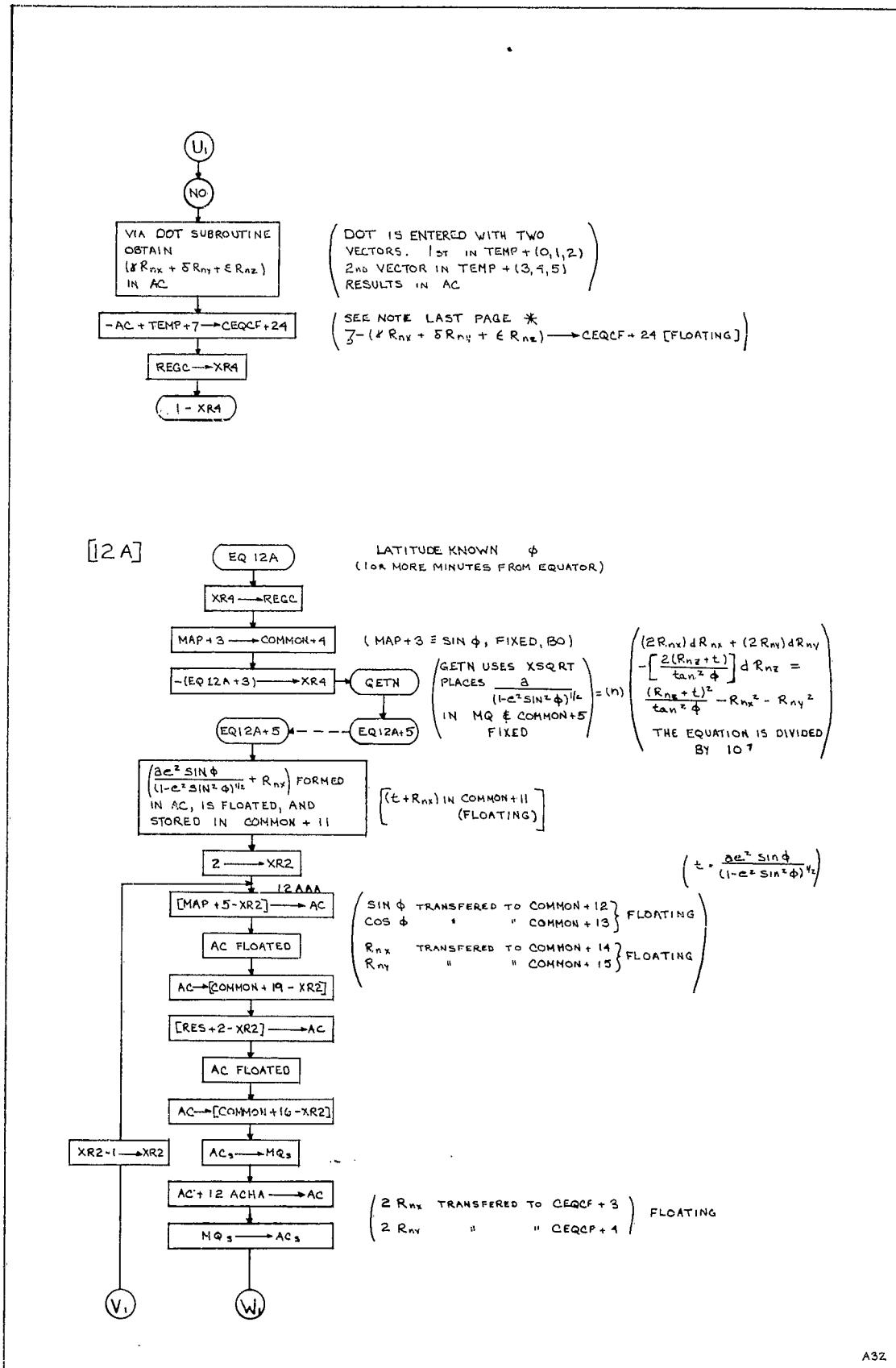


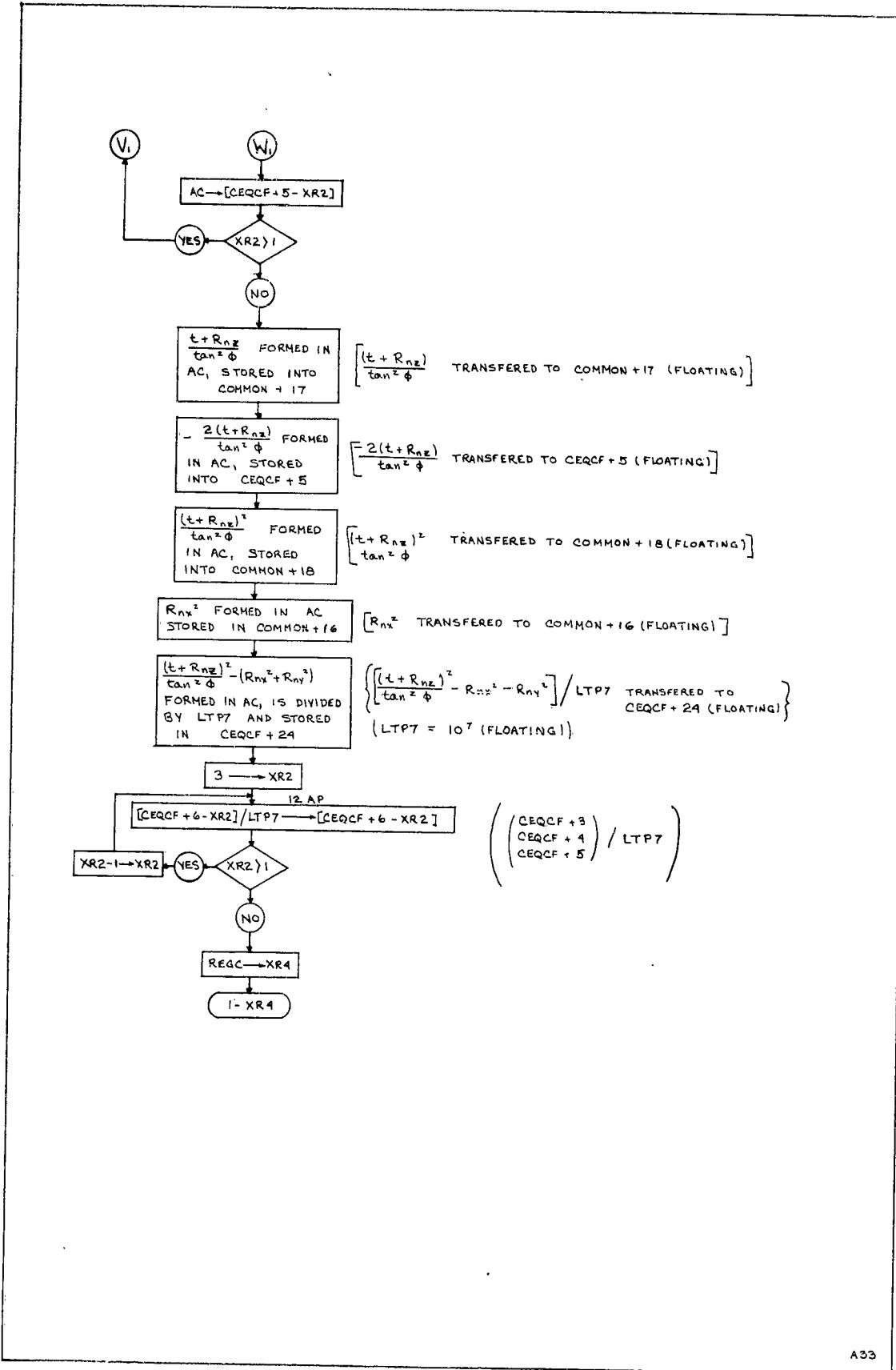




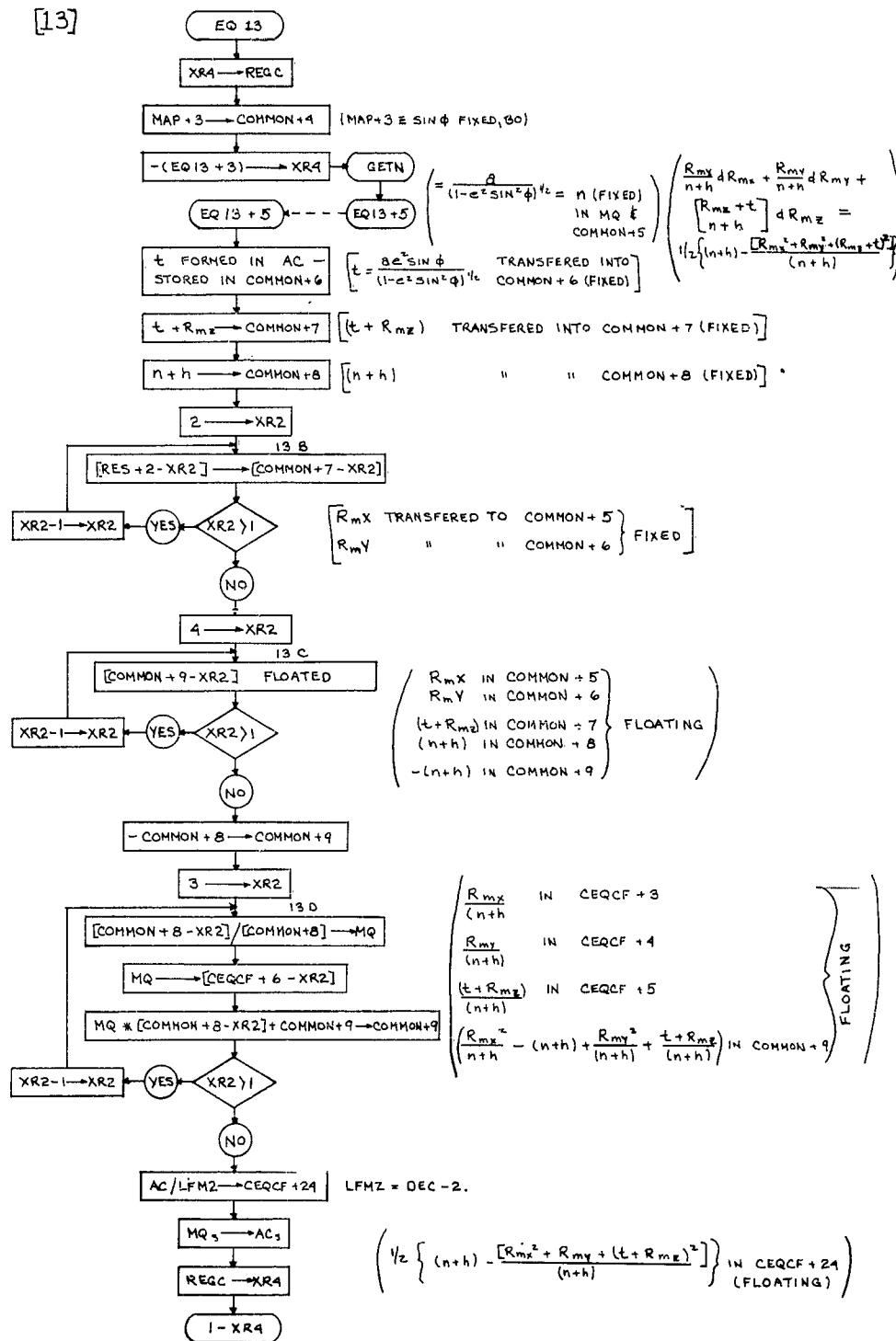
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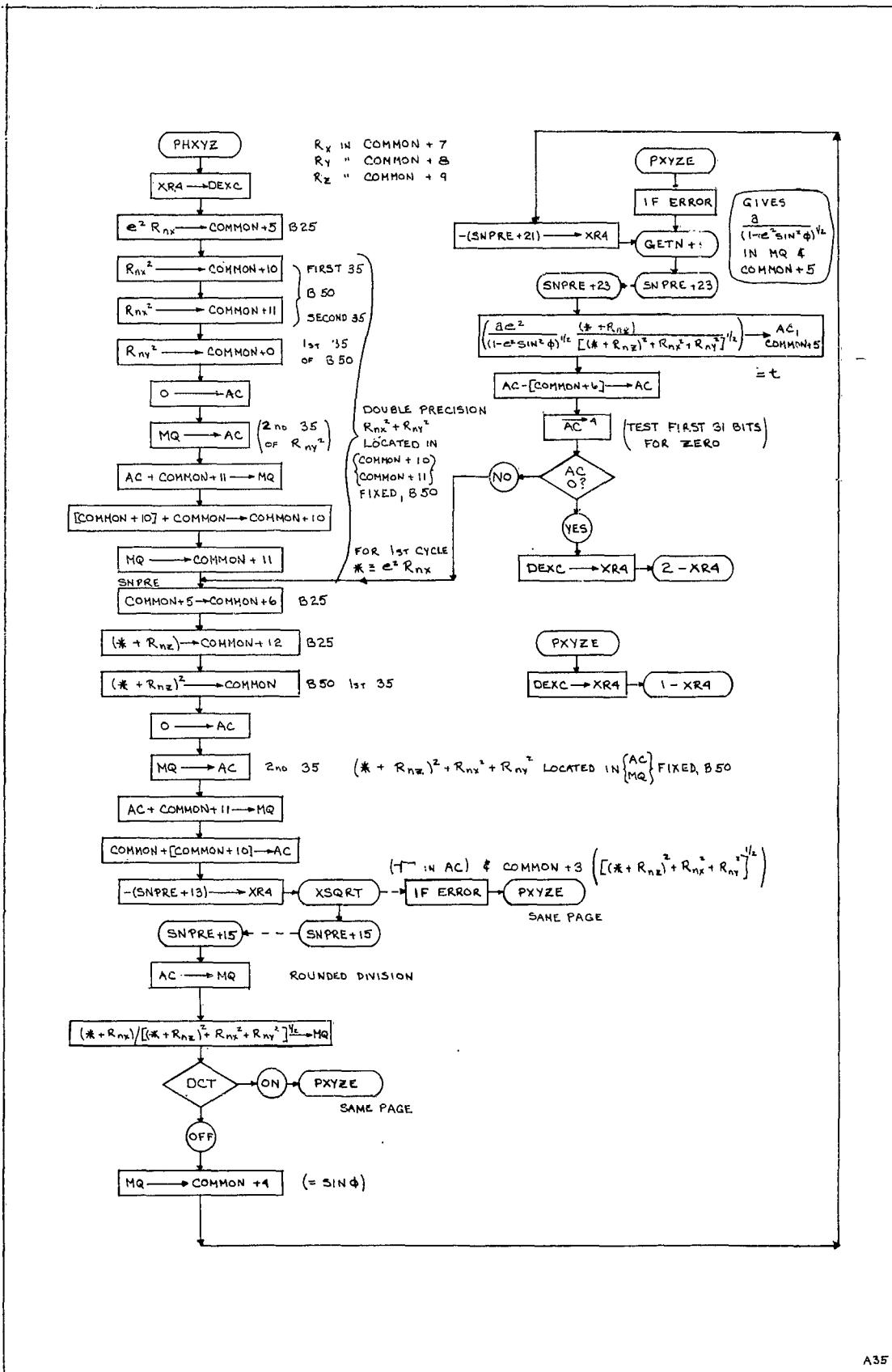


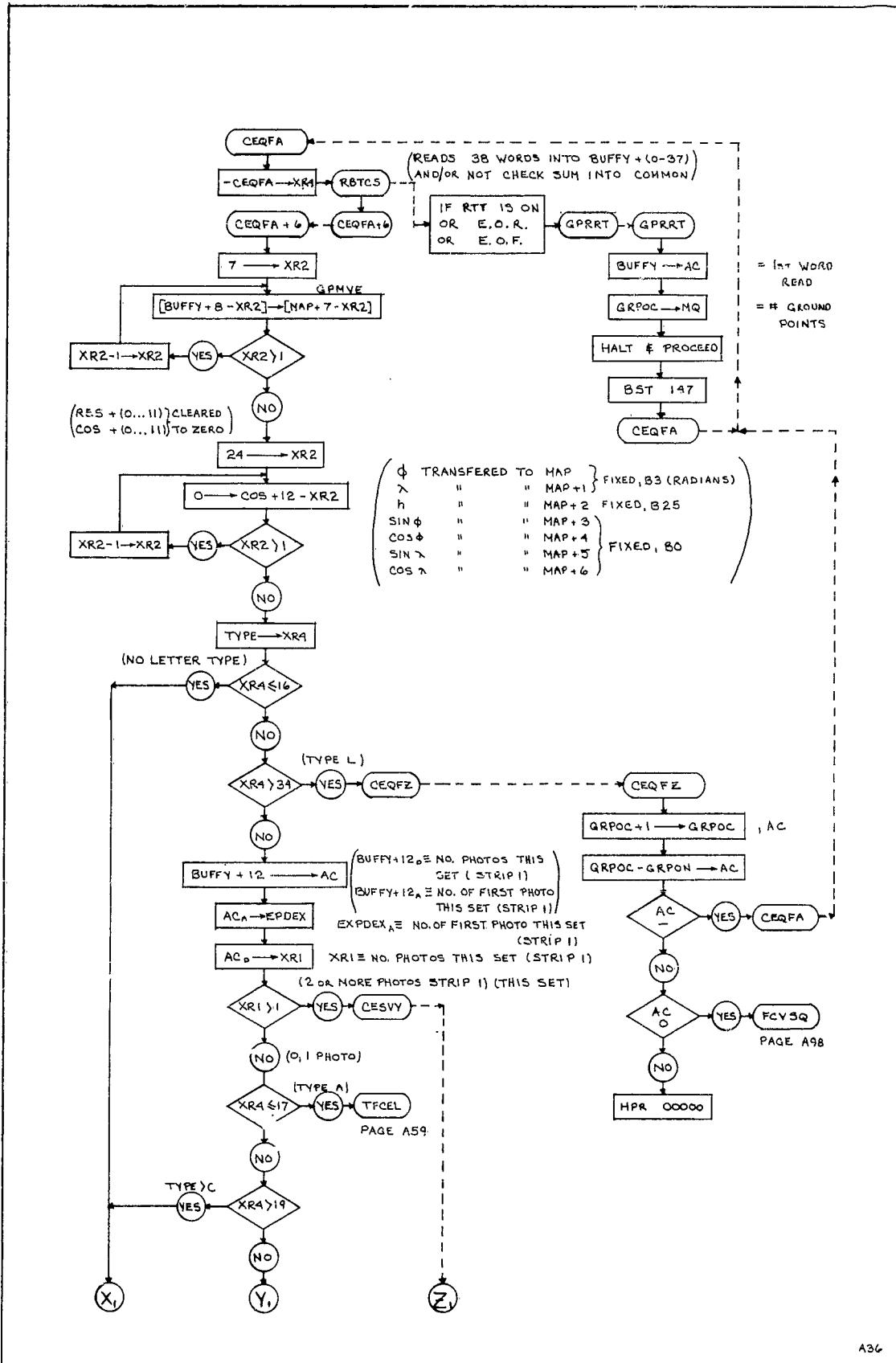


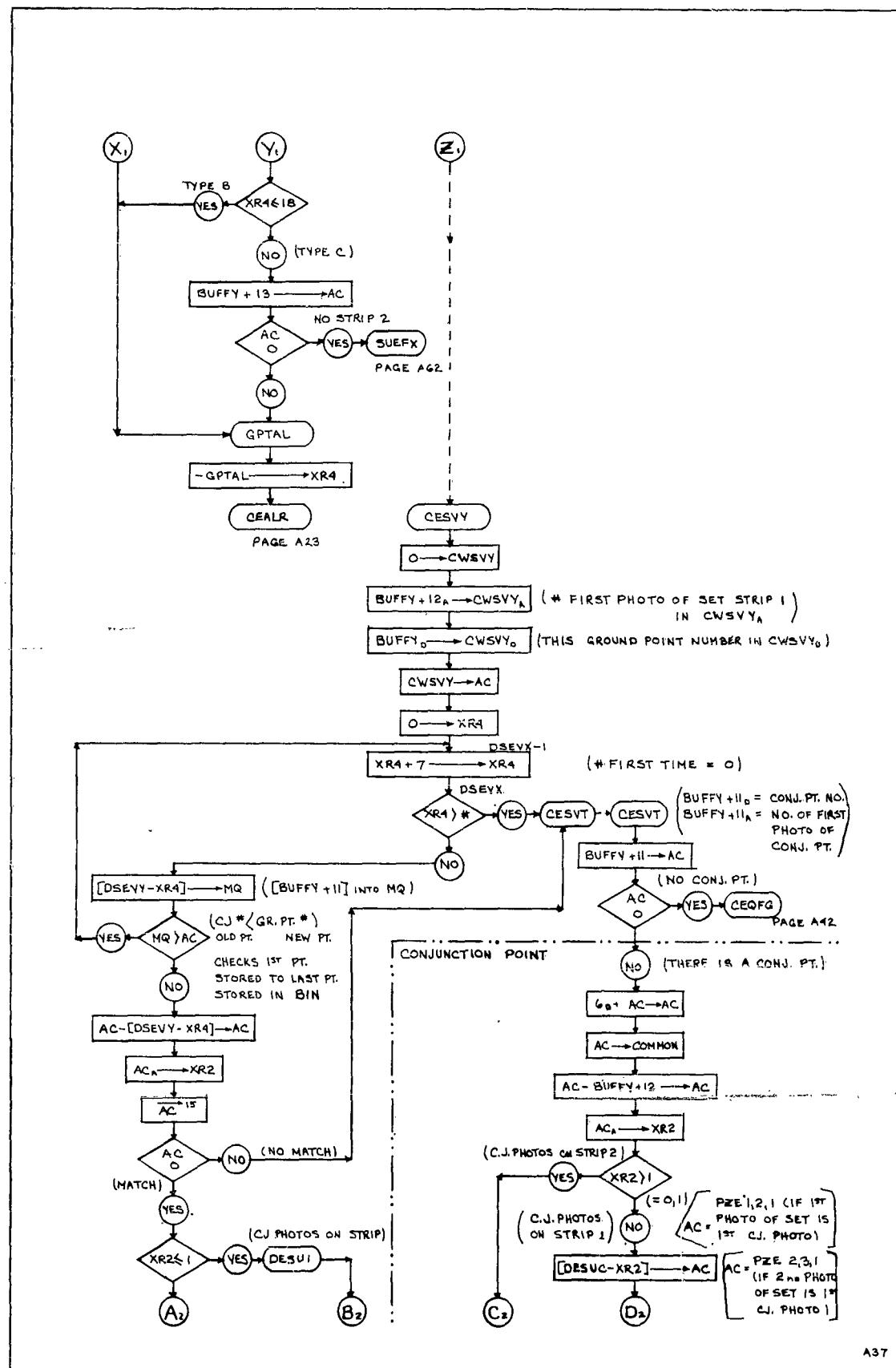


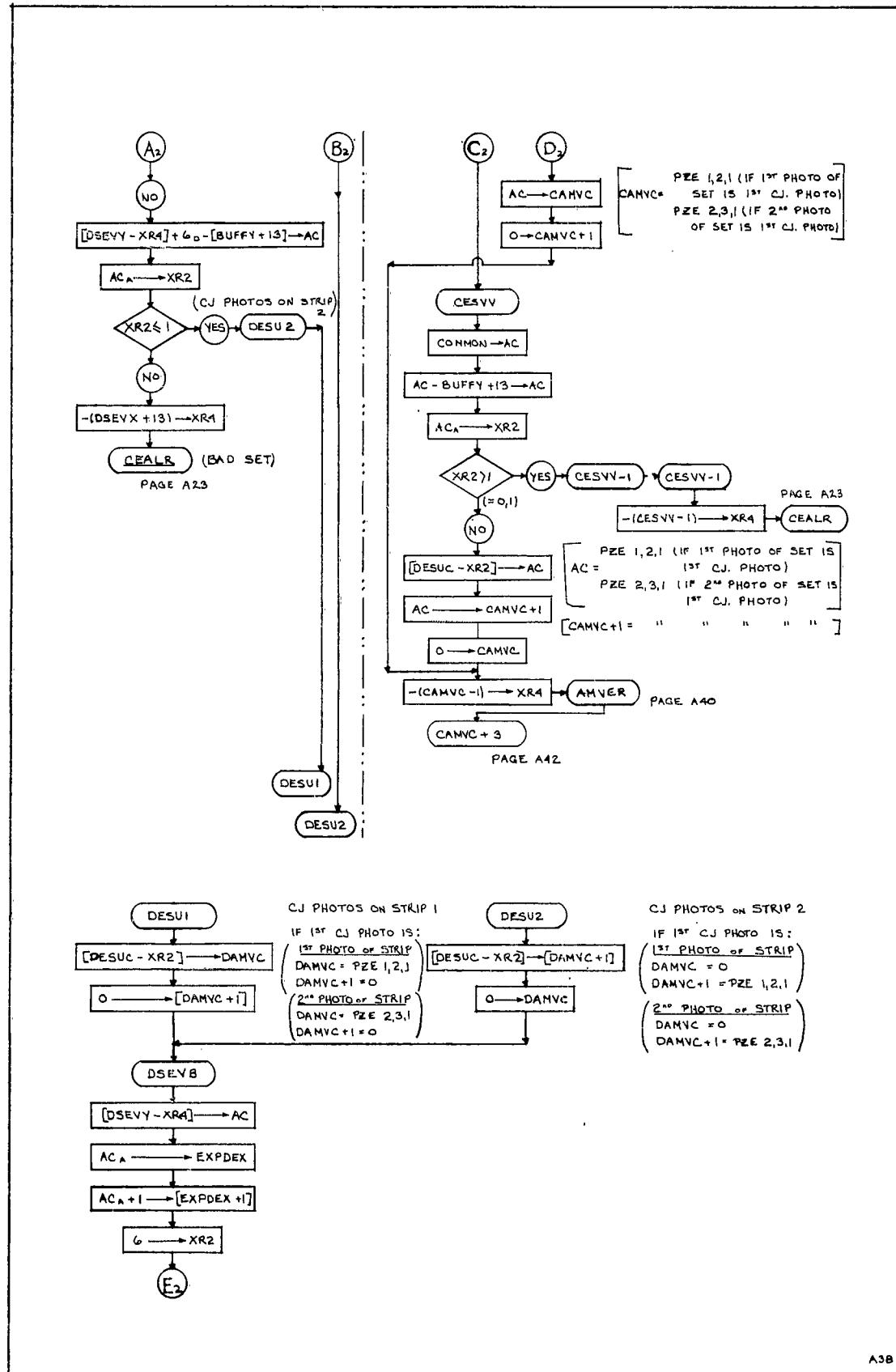
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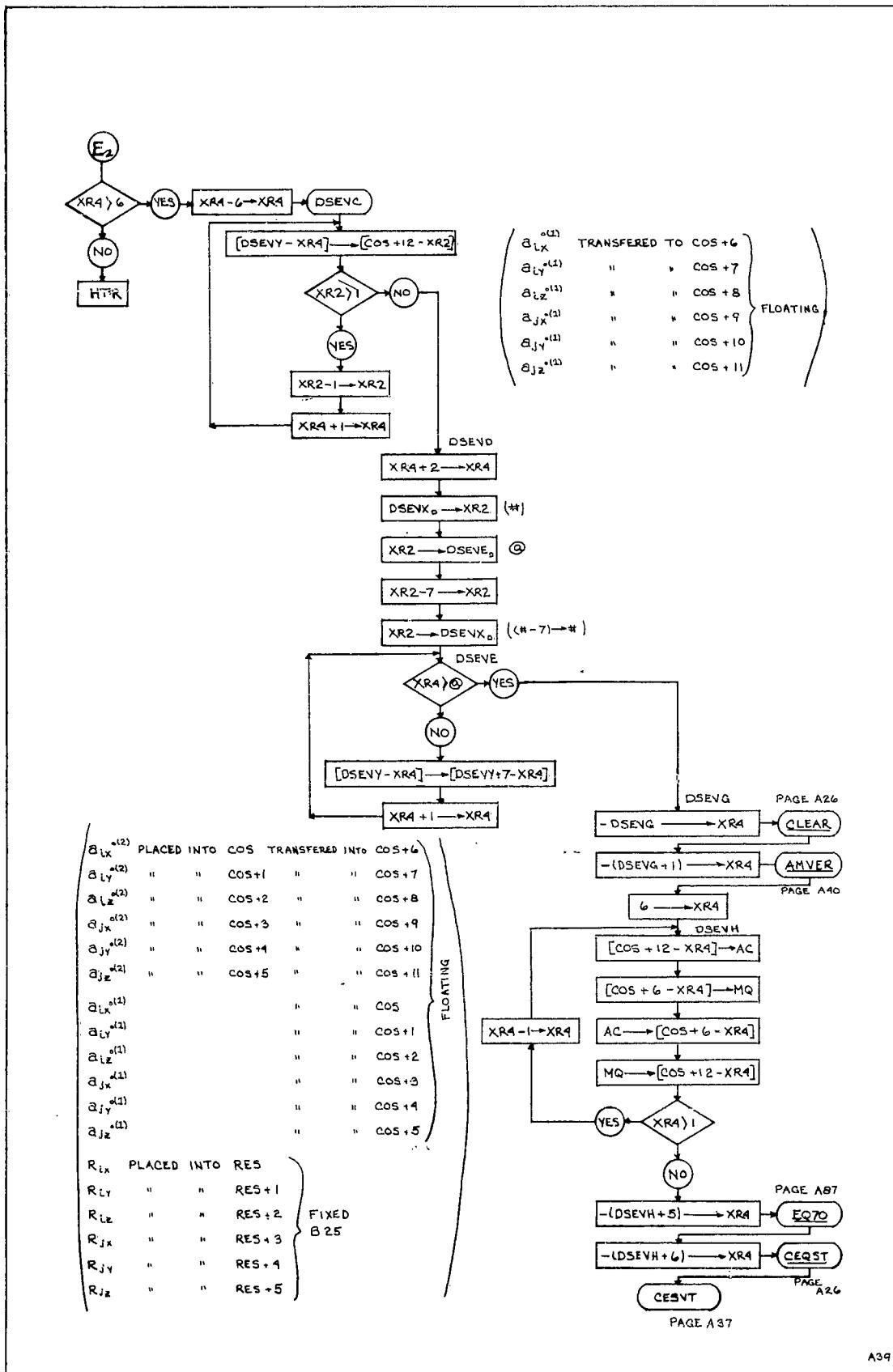


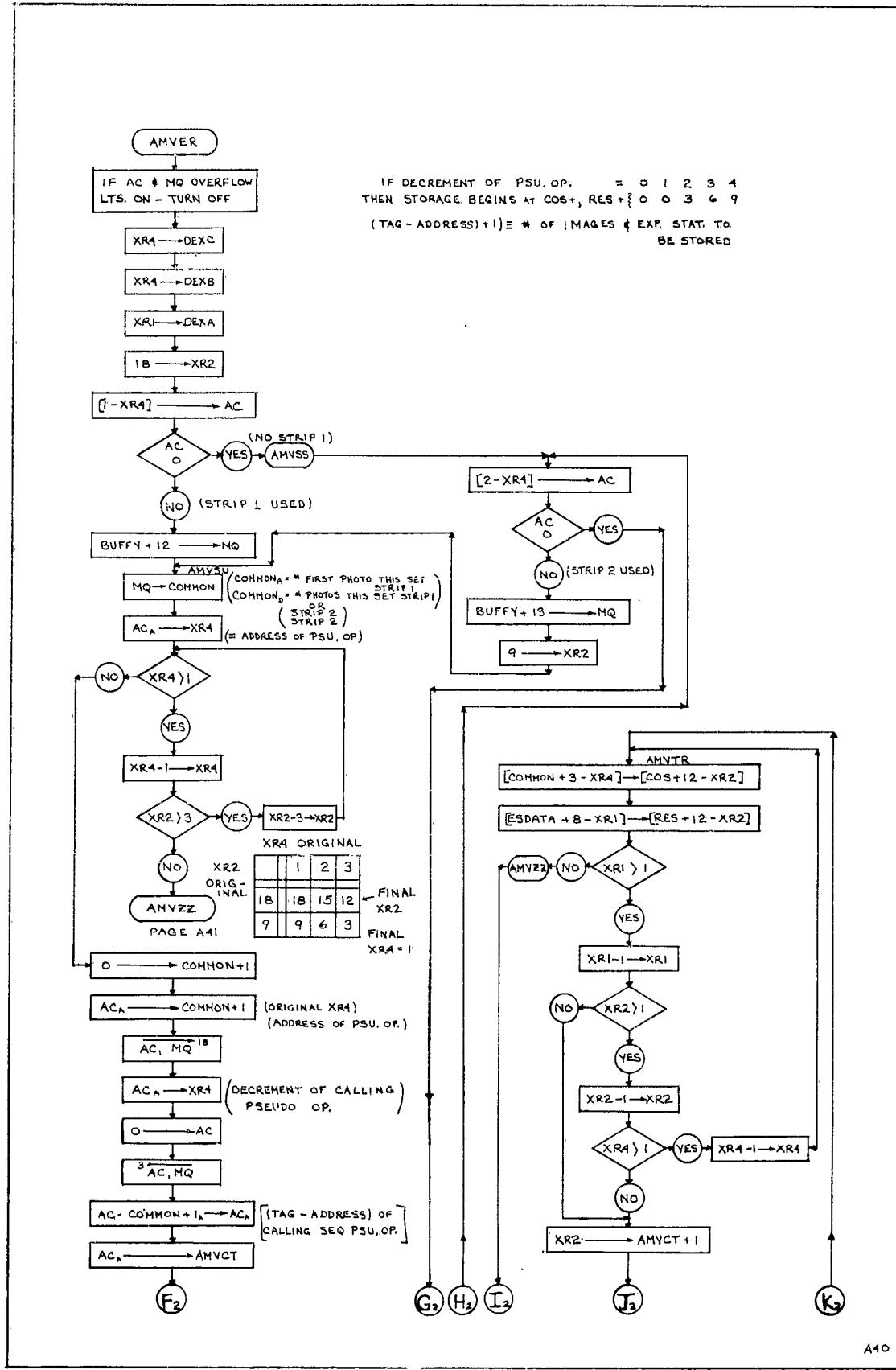


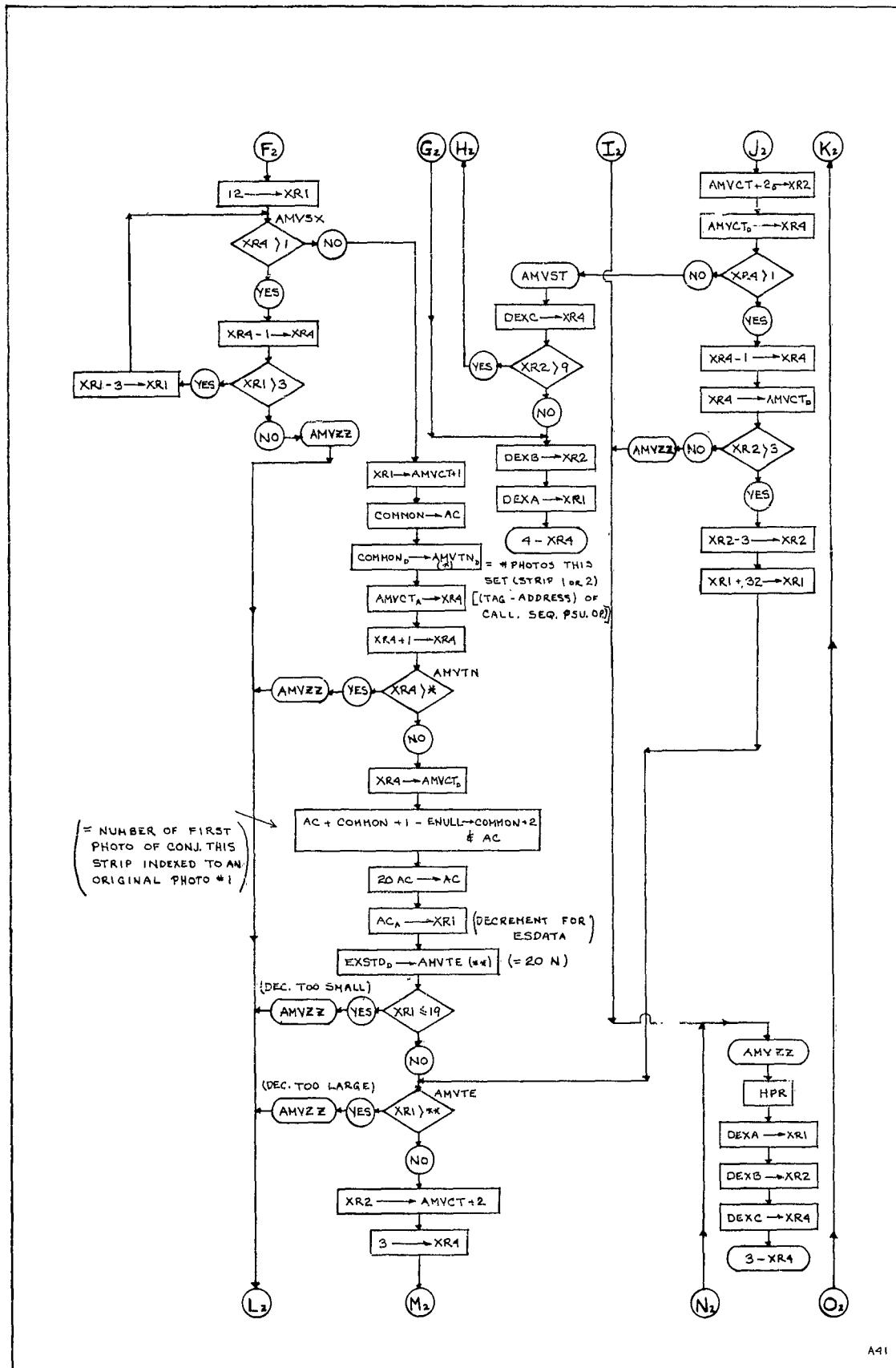


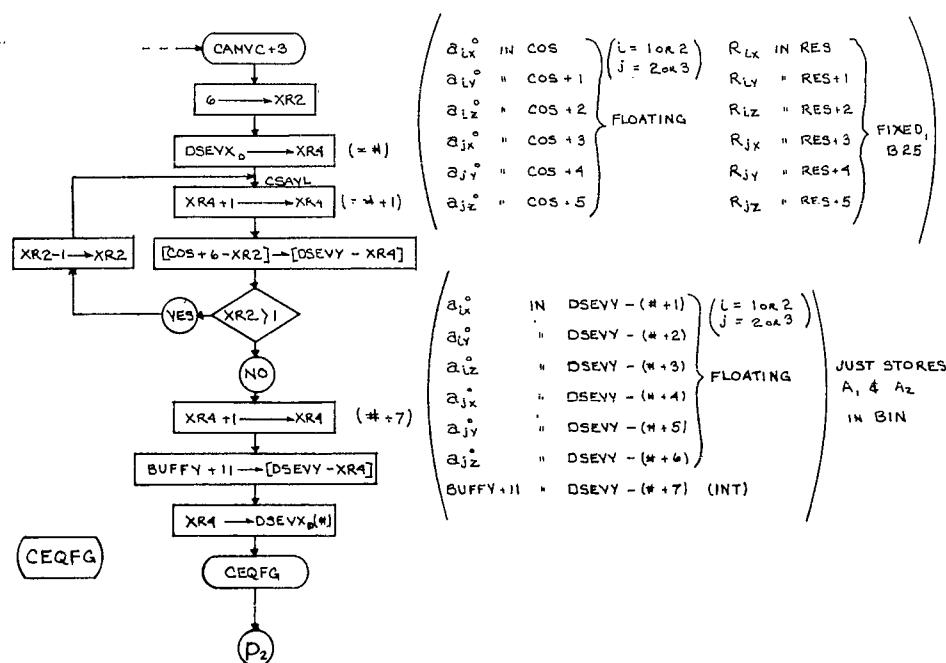
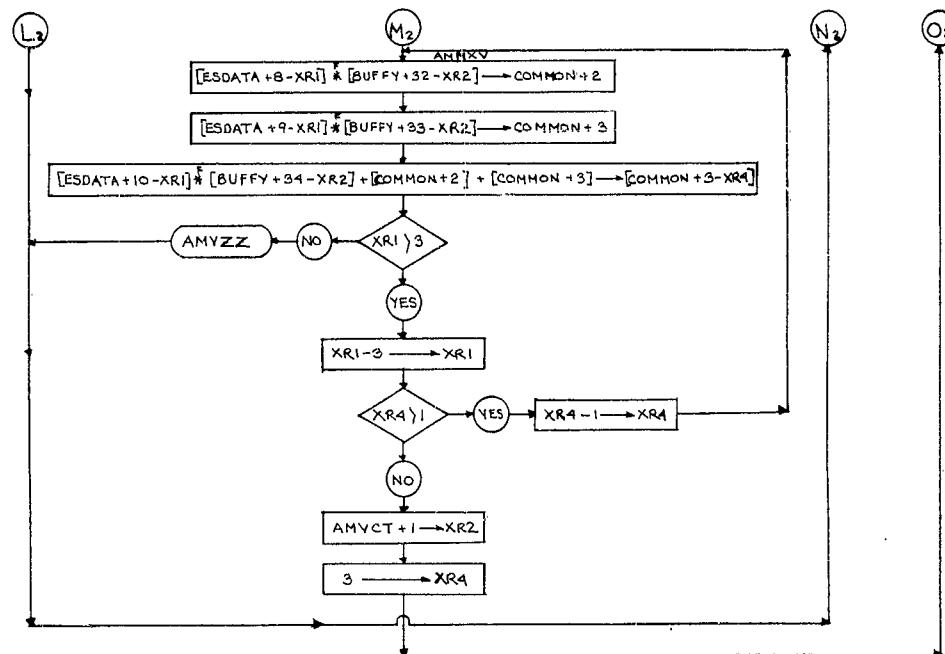


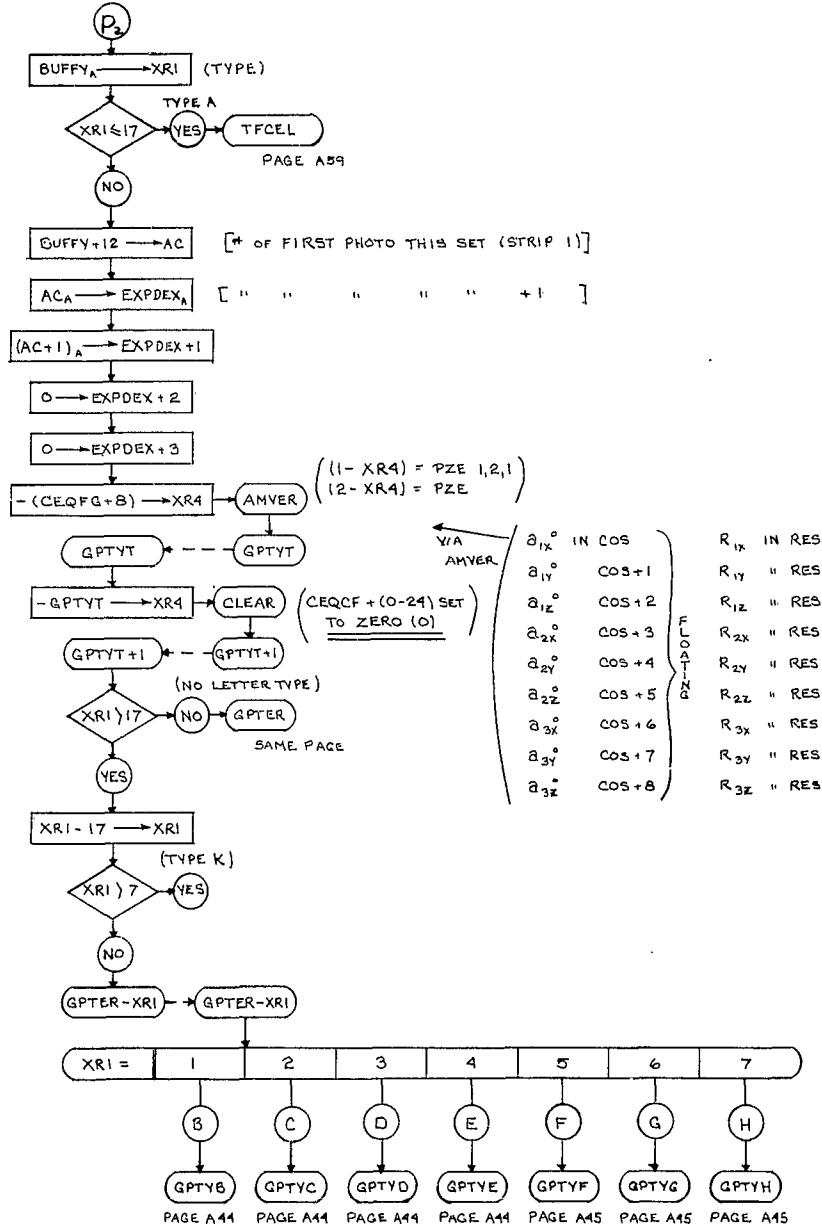


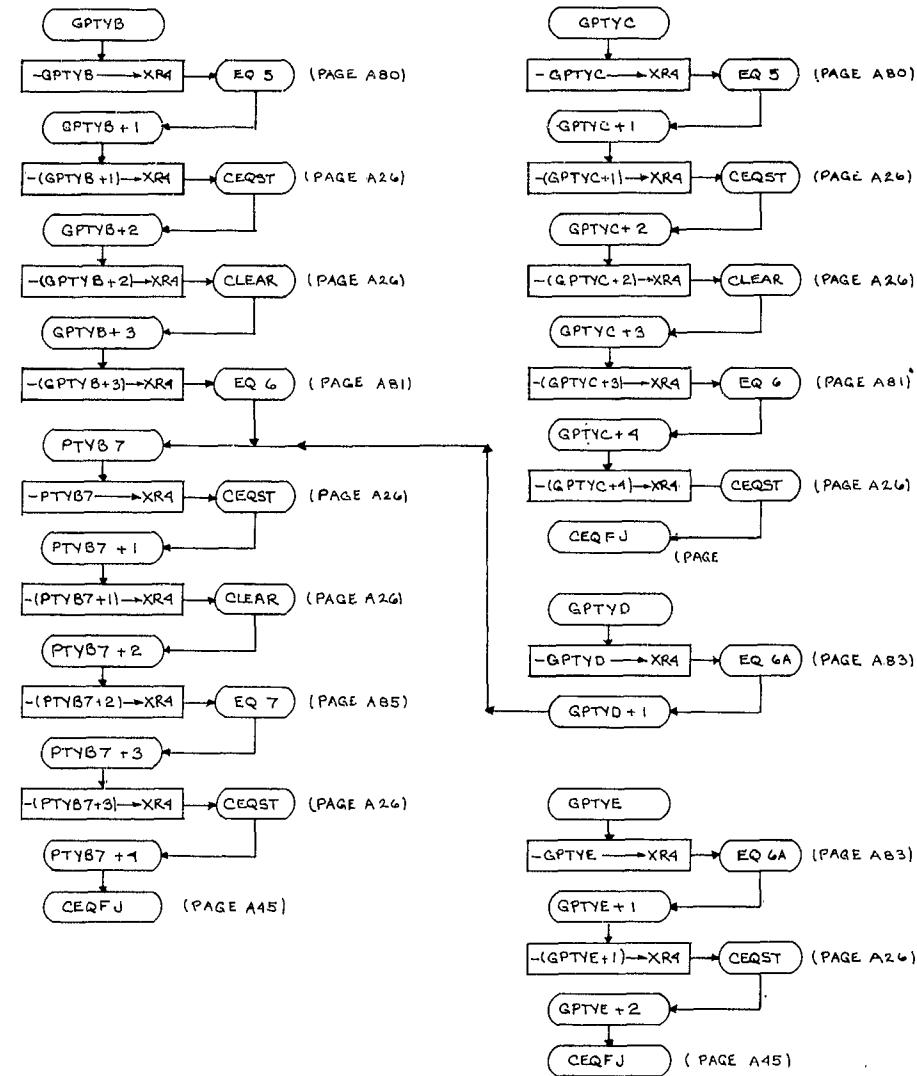


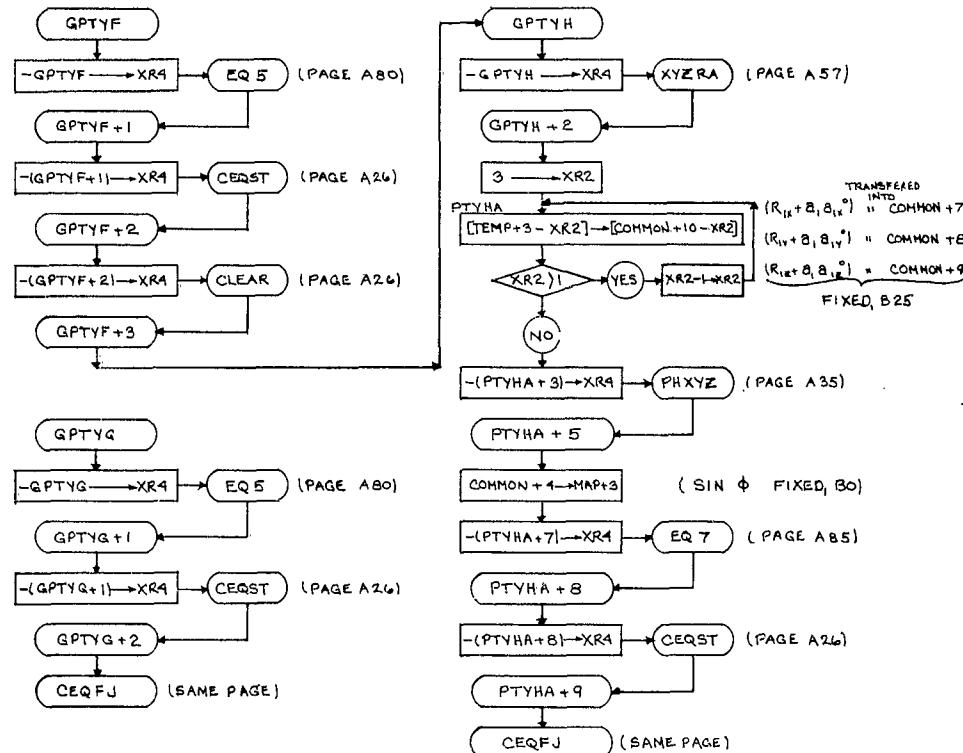




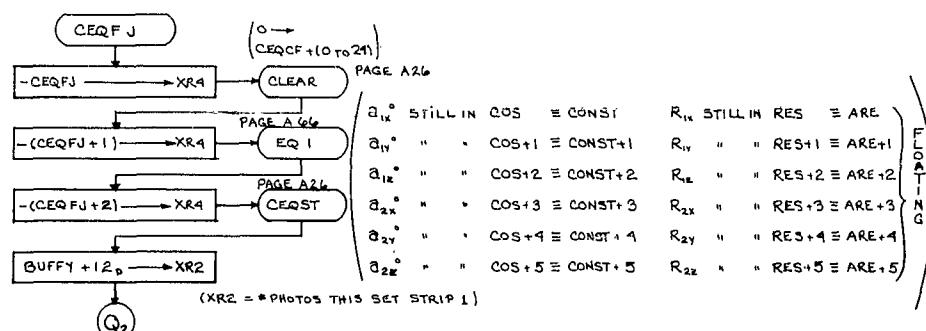


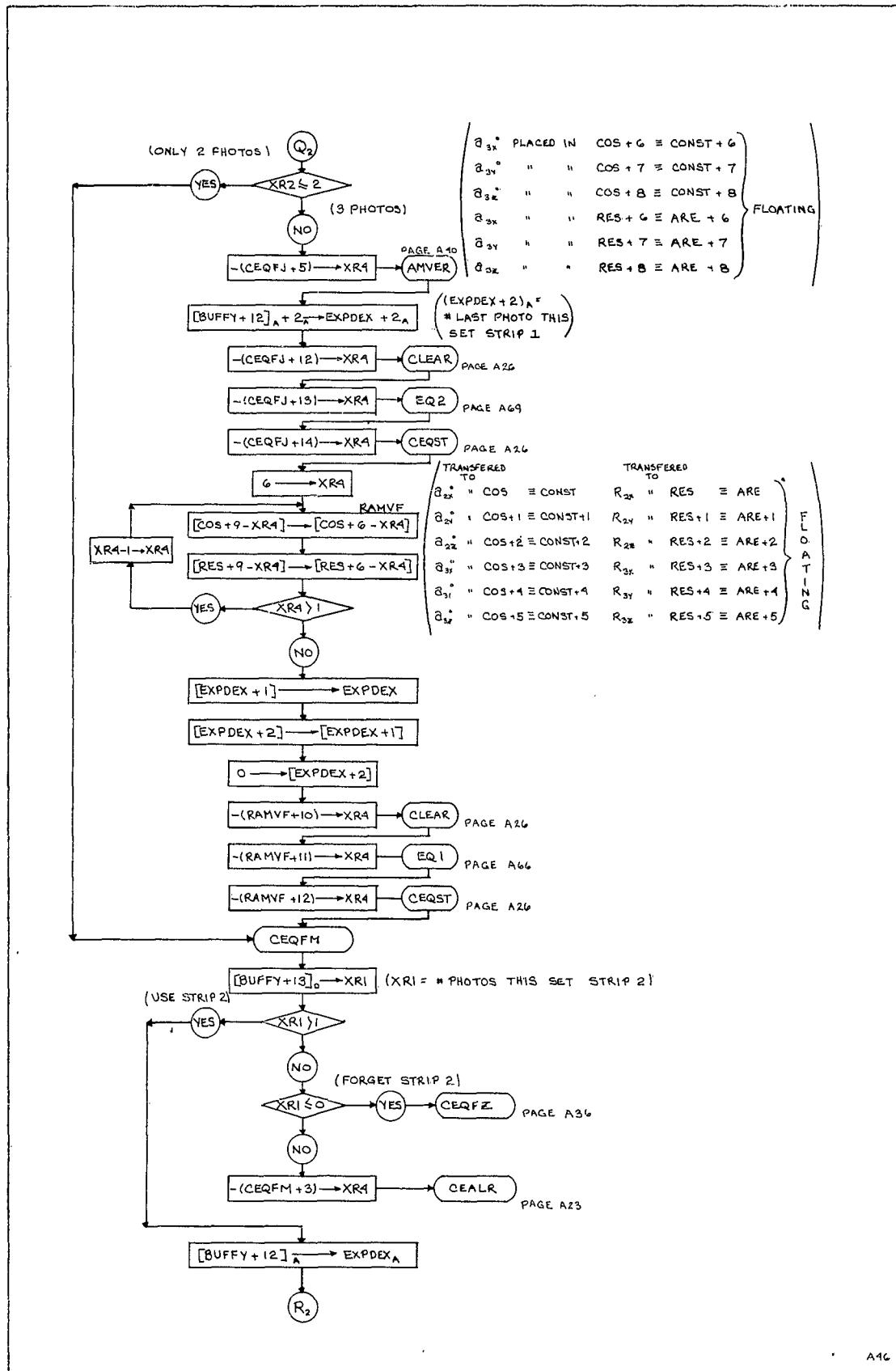


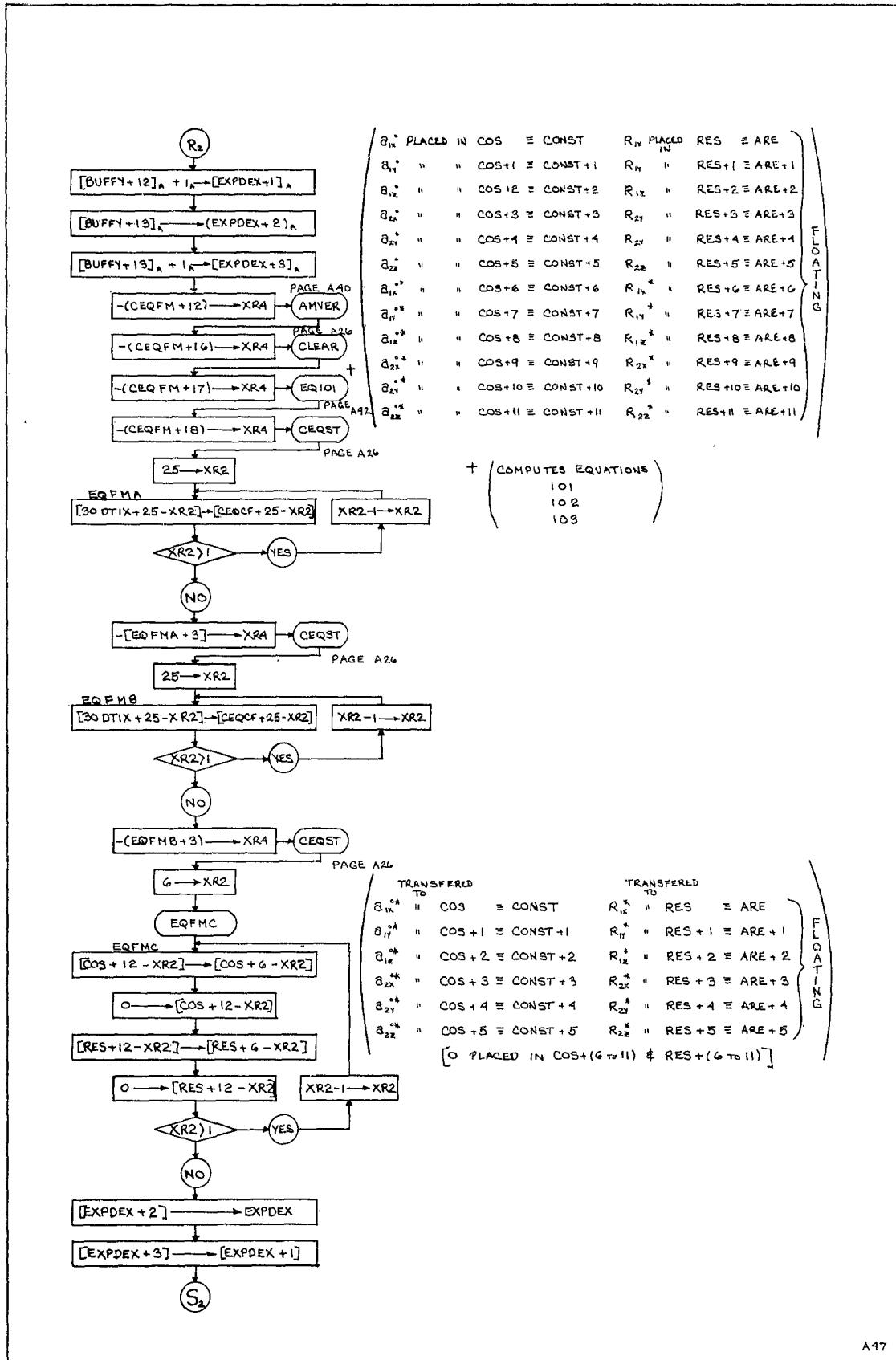


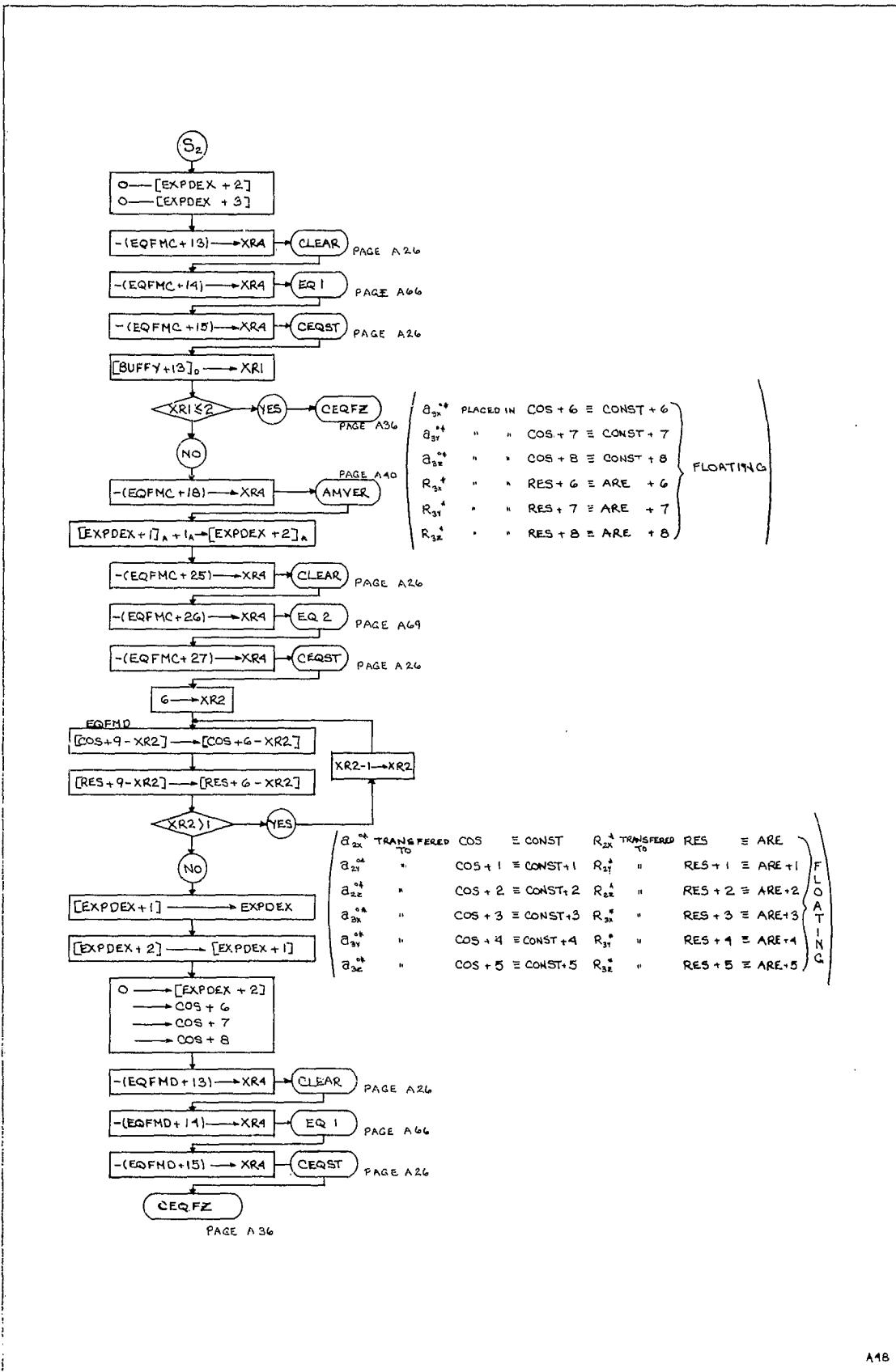


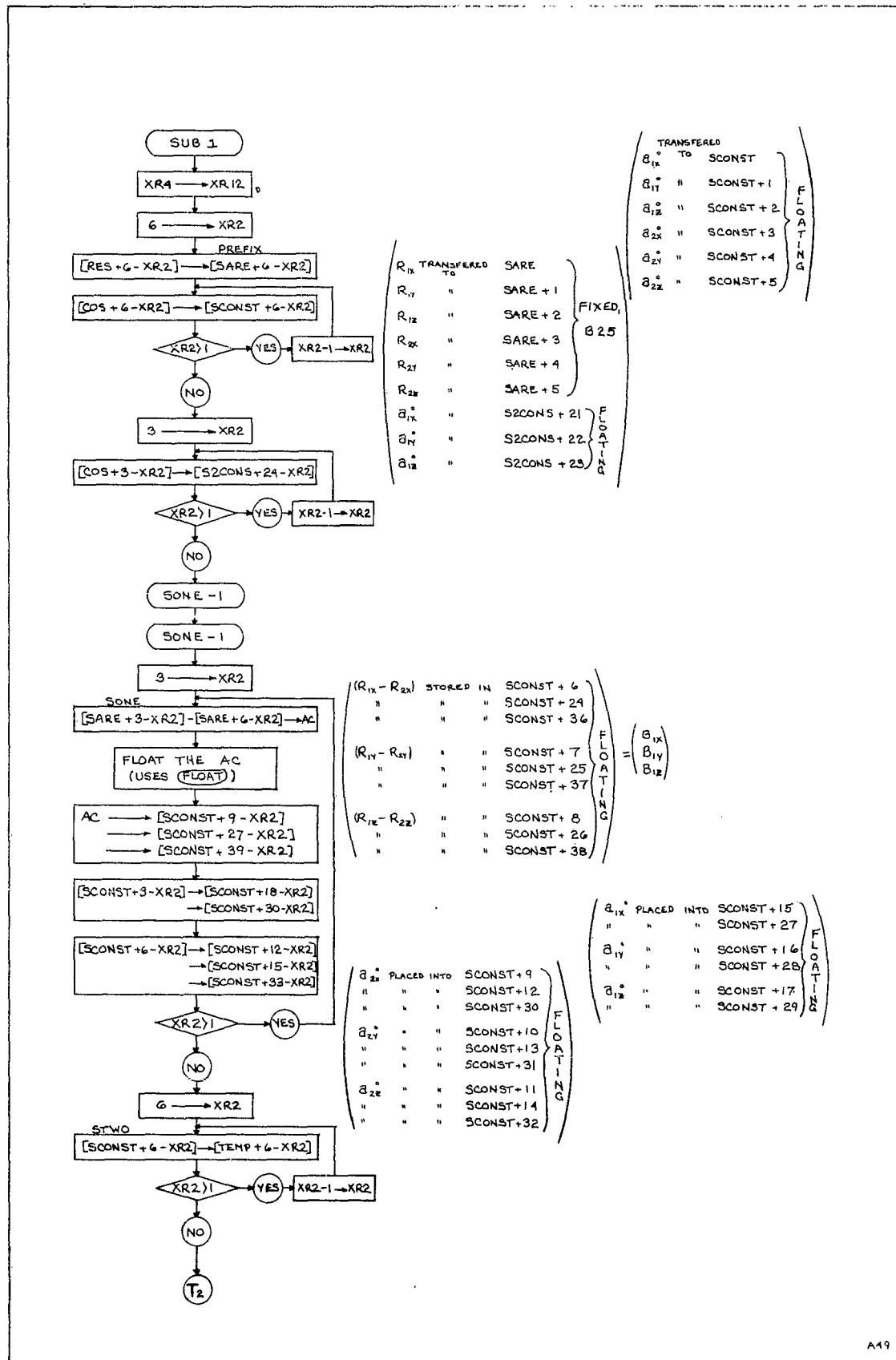
SUMMARY		
TYPE	KNOWNS	EQUATIONS
B	ϕ, γ, h	5, 6, 7
C	ϕ, γ	5, 6
D	ϕ, h	6A, 7
E	ϕ	6A
F	γ, h	5, (XYZRA, PHXYZ) 7
G	γ	5
H	h	(XYZRA, PHXYZ) 7

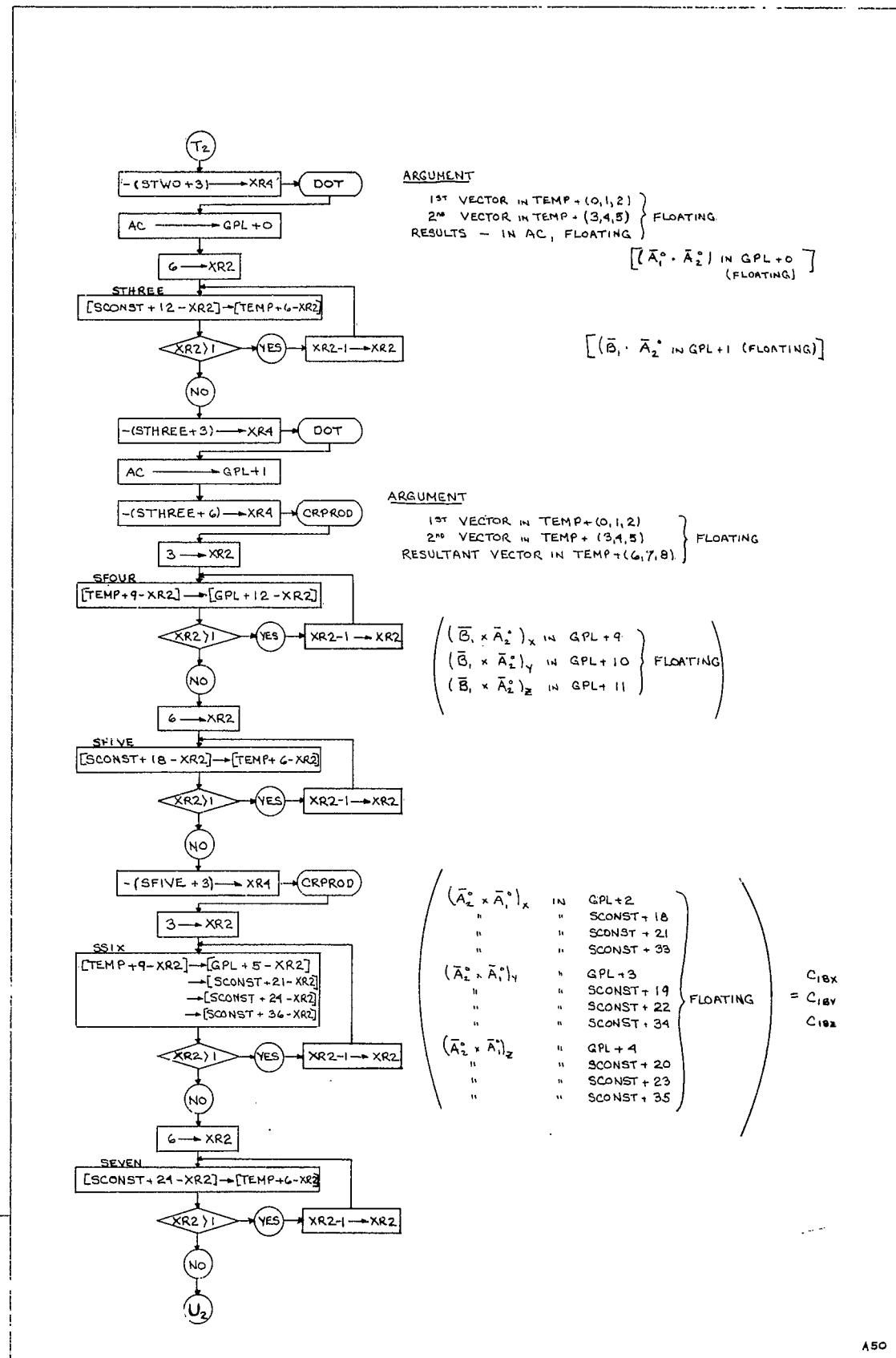


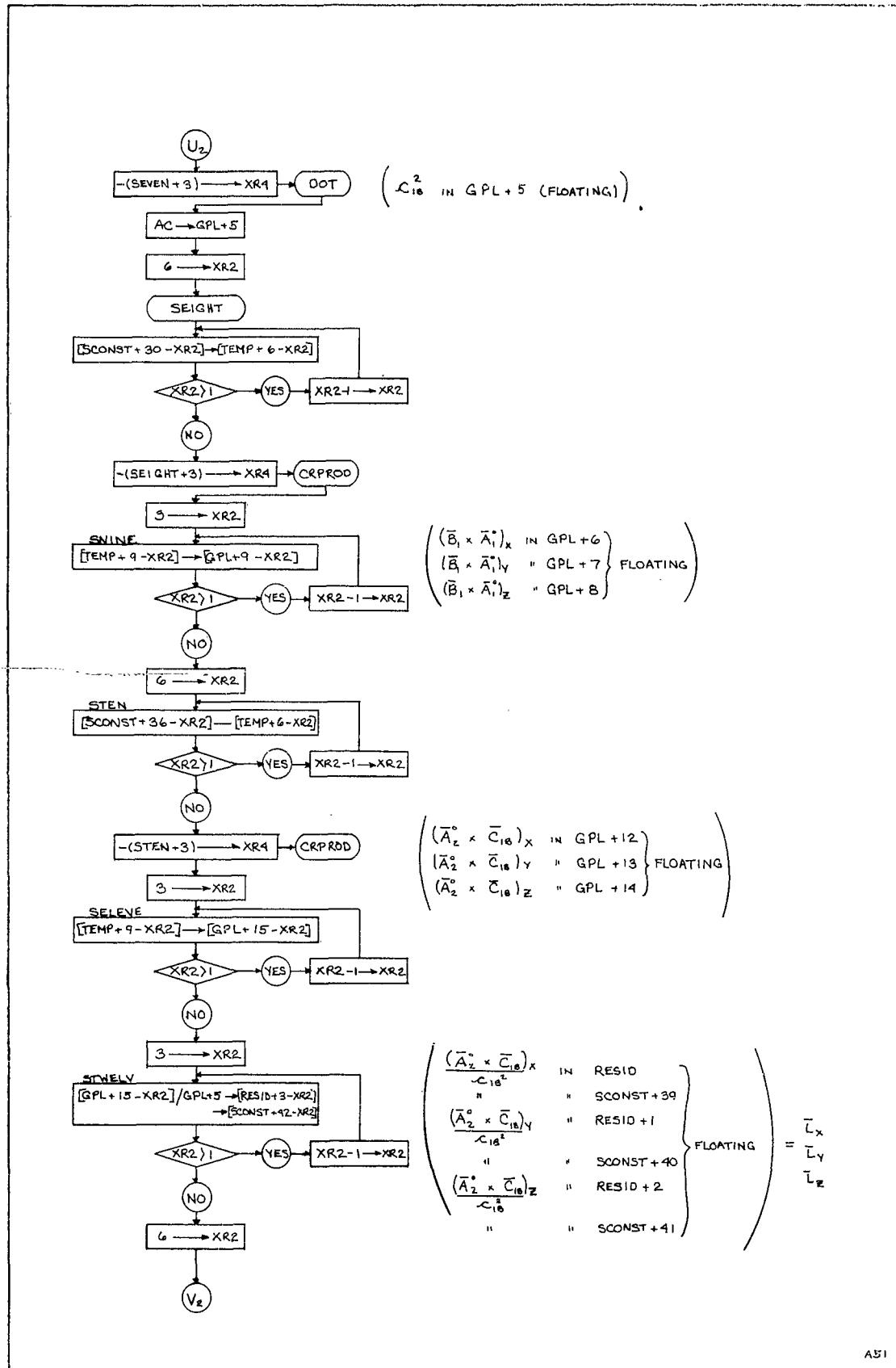


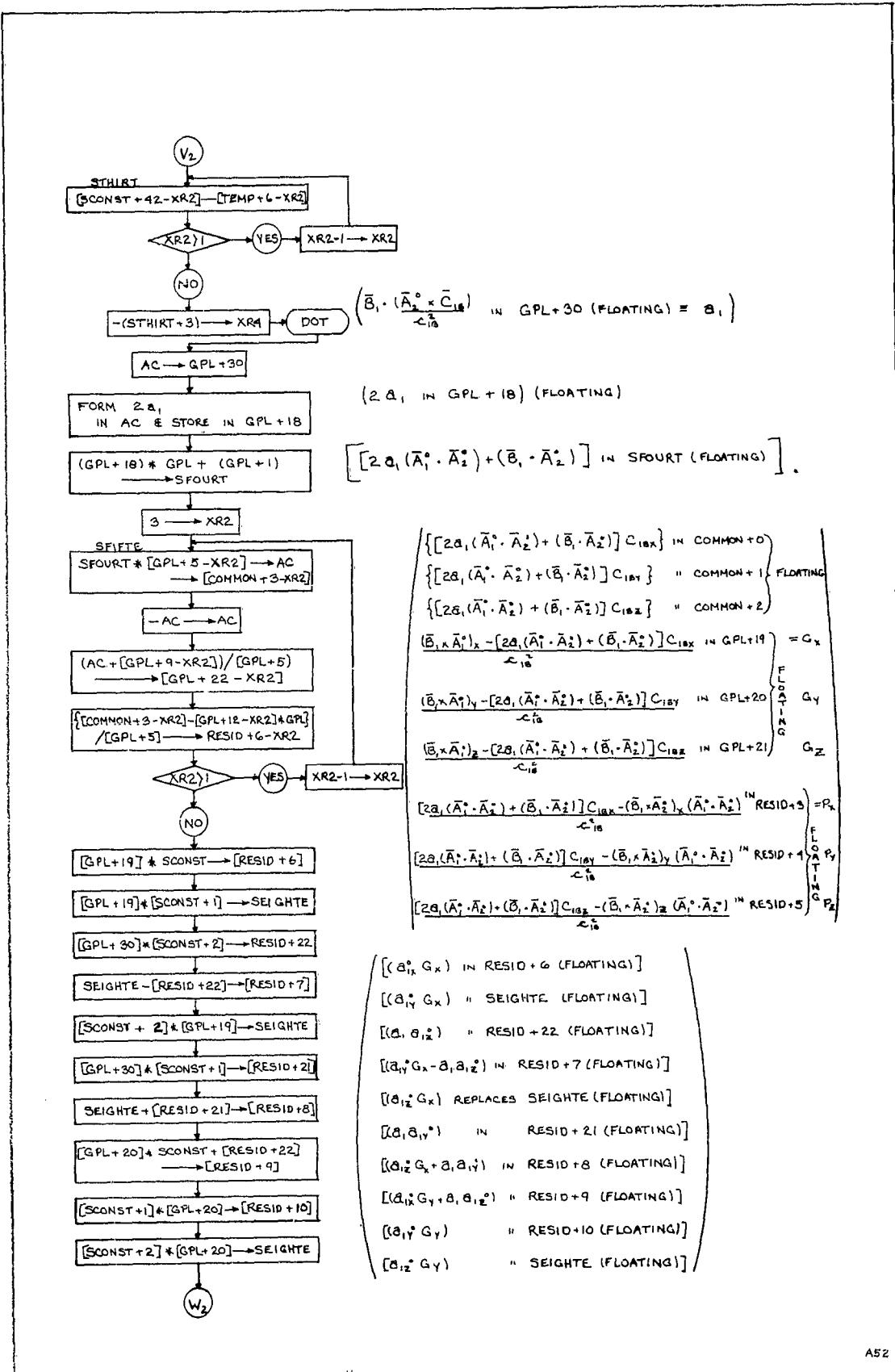


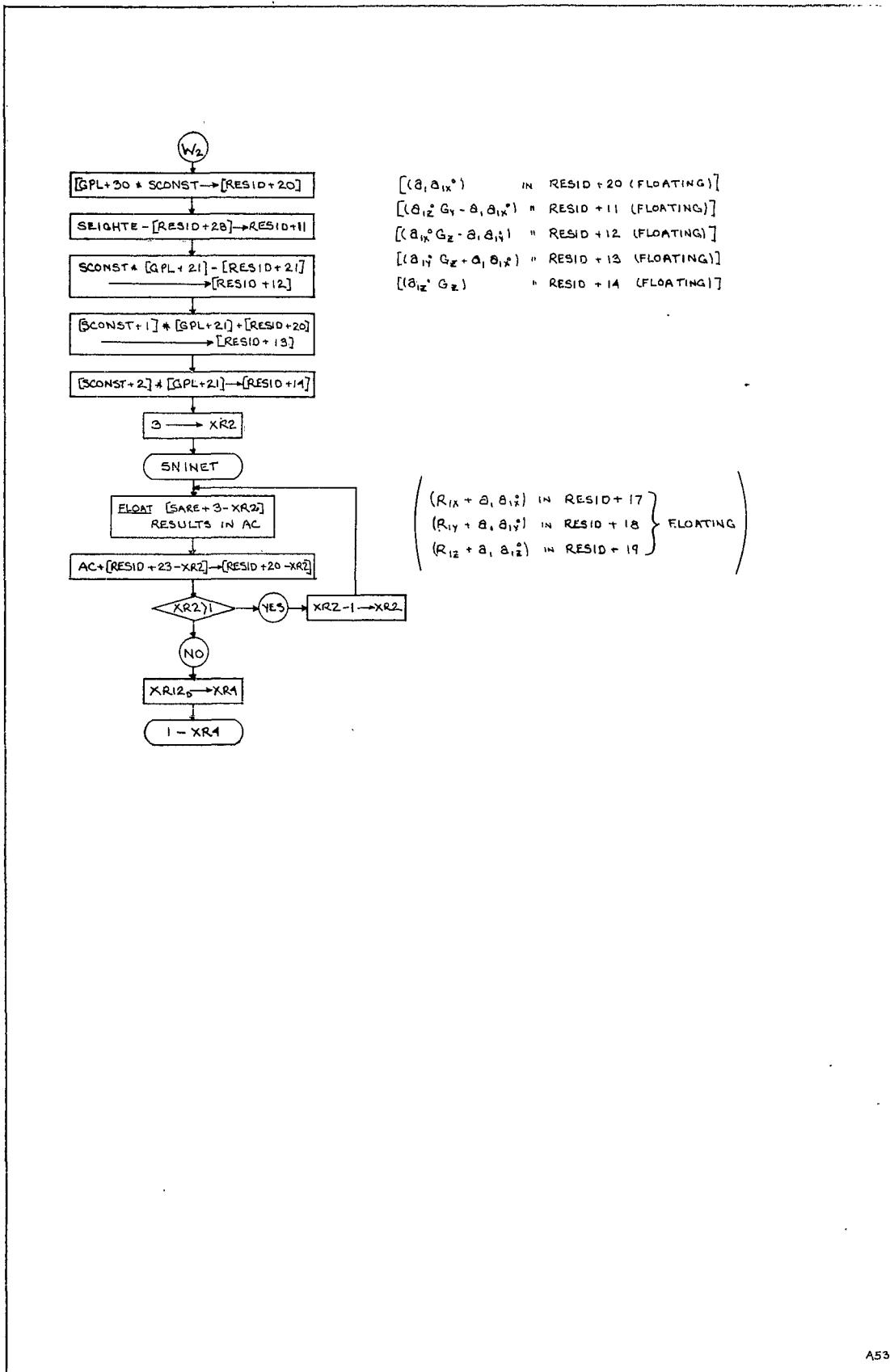












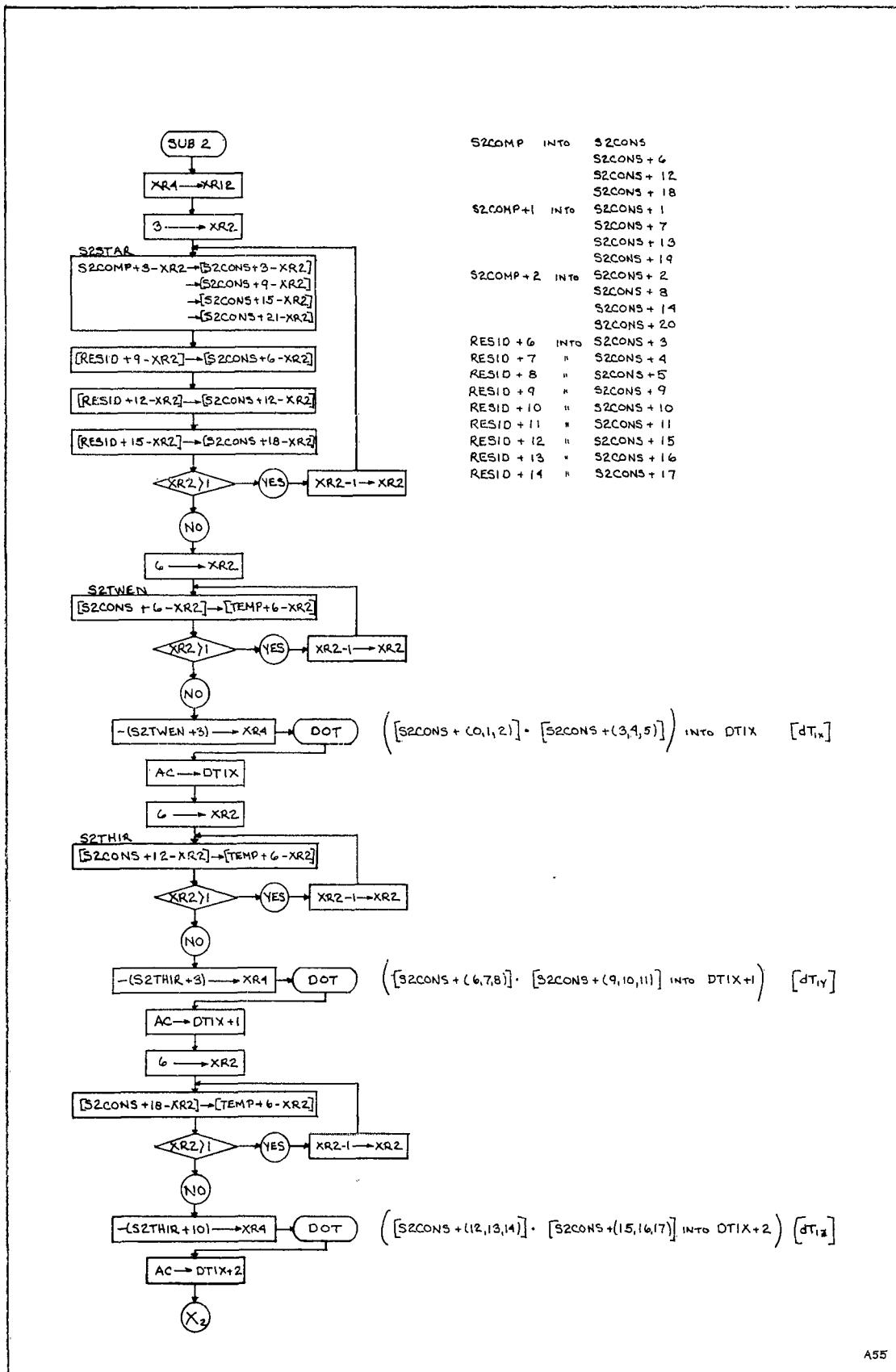
SUMMARY OF SUB 1

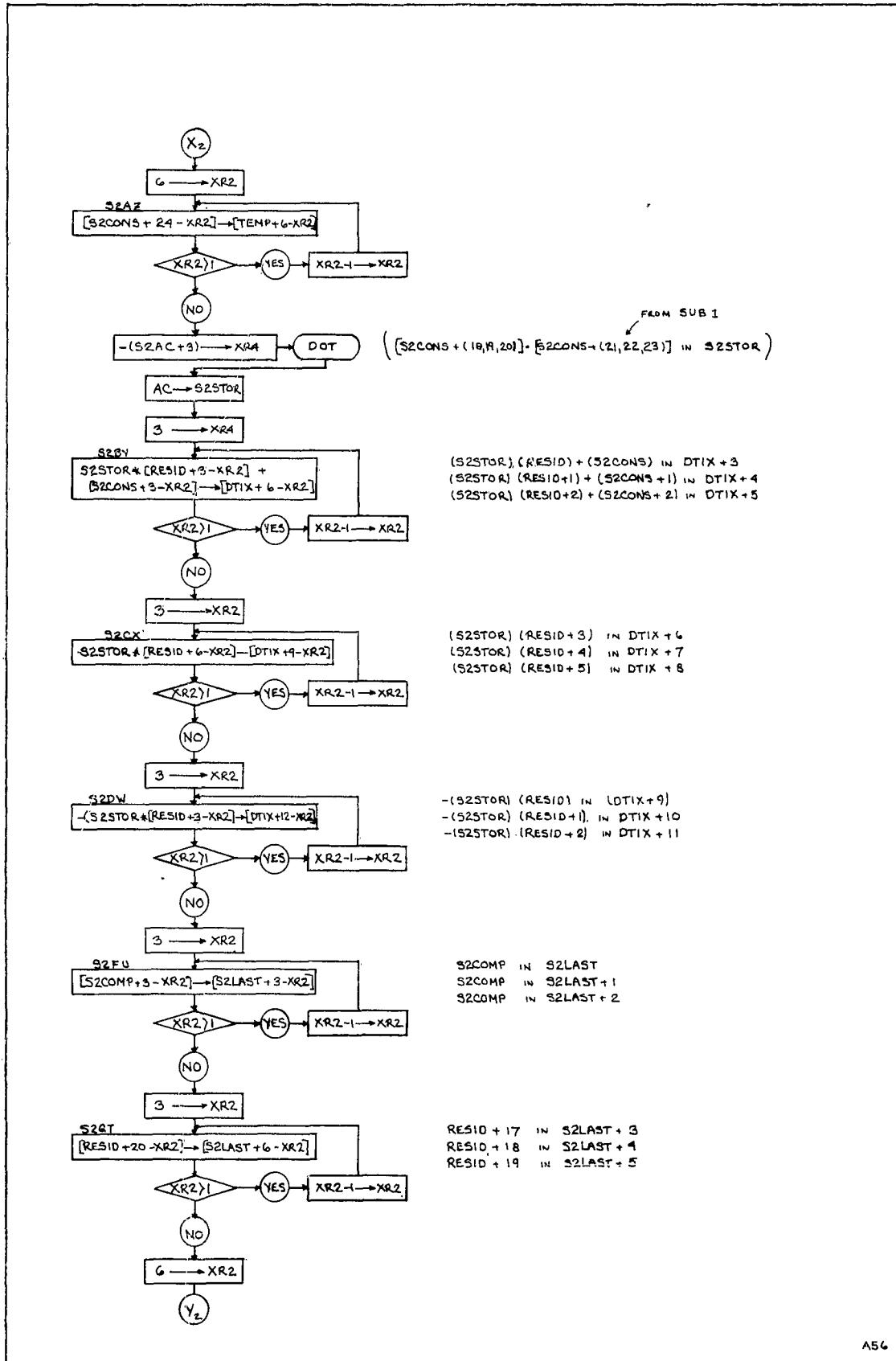
R _{1x}	IN	SARE
R _{1y}	"	SARE + 1
R _{1z}	"	SARE + 2
R _{2x}	"	SARE + 3
R _{2y}	"	SARE + 4
R _{2z}	"	SARE + 5

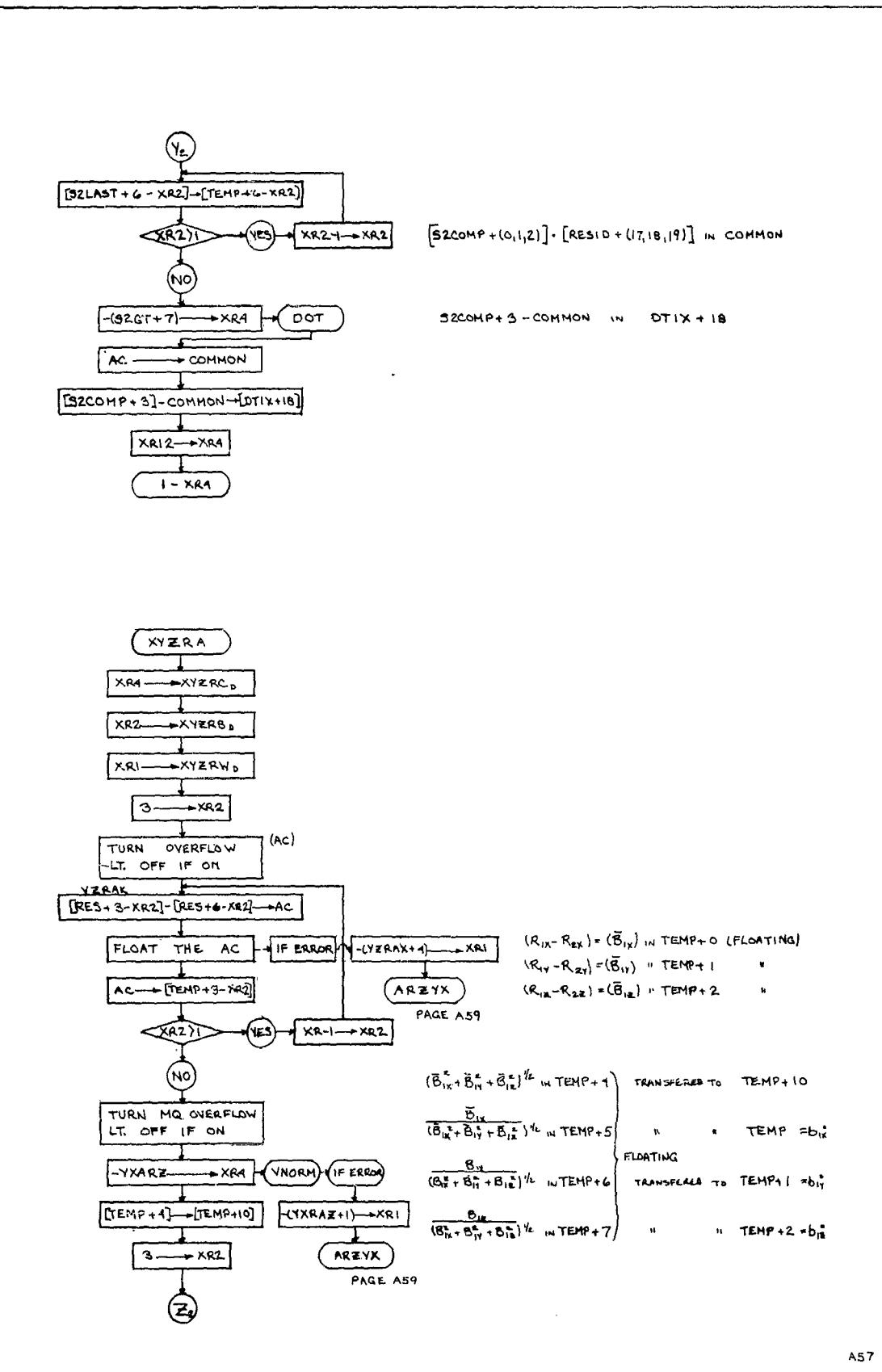
} FIXED, B25

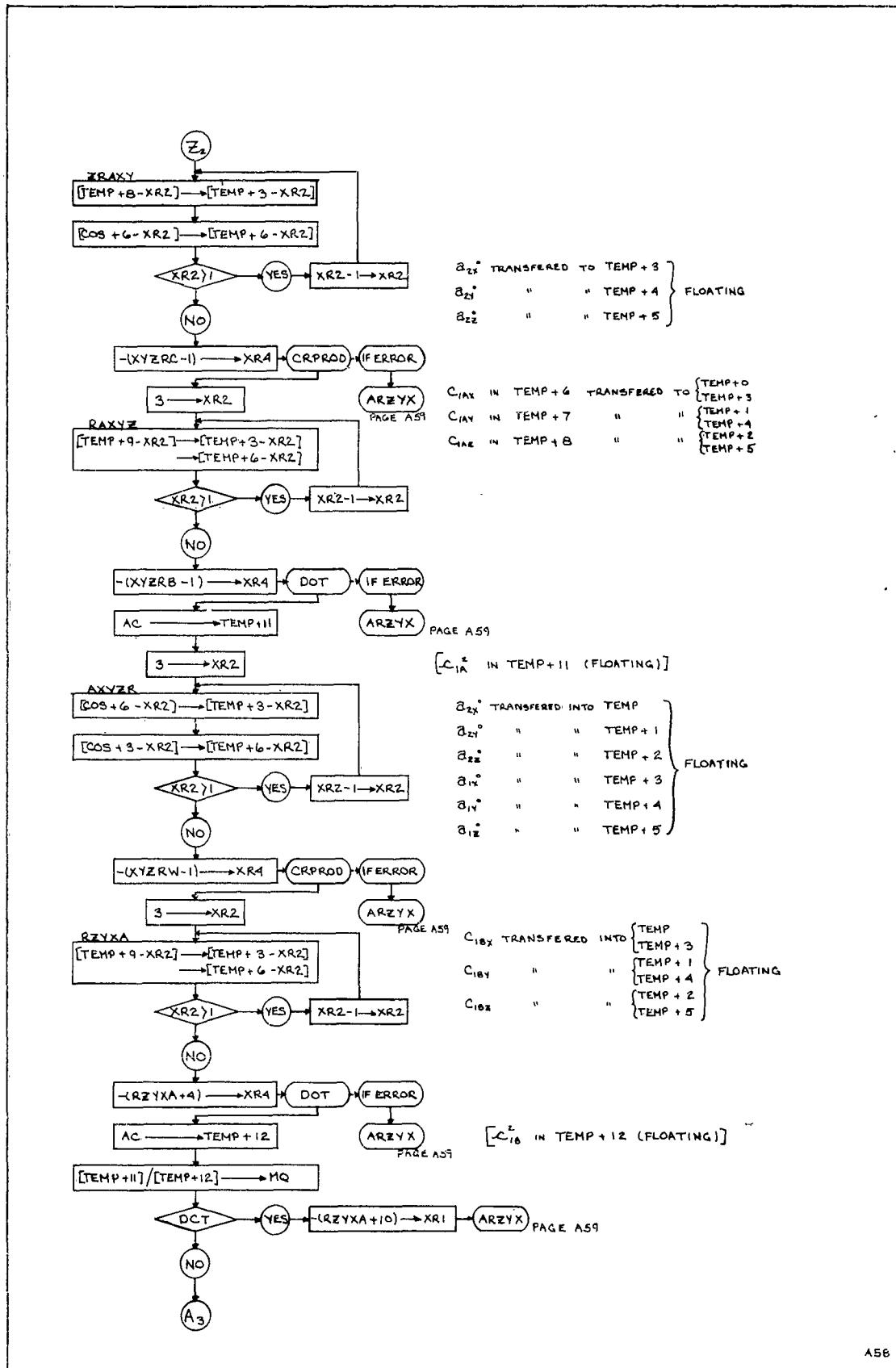
FLOATING

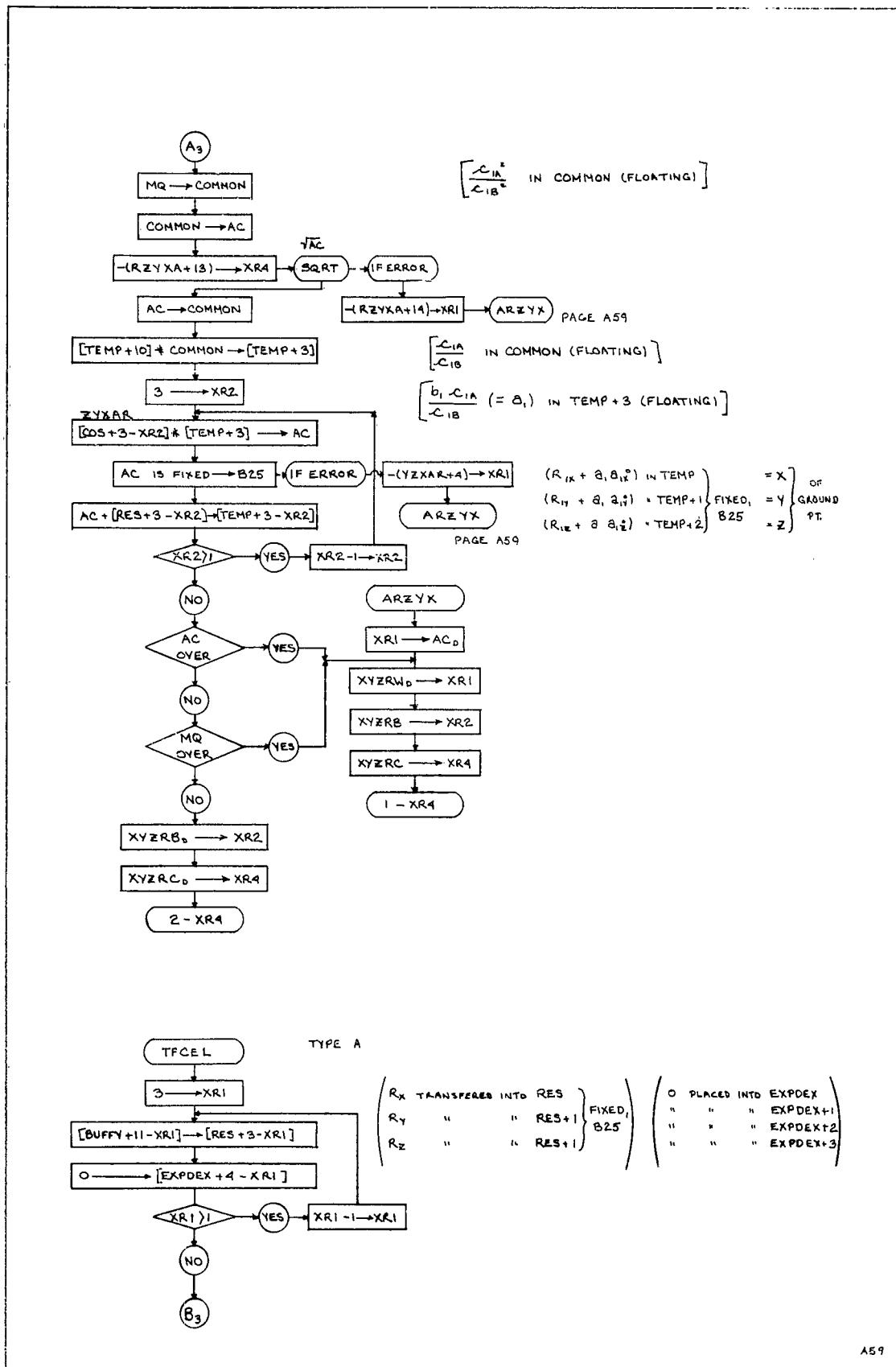
L _x	IN	RESID	B _{1x}	"	S2CONST + 21	($\bar{A}_1^0 \cdot \bar{A}_2^0$)	IN	GPL
L _y	"	RESID + 1	B _{1y}	"	S2CONST + 22	($\bar{B}_1 \cdot \bar{A}_2^0$)	"	GPL + 1
L _z	"	RESID + 2	B _{1z}	"	S2CONST + 23	C _{18x}	"	GPL + 2
P _x	"	RESID + 3	B _{2x}	"	SCONST	C _{18y}	"	GPL + 3
P _y	"	RESID + 4	B _{2y}	"	SCONST + 1	C _{18z}	"	GPL + 4
P _z	"	RESID + 5	B _{2z}	"	SCONST + 2	-C ₁₈	"	GPL + 5
(B _{1x} G _x)	"	RESID + 6	B _{2y}	"	SCONST + 3	($\bar{B}_1 \cdot \bar{A}_1^0$) _x	"	GPL + 6
(B _{1y} G _x - A ₁ A _{1z})	"	RESID + 7	B _{2z}	"	SCONST + 4	($\bar{B}_1 \cdot \bar{A}_1^0$) _y	"	GPL + 7
(B _{1z} G _x + B ₁ A _{1y})	"	RESID + 8	B _{1x}	"	SCONST + 5	($\bar{B}_1 \cdot \bar{A}_1^0$) _z	"	GPL + 8
(B _{1x} G _y + A ₁ A _{1z})	"	RESID + 9	B _{1y}	"	SCONST + 6	($\bar{B}_1 \cdot \bar{A}_2^0$) _x	"	GPL + 9
(B _{1y} G _y)	"	RESID + 10	B _{1z}	"	SCONST + 7	($\bar{B}_1 \cdot \bar{A}_2^0$) _y	"	GPL + 10
(B _{1z} G _y - A ₁ A _{1x})	"	RESID + 11	B _{2x}	"	SCONST + 8	($\bar{B}_1 \cdot \bar{A}_2^0$) _z	"	GPL + 11
(B _{1x} G _z - A ₁ A _{1y})	"	RESID + 12	B _{2y}	"	SCONST + 9	($\bar{A}_2^0 \times \bar{C}_{18}$) _x	"	GPL + 12
(B _{1y} G _z + A ₁ A _{1x})	"	RESID + 13	B _{2z}	"	SCONST + 10	($\bar{A}_2^0 \times \bar{C}_{18}$) _y	"	GPL + 13
(B _{1z} G _z)	"	RESID + 14	B _{1x}	"	SCONST + 11	($\bar{A}_2^0 \times \bar{C}_{18}$) _z	"	GPL + 14
(R _{1x} + A ₁ A _{1x})	"	RESID + 17	B _{1y}	"	SCONST + 12	2 A ₁	IN	GPL + 18
(R _{1y} + A ₁ A _{1y})	"	RESID + 18	B _{1z}	"	SCONST + 13	G _x	"	GPL + 19
(R _{1z} + A ₁ A _{1z})	"	RESID + 19	C _{18x}	"	SCONST + 14	G _y	"	GPL + 20
(A ₁ A _{1x})	"	RESID + 20	C _{18y}	"	SCONST + 15	G _z	"	GPL + 21
(A ₁ A _{1y})	"	RESID + 21	C _{18z}	"	SCONST + 16			
(A ₁ A _{1z})	"	RESID + 22	C ₁₈₁	"	SCONST + 17	A ₁	IN	GPL + 30
			C ₁₈₂	"	SCONST + 18			
			C ₁₈₃	"	SCONST + 19			
			B _{1x}	"	SCONST + 20			
			B _{1y}	"	SCONST + 21			
			B _{1z}	"	SCONST + 22			
			B _{2x}	"	SCONST + 23			
			B _{2y}	"	SCONST + 24			
			B _{2z}	"	SCONST + 25			
			B _{1x}	"	SCONST + 26			
			B _{1y}	"	SCONST + 27			
			B _{1z}	"	SCONST + 28			
			B _{2x}	"	SCONST + 29			
			B _{2y}	"	SCONST + 30			
			B _{2z}	"	SCONST + 31			
			C _{18x}	"	SCONST + 32			
			C _{18y}	"	SCONST + 33			
			C _{18z}	"	SCONST + 34			
			C ₁₈₁	"	SCONST + 35			
			C ₁₈₂	"	SCONST + 36			
			B _{1x}	"	SCONST + 37			
			B _{1y}	"	SCONST + 38			
			B _{1z}	"	SCONST + 39			
			B _{2x}	"	SCONST + 40			
			B _{2y}	"	SCONST + 41			
			B _{2z}	"	SCONST + 42			

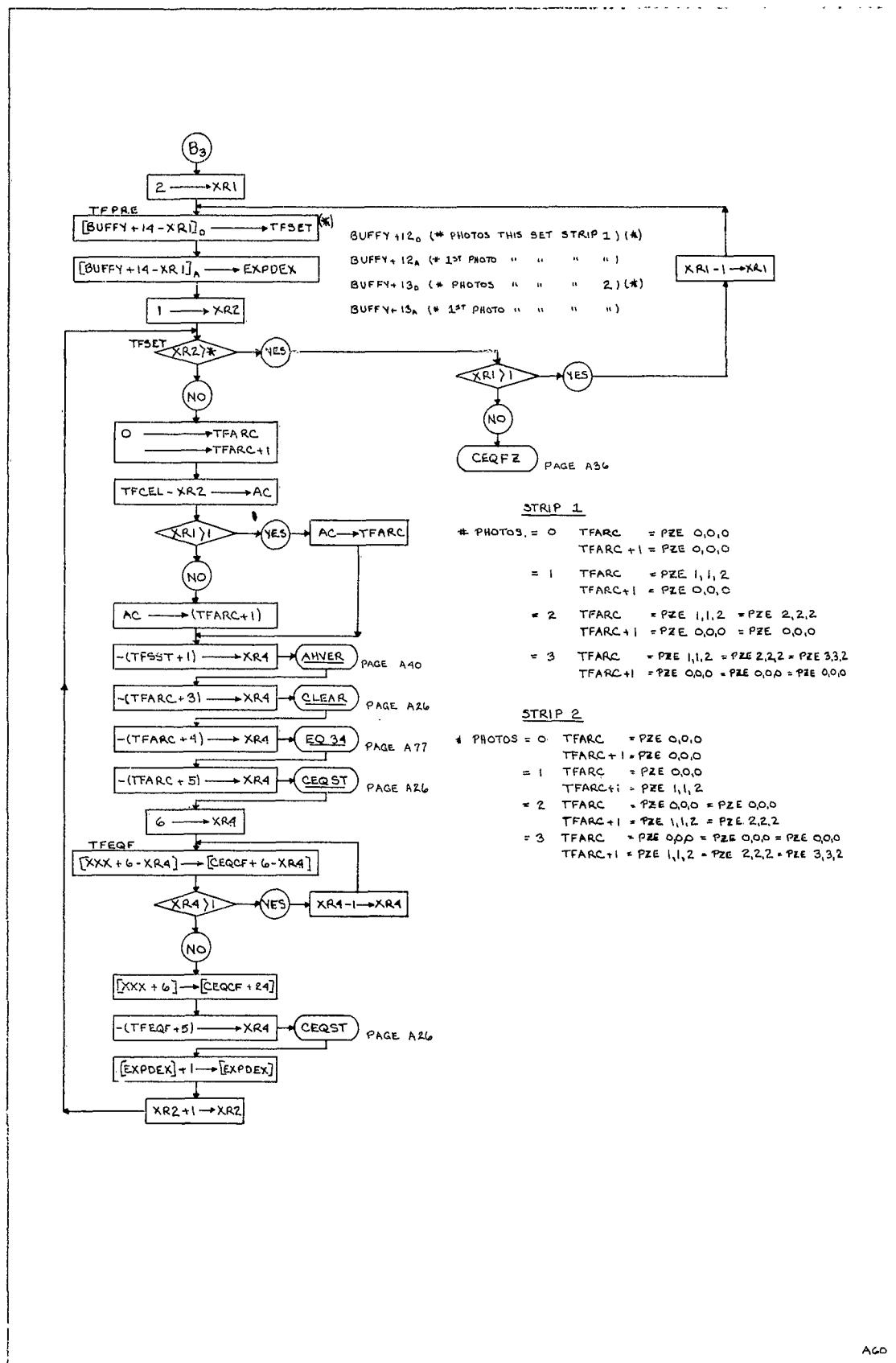










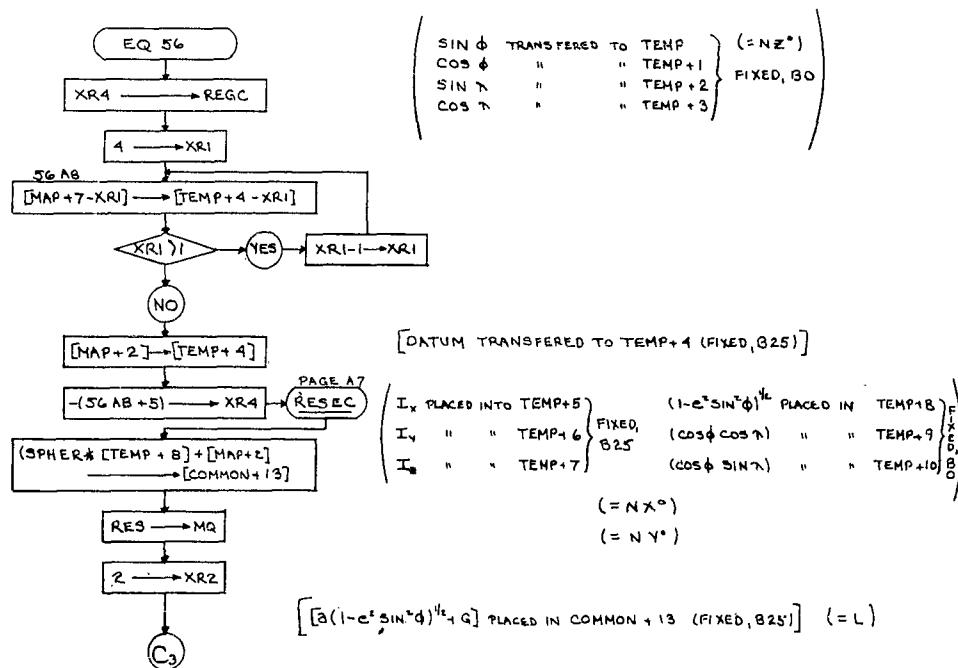
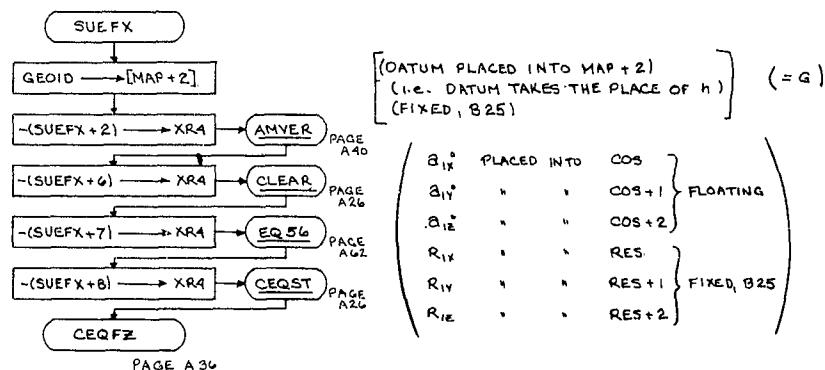


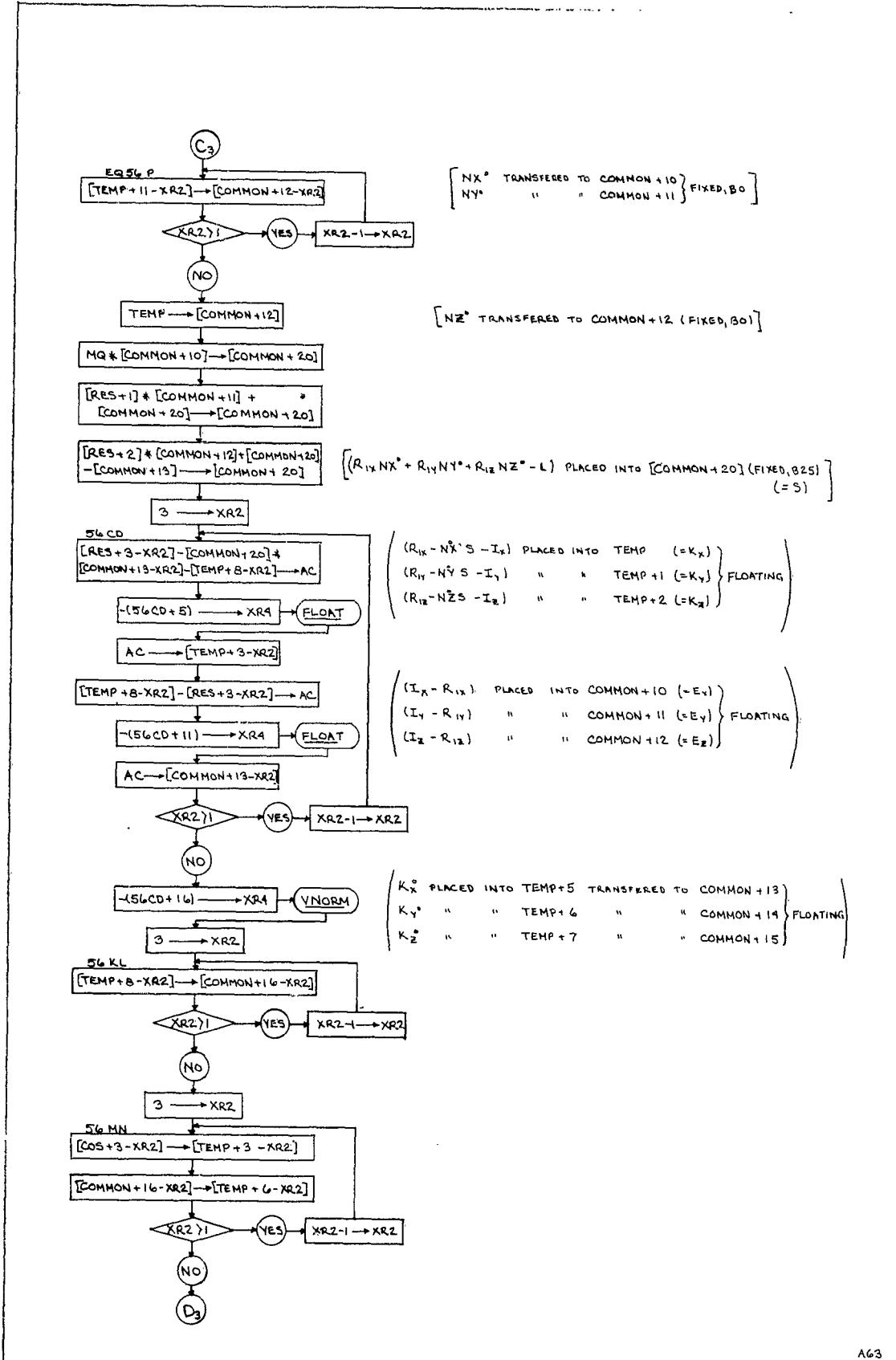
INITIALIZATION FOR ENTRY INTO EQ 34

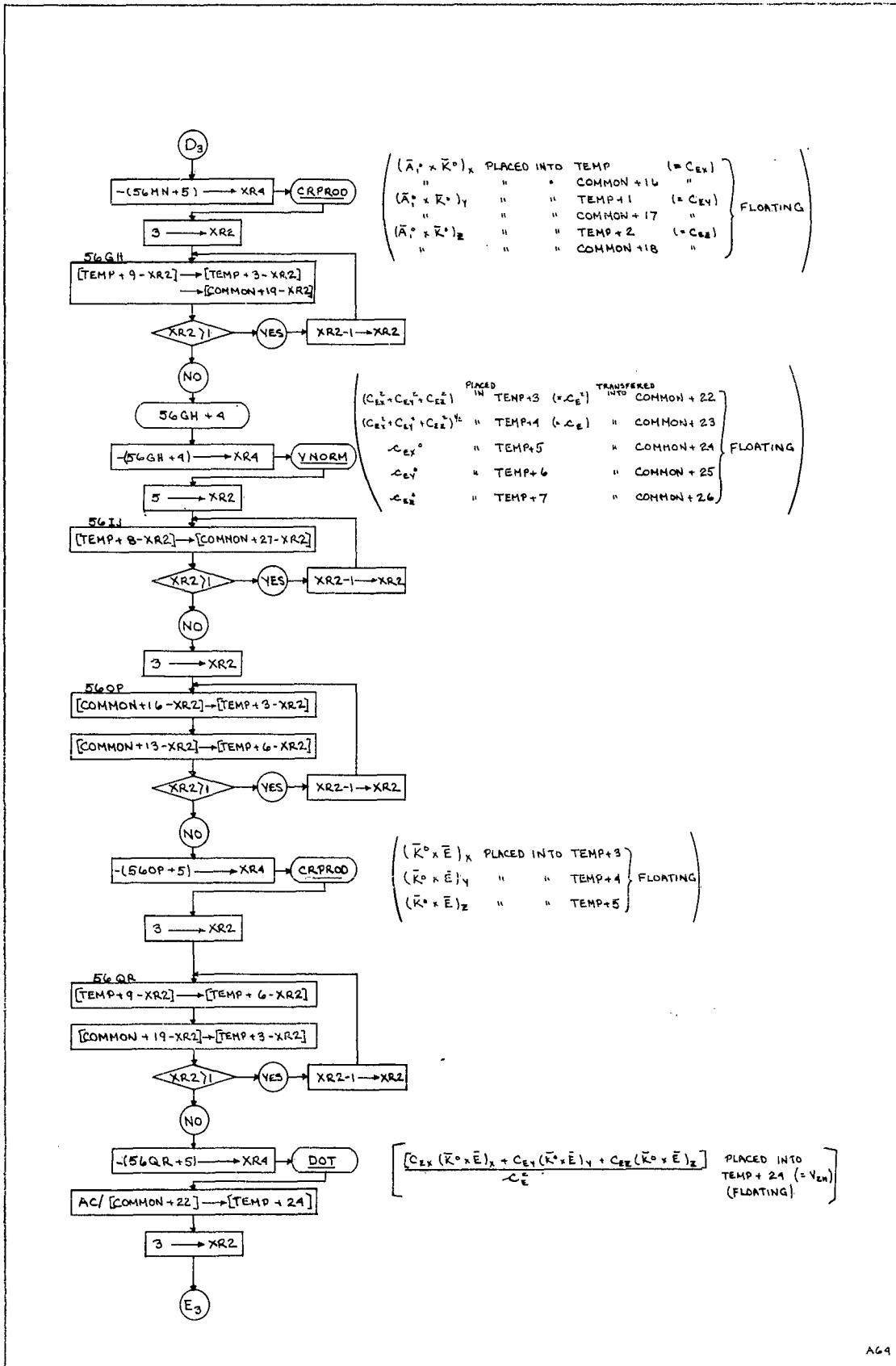
a_{ix}^o TRANSFERRED INTO COS+3	a_{iy}^o TRANSFERRED INTO COS+4	a_{iz}^o TRANSFERRED INTO COS+5	a_{ix}^{o*} TRANSFERRED INTO COS+3	a_{iy}^{o*} TRANSFERRED INTO COS+4	a_{iz}^{o*} TRANSFERRED INTO COS+5
a_{1x}^o "	" COS+4	" COS+5	a_{1x}^{o*} "	" COS+4	" COS+5
a_{1y}^o "	"	"	a_{1y}^{o*} "	"	"
a_{1z}^o "	"	"	a_{1z}^{o*} "	"	"
R_x "	" RES+0	"	R_x "	" RES	"
R_y "	" RES+1	"	R_y "	" RSS+1	"
R_z "	" RES+2	"	R_z "	" RES+2	"
R_{1x} "	" RES+3	"	R_{1x} "	" RES+3	"
R_{1y} "	" RES+4	"	R_{1y} "	" RES+4	"
R_{1z} "	" RES+5	"	R_{1z} "	" RES+5	"

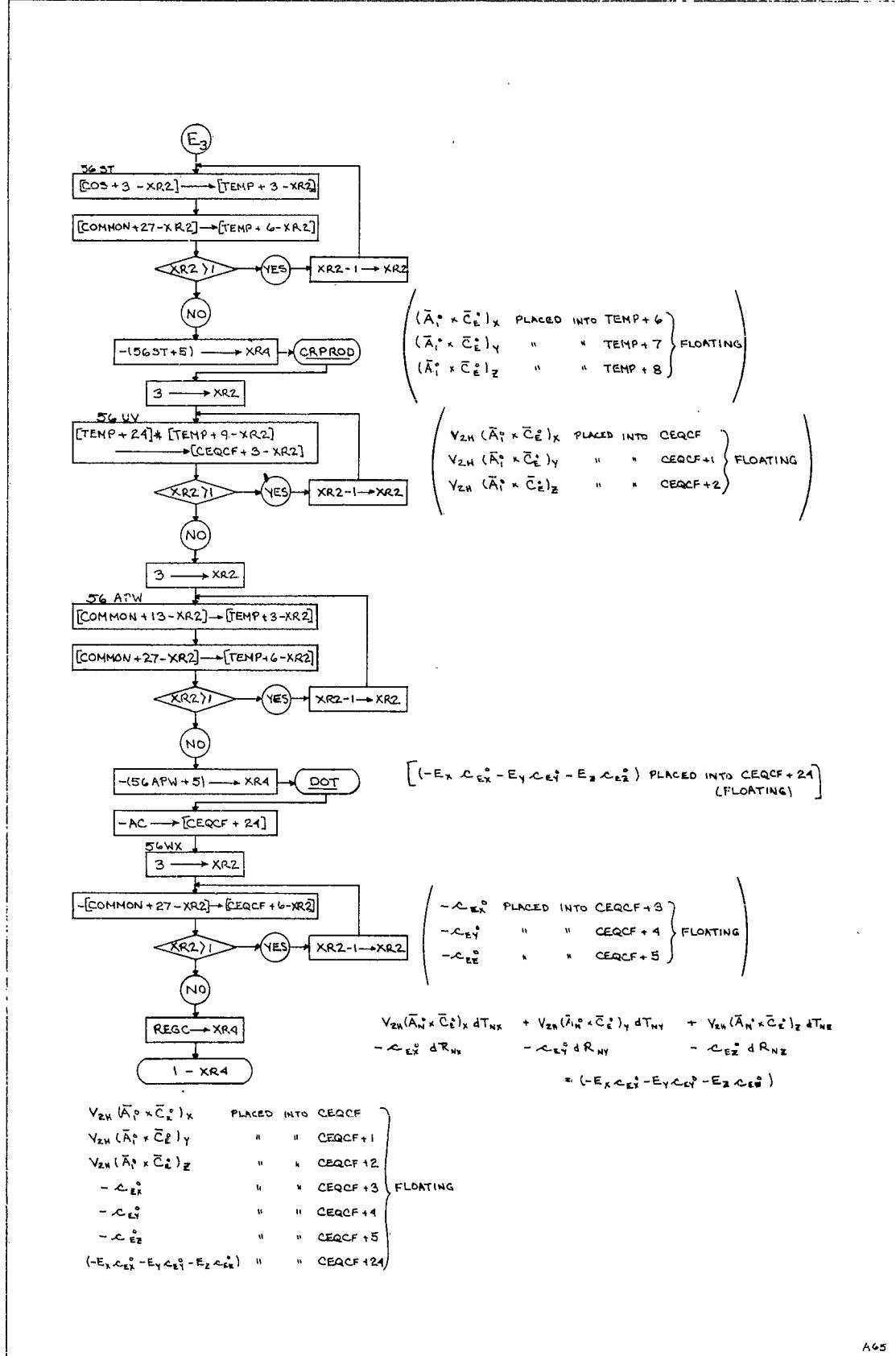
a_{ix}^{o*}	" COS+3	a_{iy}^{o*}	" COS+4	a_{iz}^{o*}	" COS+5	a_{ix}^{o*}	" COS+3	a_{iy}^{o*}	" COS+4	a_{iz}^{o*}	" COS+5
a_{1x}^{o*}	"	a_{1y}^{o*}	"	a_{1z}^{o*}	"	a_{1x}^{o*}	"	a_{1y}^{o*}	"	a_{1z}^{o*}	"
a_{1y}^{o*}	"	"	"	a_{1y}^{o*}	"	a_{1y}^{o*}	"	"	"	a_{1y}^{o*}	"
a_{1z}^{o*}	"	"	"	a_{1z}^{o*}	"	a_{1z}^{o*}	"	"	"	a_{1z}^{o*}	"
R_x	"	" RES	"	R_x	"	" RES	"	R_x	"	" RES	"
R_y	"	" RES+1	"	R_y	"	" RES+1	"	R_y	"	" RES+1	"
R_z	"	" RES+2	"	R_z	"	" RES+2	"	R_z	"	" RES+2	"
R_{1x}	"	" RES+3	"	R_{1x}	"	" RES+3	"	R_{1x}	"	" RES+3	"
R_{1y}	"	" RES+4	"	R_{1y}	"	" RES+4	"	R_{1y}	"	" RES+4	"
R_{1z}	"	" RES+5	"	R_{1z}	"	" RES+5	"	R_{1z}	"	" RES+5	"

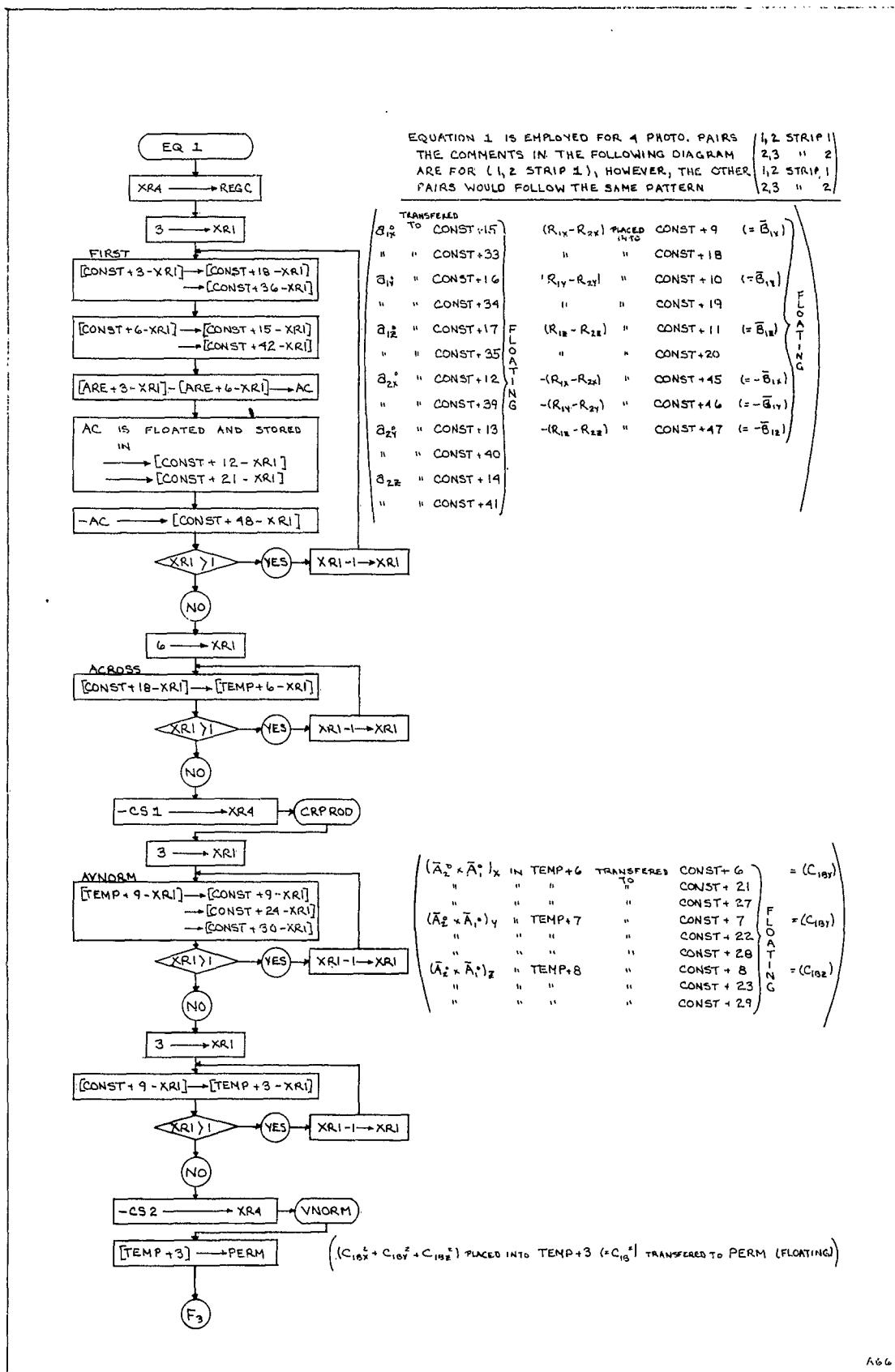
TYPE C | PHOTO STRIP 1 O PHOTOS STRIP 2

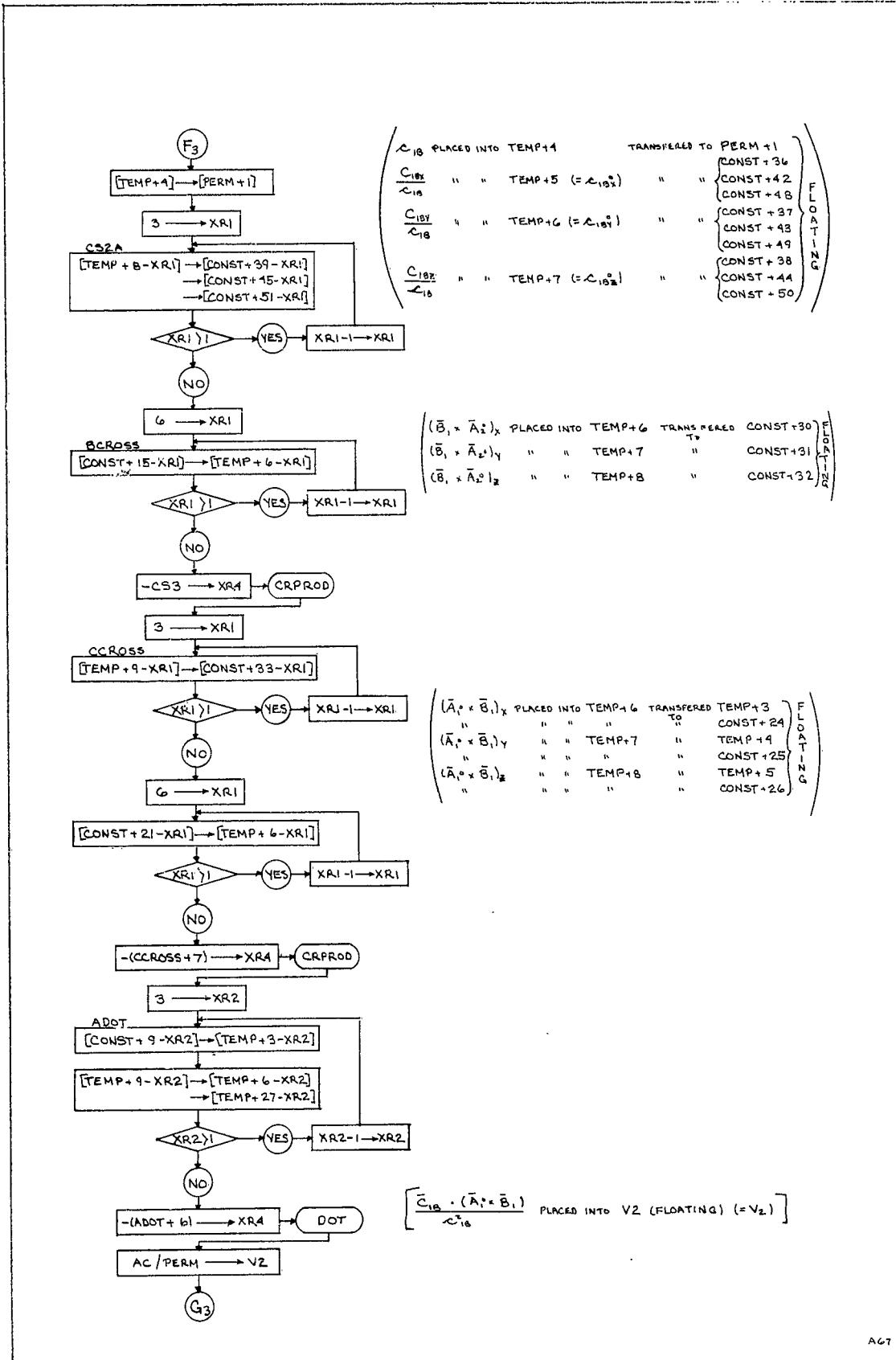


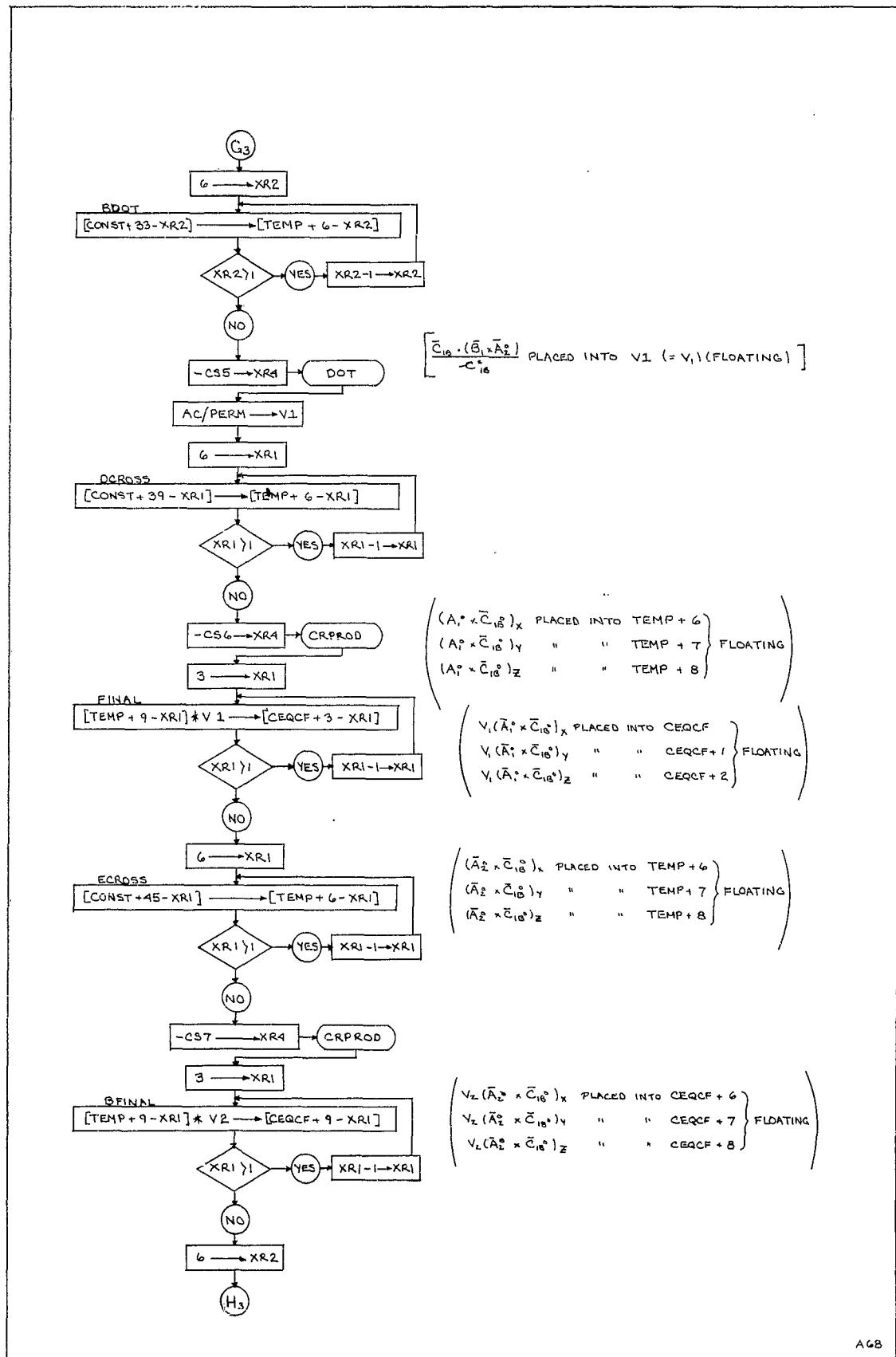


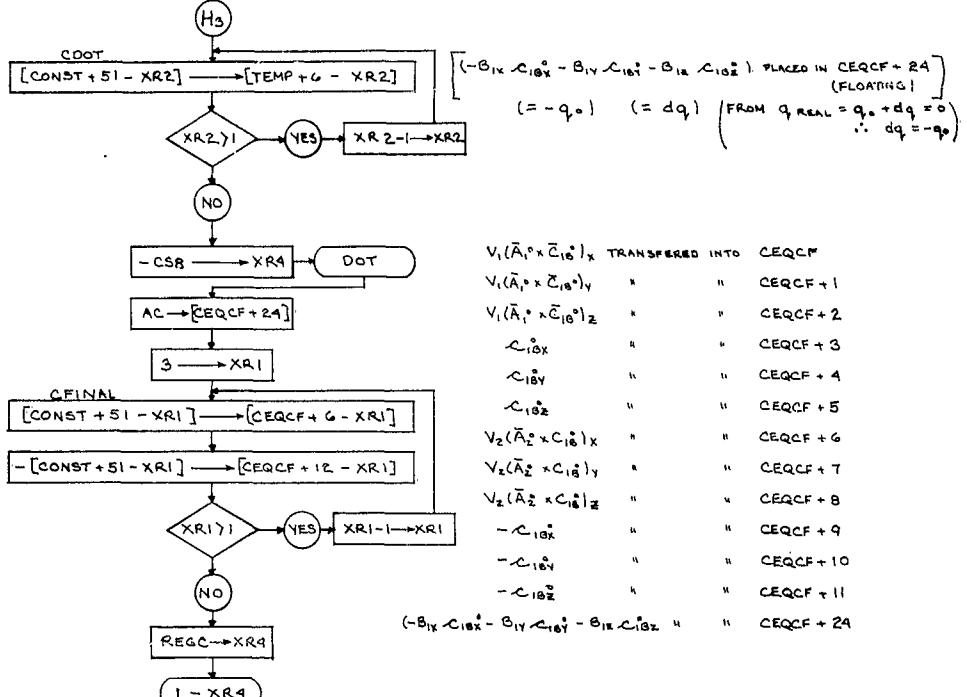




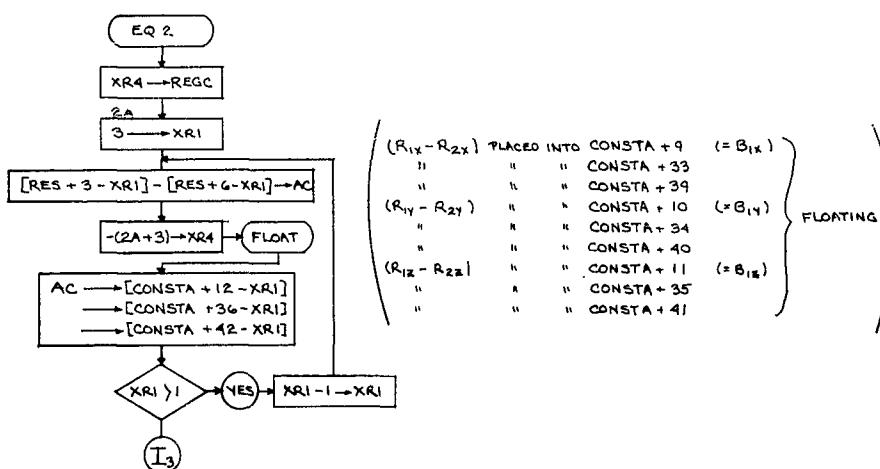


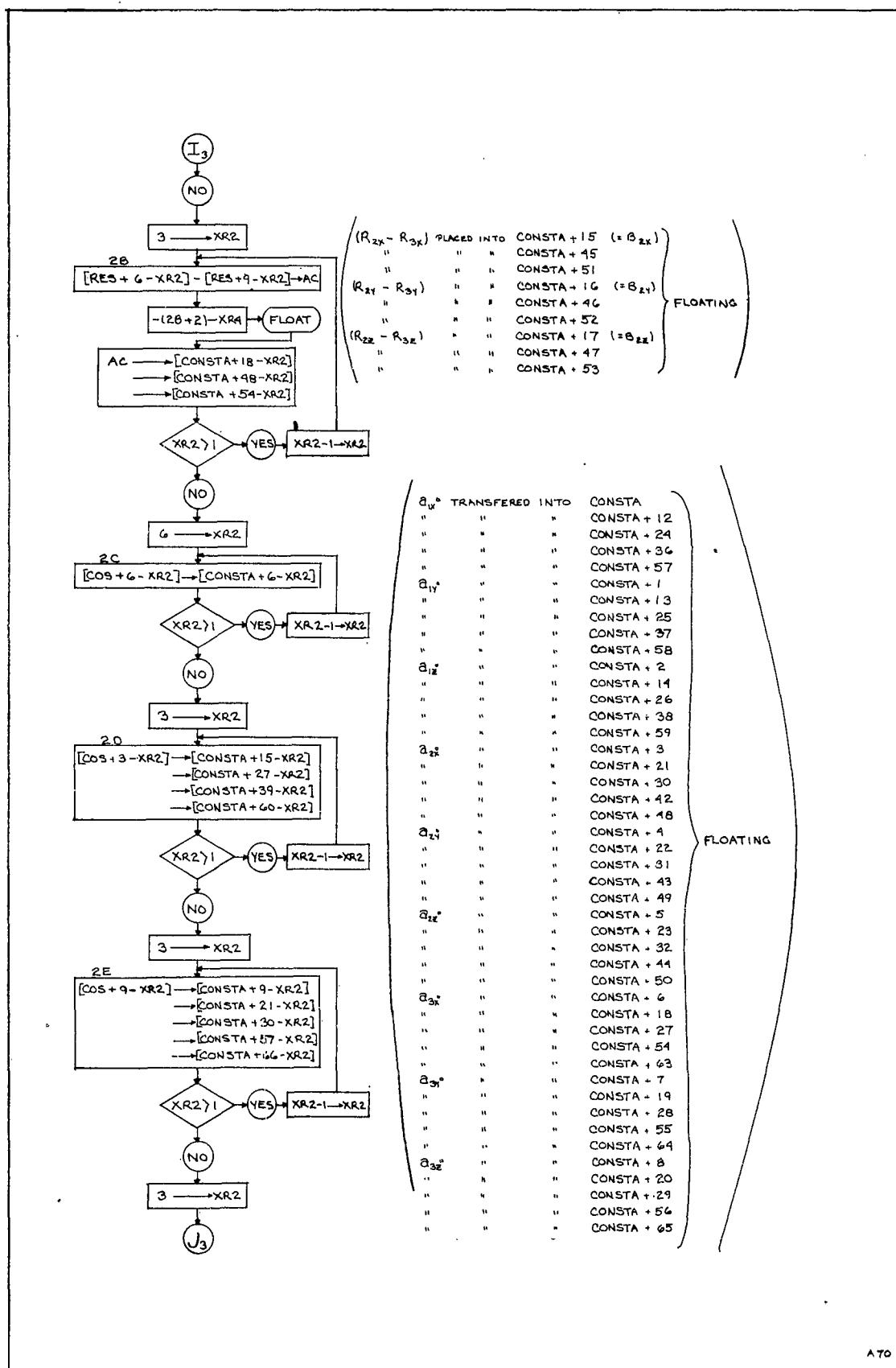


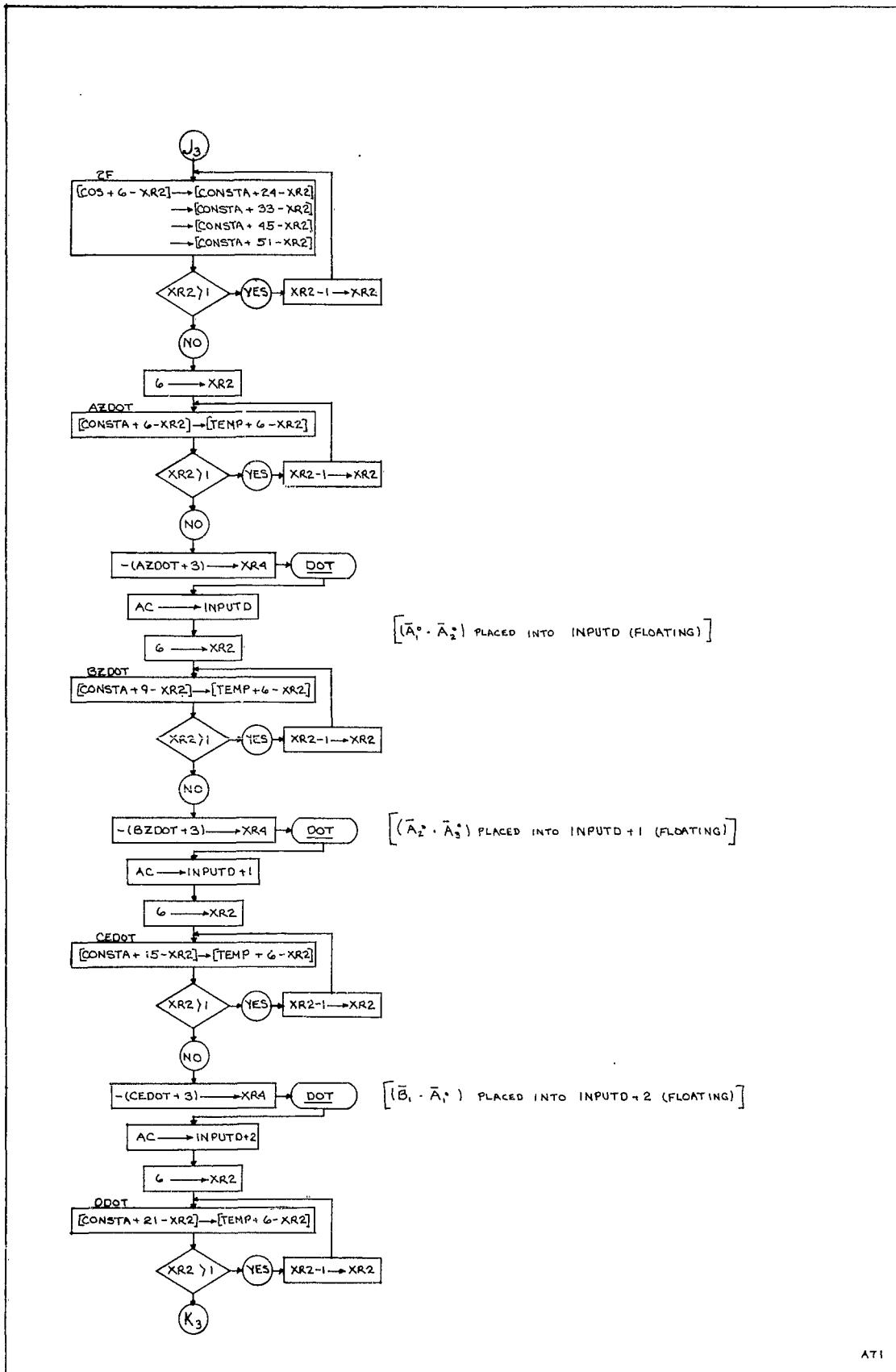


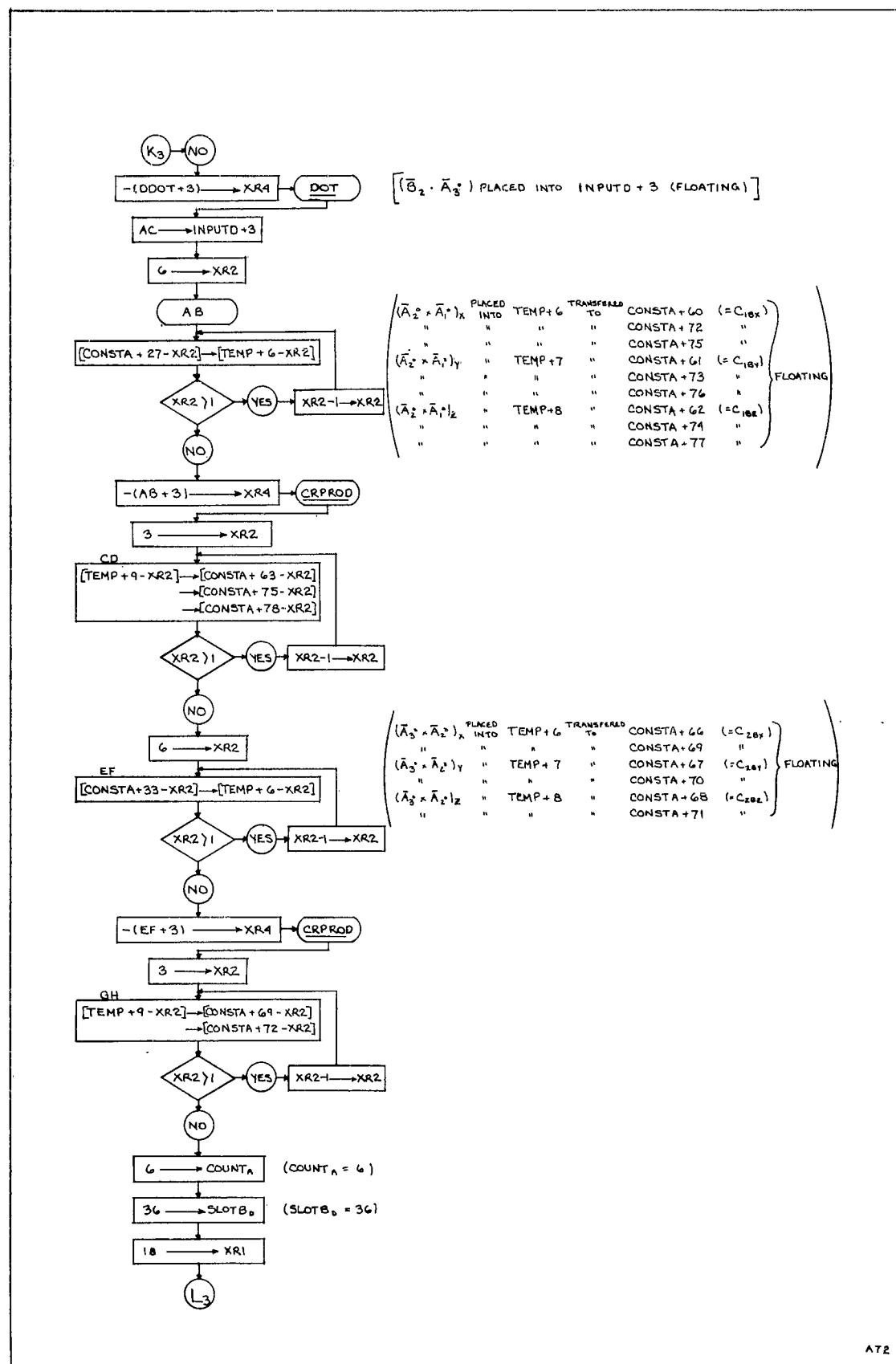


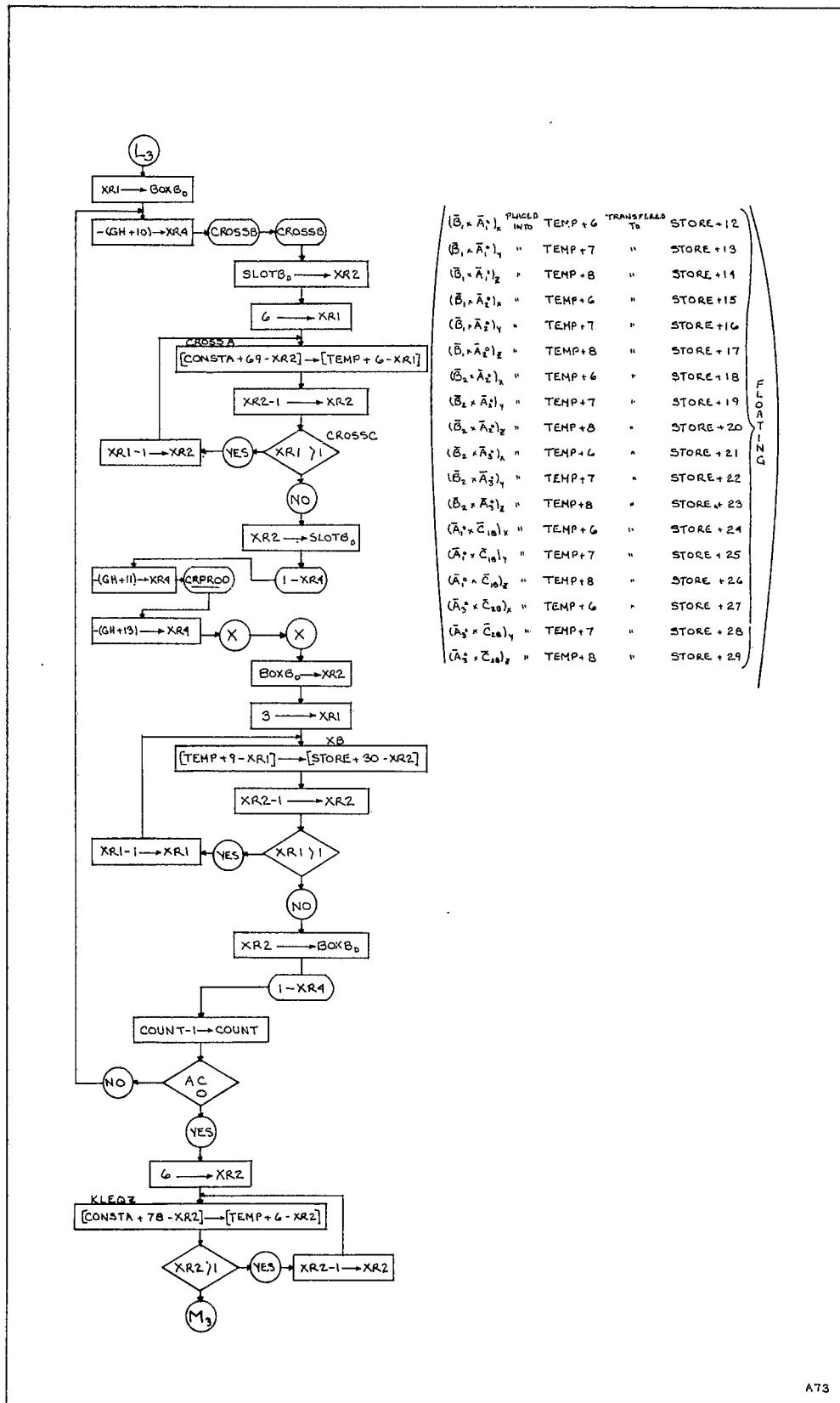
$$\begin{aligned}
 & V_1(\bar{A}_1^x \times \bar{C}_{18}^z)_x dT_{1x} + V_1(\bar{A}_1^x \times \bar{C}_{18}^z)_y dT_{1y} + V_1(\bar{A}_1^x \times \bar{C}_{18}^z)_z dT_{1z} + C_{18x} dR_{1x} + C_{18y} dR_{1y} + C_{18z} dR_{1z} \\
 & + V_2(\bar{A}_2^x \times \bar{C}_{18}^z)_x dT_{2x} + V_2(\bar{A}_2^x \times \bar{C}_{18}^z)_y dT_{2y} + V_2(\bar{A}_2^x \times \bar{C}_{18}^z)_z dT_{2z} - C_{18x} dR_{2x} - C_{18y} dR_{2y} - C_{18z} dR_{2z} \\
 & = dq = -q_0 = (-B_{1x}C_{18y} - B_{1y}C_{18z} - B_{1z}C_{18x})
 \end{aligned}$$

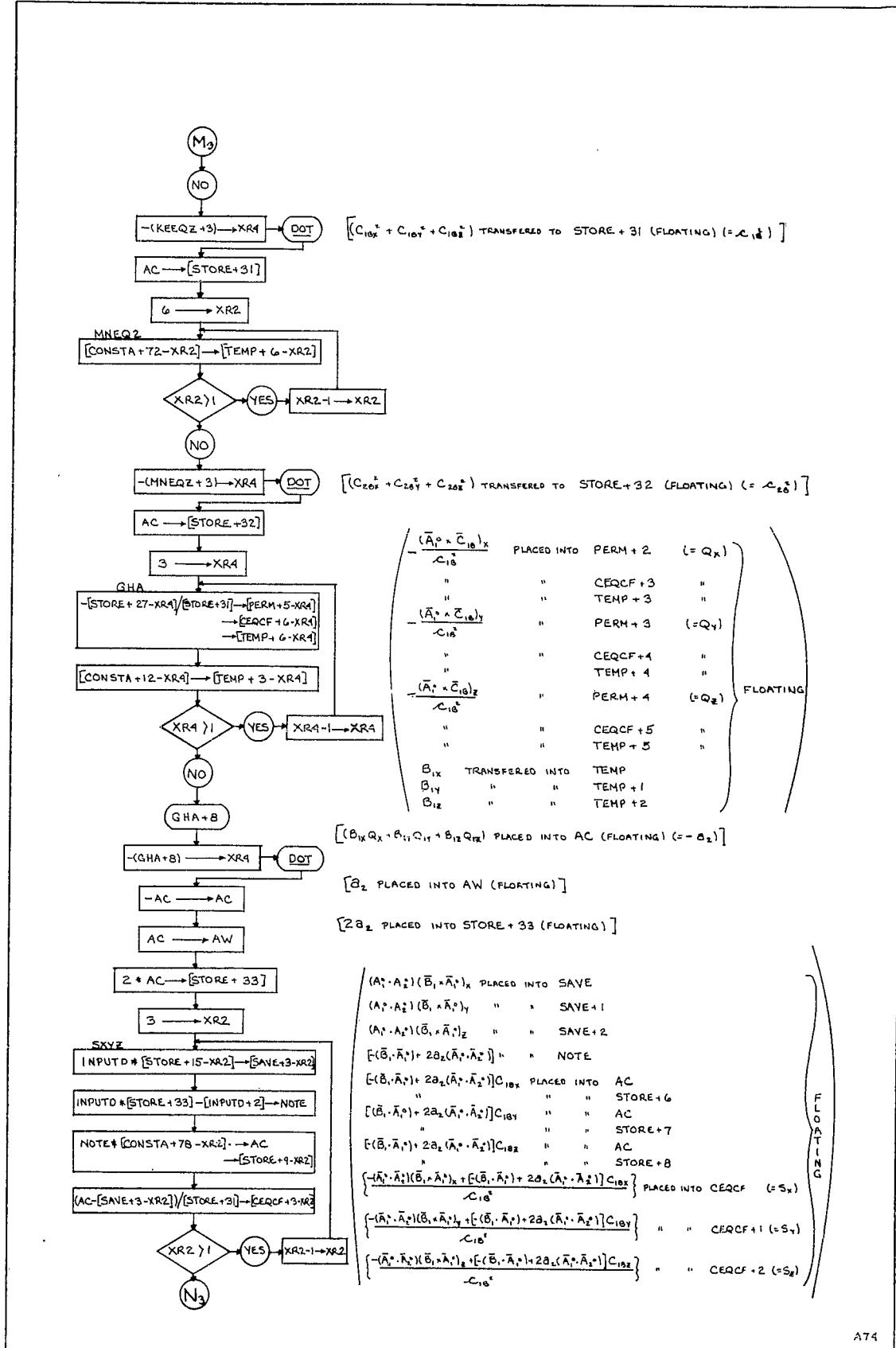


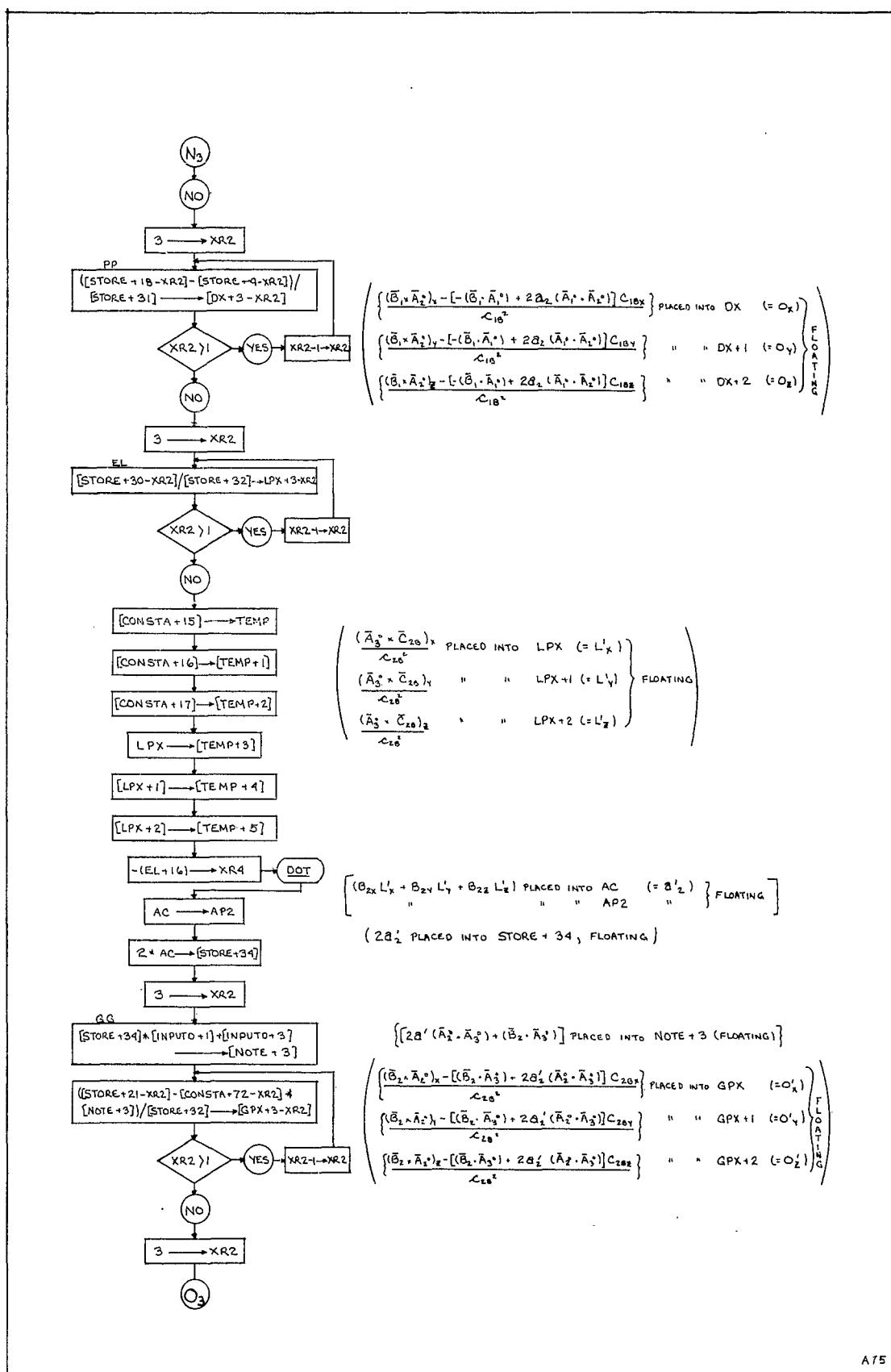


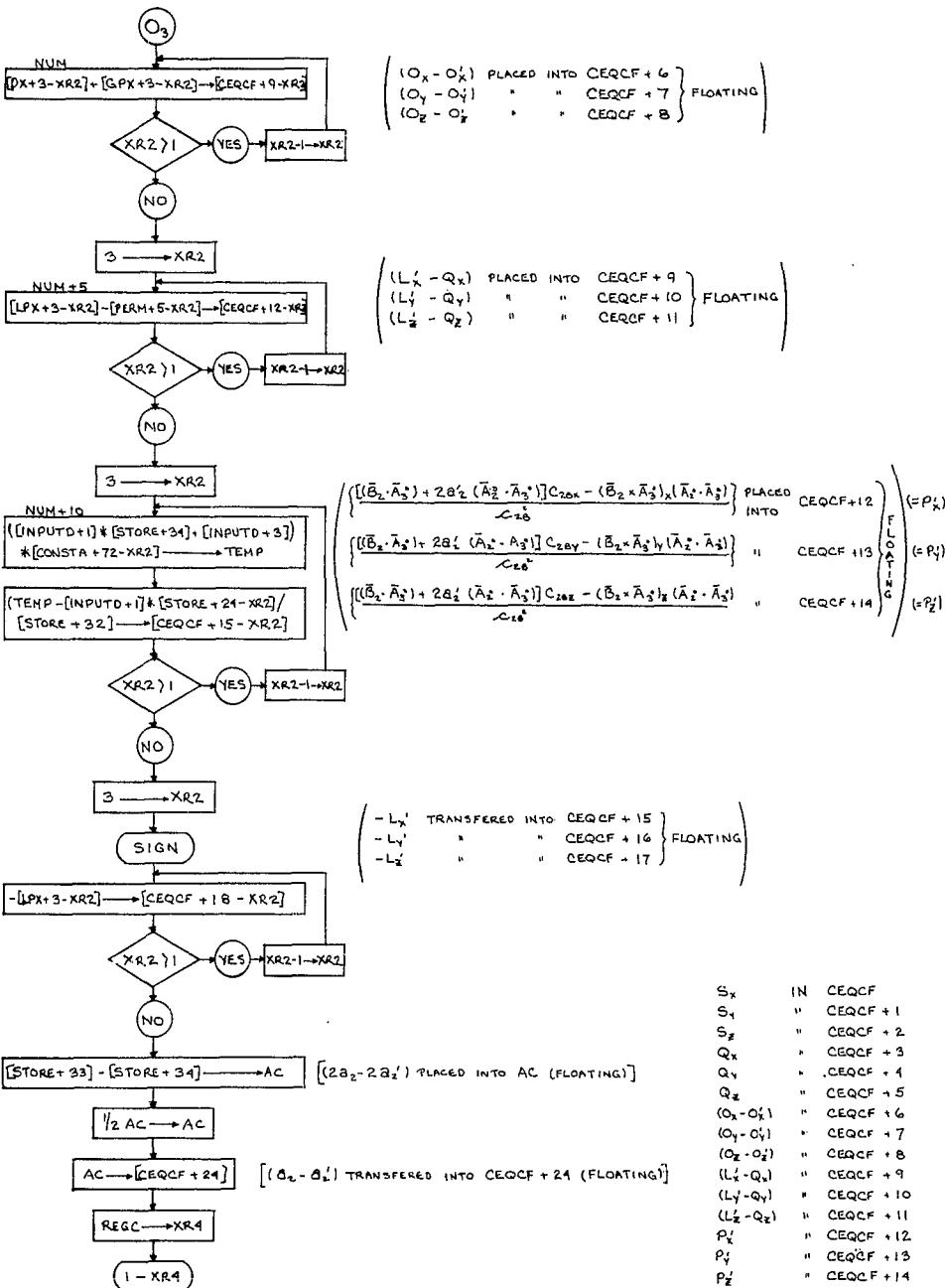








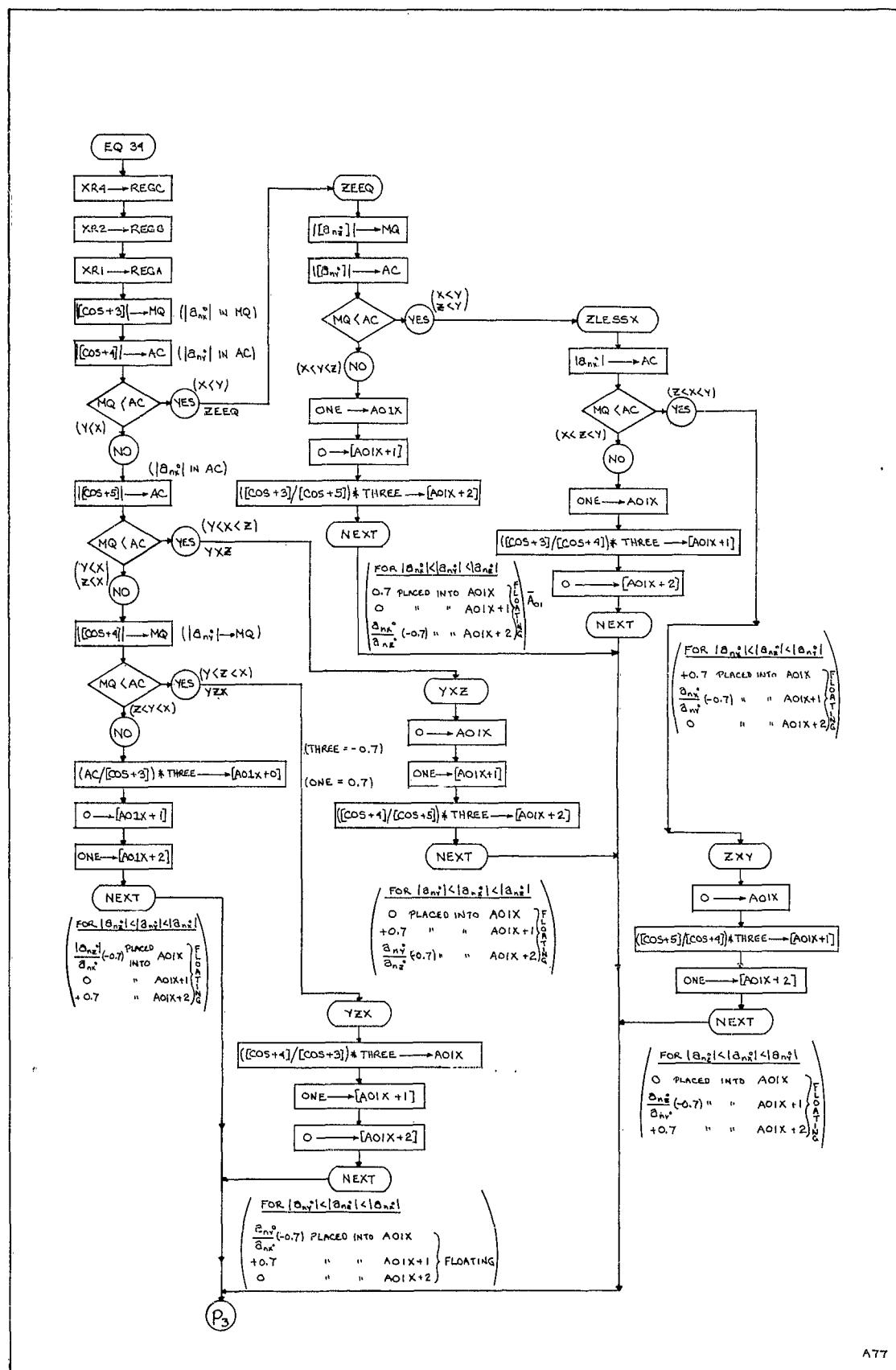


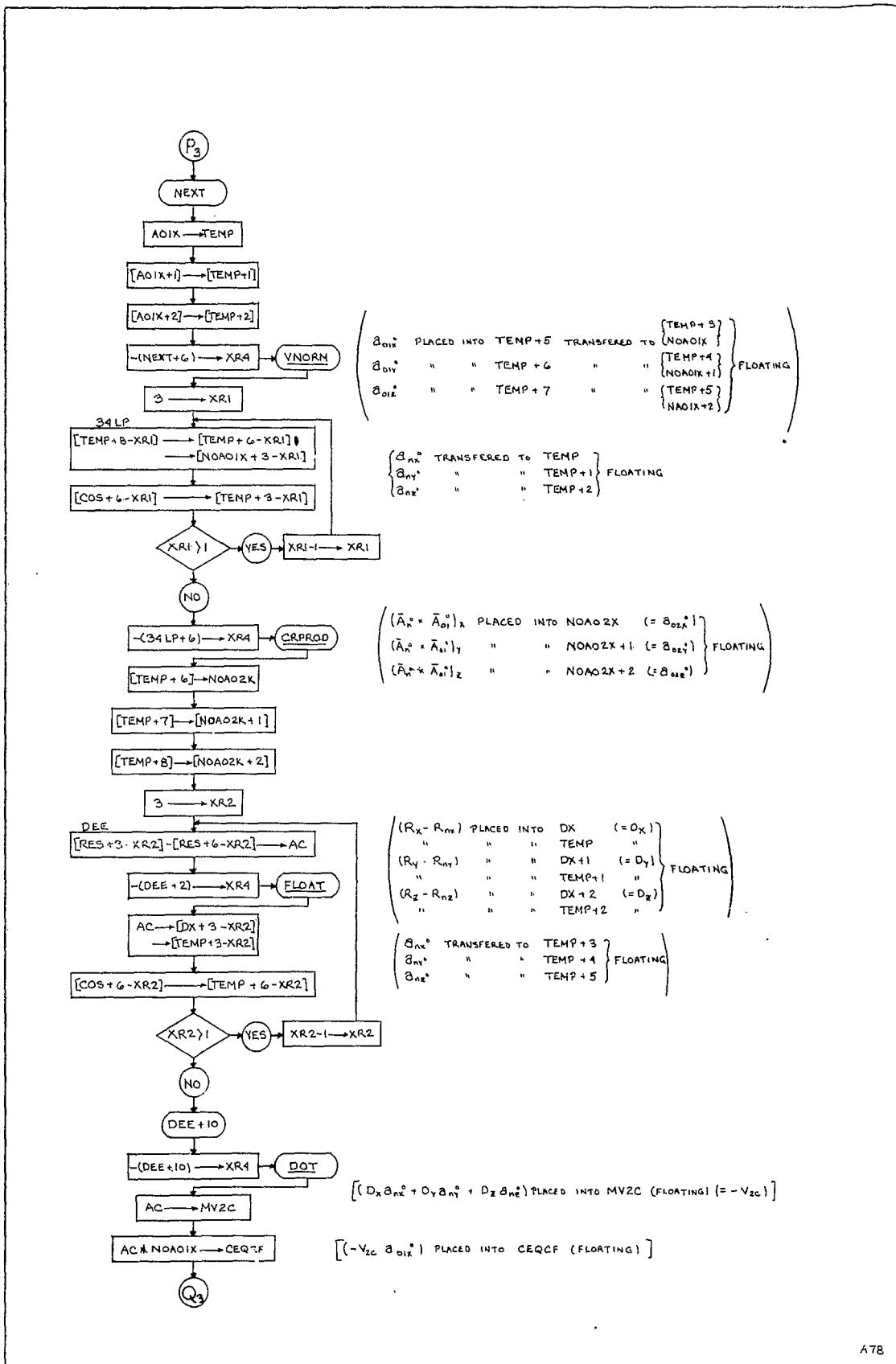


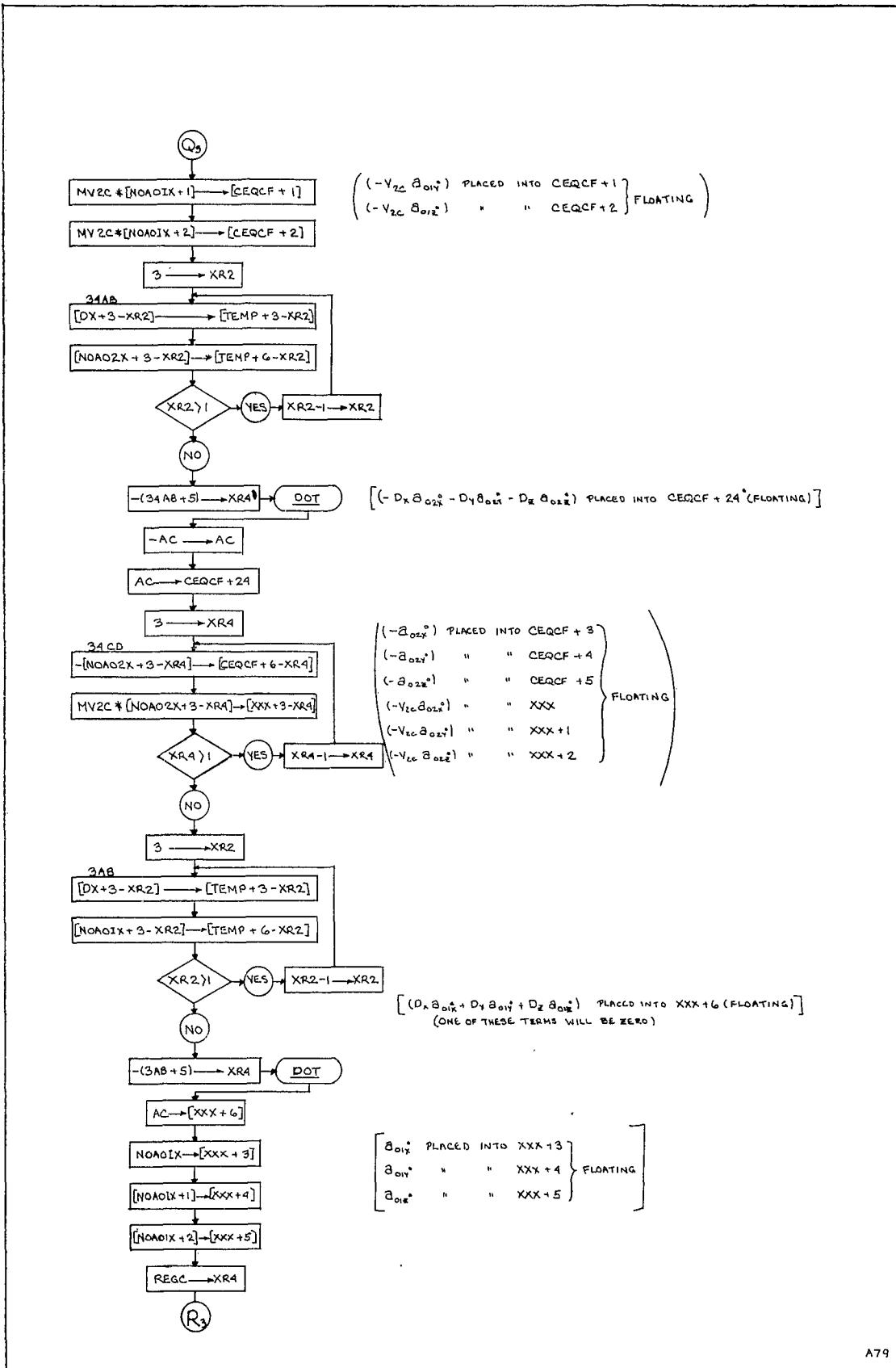
$$\begin{aligned}
 S_x dT_{1x} &+ S_y dT_{1y} &+ S_z dT_{1z} &+ Q_x dR_{1x} &+ Q_y dR_{1y} &+ Q_z dR_{1z} \\
 + (O_x - O'_x) dT_{2x} &+ (O_y - O'_y) dT_{2y} &+ (O_z - O'_z) dT_{2z} &+ (L'_x - Q_x) dR_{2x} &+ (L'_y - Q_y) dR_{2y} &+ (L'_z - Q_z) dR_{2z} \\
 + P_x dT_{3x} &+ P_y dT_{3y} &+ P_z dT_{3z} &+ (-L'_x) dR_{3x} &+ (-L'_y) dR_{3y} &+ (-L'_z) dR_{3z}
 \end{aligned}$$

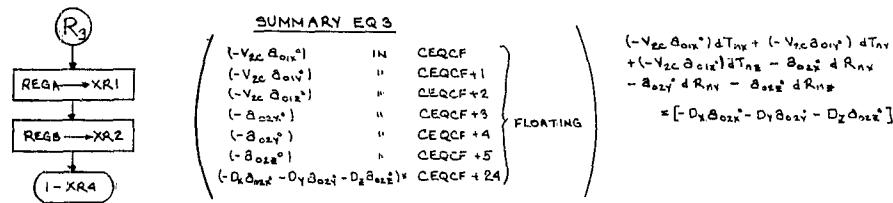
$$= a_2 - a'_2$$

S_x	\rightarrow	CEQCF
S_y	"	CEQCF + 1
S_z	"	CEQCF + 2
Q_x	\rightarrow	CEQCF + 3
Q_y	"	CEQCF + 4
Q_z	"	CEQCF + 5
$(O_x - O'_x)$	"	CEQCF + 6
$(O_y - O'_y)$	"	CEQCF + 7
$(O_z - O'_z)$	"	CEQCF + 8
$(L'_x - Q_x)$	"	CEQCF + 9
$(L'_y - Q_y)$	"	CEQCF + 10
$(L'_z - Q_z)$	"	CEQCF + 11
P_x	\rightarrow	CEQCF + 12
P_y	"	CEQCF + 13
P_z	\rightarrow	CEQCF + 14
$-L'_x$	"	CEQCF + 15
$-L'_y$	"	CEQCF + 16
$-L'_z$	"	CEQCF + 17
$(a_2 - a'_2)$	"	CEQCF + 24







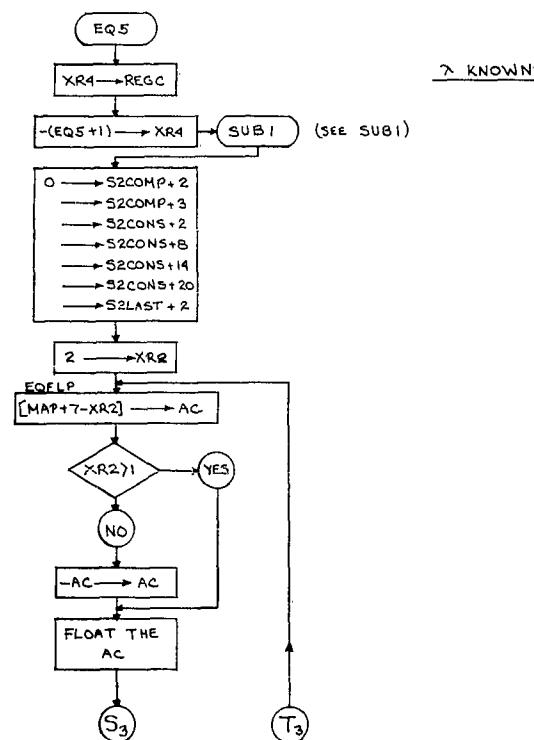


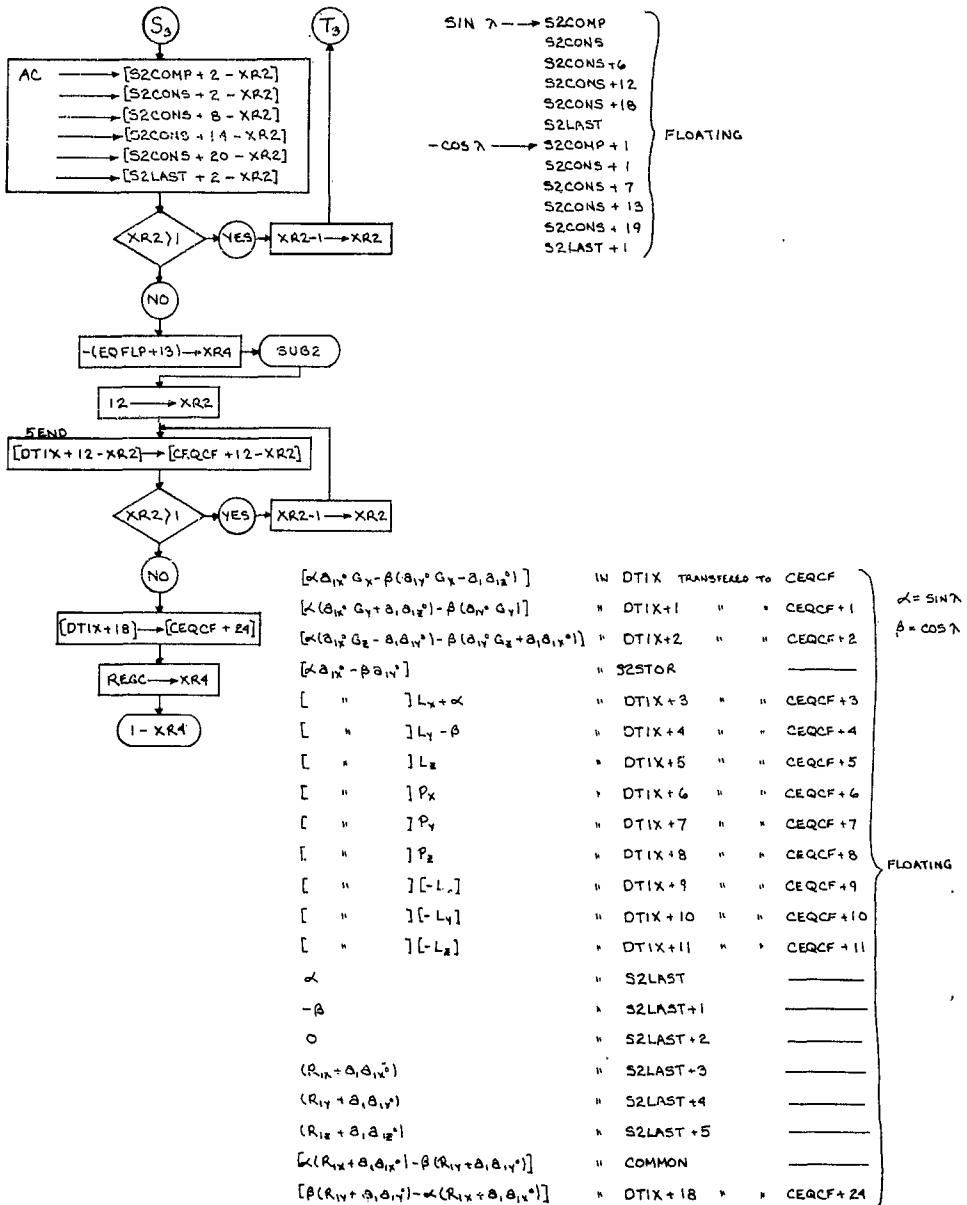
SUMMARY EQ 4

($-V_{2c} \theta_{02x}^*$)	IN	XXX	TRANSFERRED LATER TO	CEQCF	
($-V_{2c} \theta_{02y}^*$)	"	XXX + 1	"	"	CEQCF + 1
($-V_{2c} \theta_{02z}^*$)	"	XXX + 2	"	"	CEQCF + 2
θ_{01x}^*	"	XXX + 3	"	"	CEQCF + 3
θ_{01y}^*	"	XXX + 4	"	"	CEQCF + 4
θ_{01z}^*	"	XXX + 5	"	"	CEQCF + 5
$[D_x \theta_{01x}^* + D_y \theta_{01y}^* + D_z \theta_{01z}^*]$	*	XXX + 6	"	"	CEQCF + 24

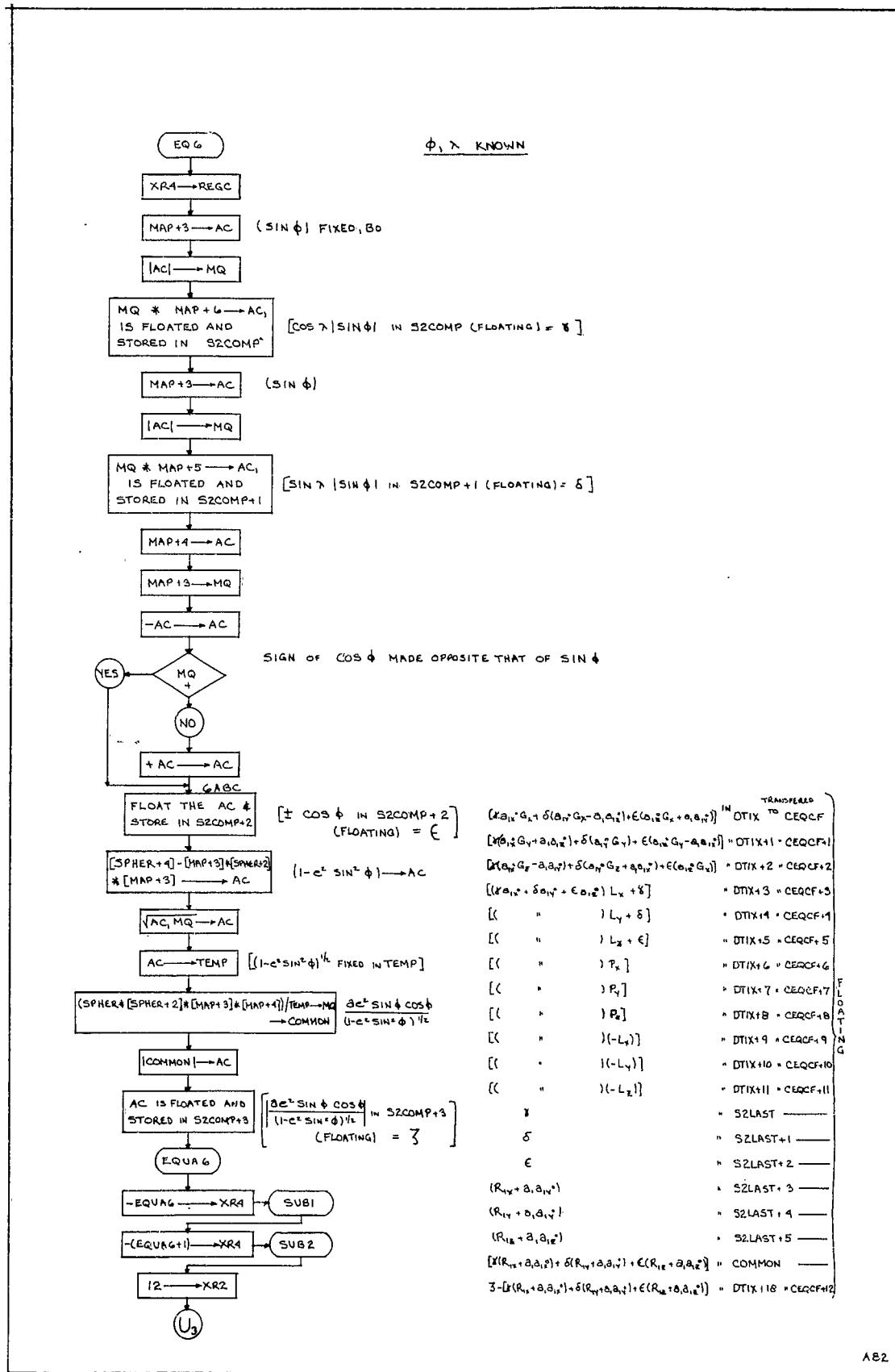
$$(-V_{2c} \theta_{02x}^*) dT_{nx} + (-V_{2c} \theta_{02y}^*) dT_{ny} + (-V_{2c} \theta_{02z}^*) dT_{nz} + \theta_{01x}^* dR_{nx} + \theta_{01y}^* dR_{ny} + \theta_{01z}^* dR_{nz}$$

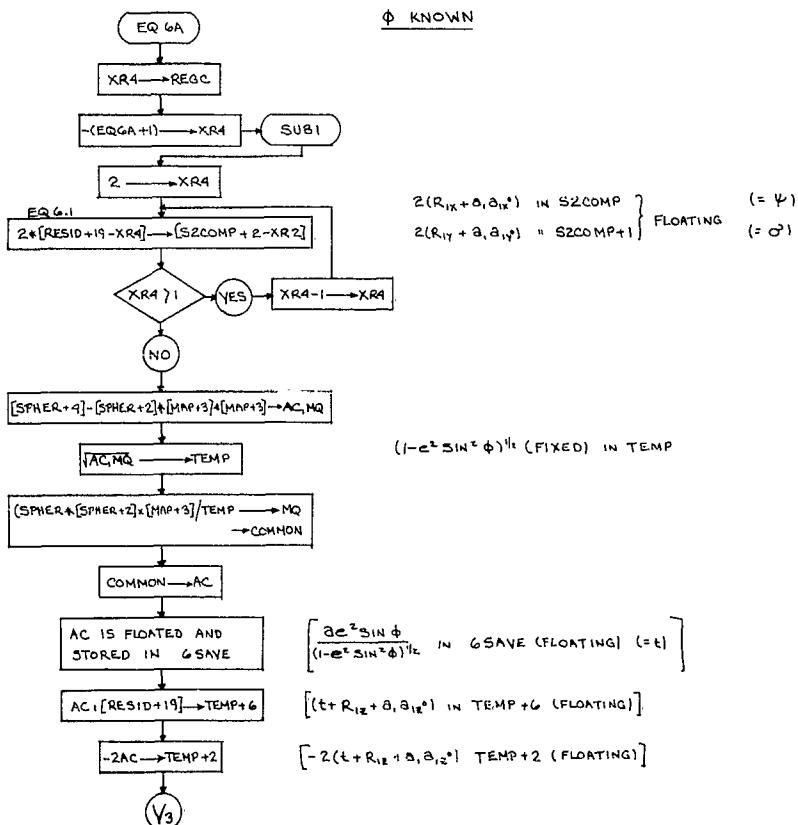
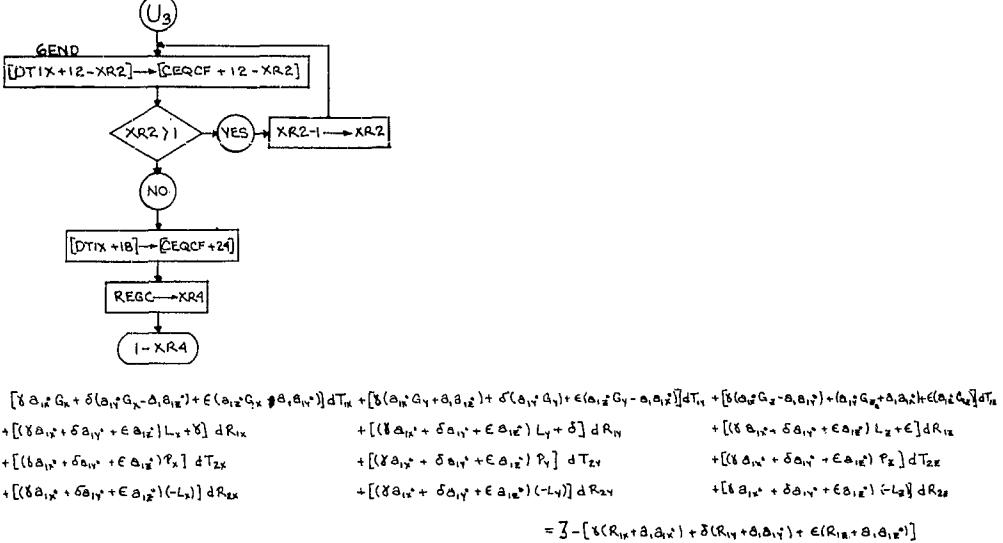
$$= D_x \theta_{01x}^* + D_y \theta_{01y}^* + D_z \theta_{01z}^*$$

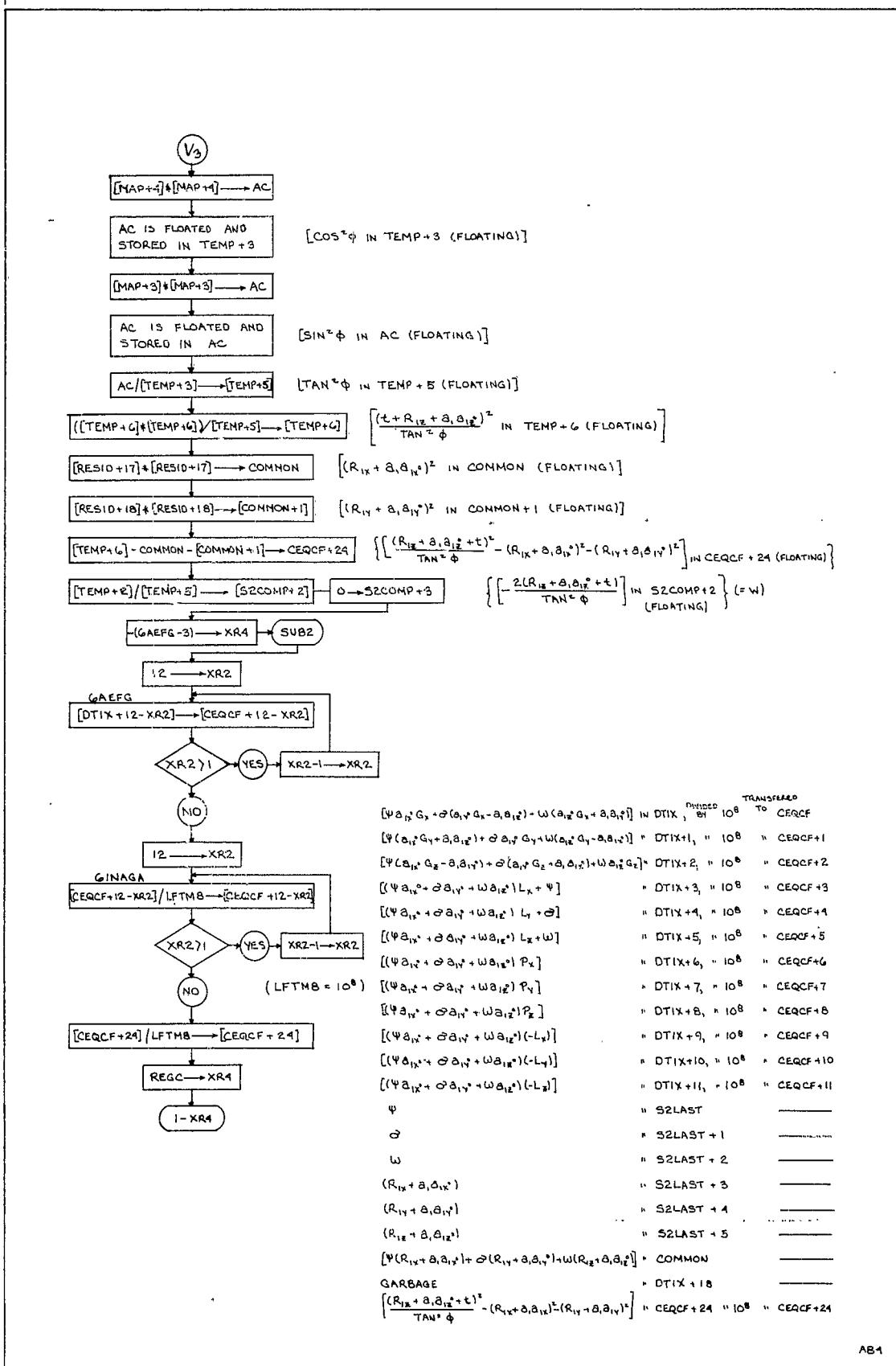




$$\begin{aligned}
& [\alpha A_{1x} G_x - \beta (A_{1y} G_x - A_{1z} A_{1x}^*)] dT_{1x} + [\alpha (A_{1x} G_y + A_{1z} A_{1x}^*) - \beta A_{1y} G_x] dT_{1y} + [\alpha (A_{1x} G_z - A_{1y} A_{1x}^*) - \beta (A_{1y} G_x + A_{1x} A_{1y}^*)] dT_{1z} \\
& + [(A_{1x}^* - \beta A_{1y}^*) L_x + \alpha] dR_{1x} + [(A_{1x}^* - \beta A_{1y}^*) L_y - \beta] dR_{1y} + [(A_{1x}^* - \beta A_{1y}^*) L_z] dR_{1z} \\
& + [(A_{1x}^* - \beta A_{1y}^*) P_x] dT_{2x} + [(A_{1x}^* - \beta A_{1y}^*) P_y] dT_{2y} + [(A_{1x}^* - \beta A_{1y}^*) P_z] dT_{2z} \\
& + [(A_{1x}^* - \beta A_{1y}^*) (-L_x)] dR_{2x} + [(A_{1x}^* - \beta A_{1y}^*) (-L_y)] dR_{2y} + [(A_{1x}^* - \beta A_{1y}^*) (-L_z)] dR_{2z} \\
& = [\beta (R_{1y} + A_{1y} A_{1x}^*) - \alpha (R_{1x} + A_{1y} A_{1x}^*)]
\end{aligned}$$

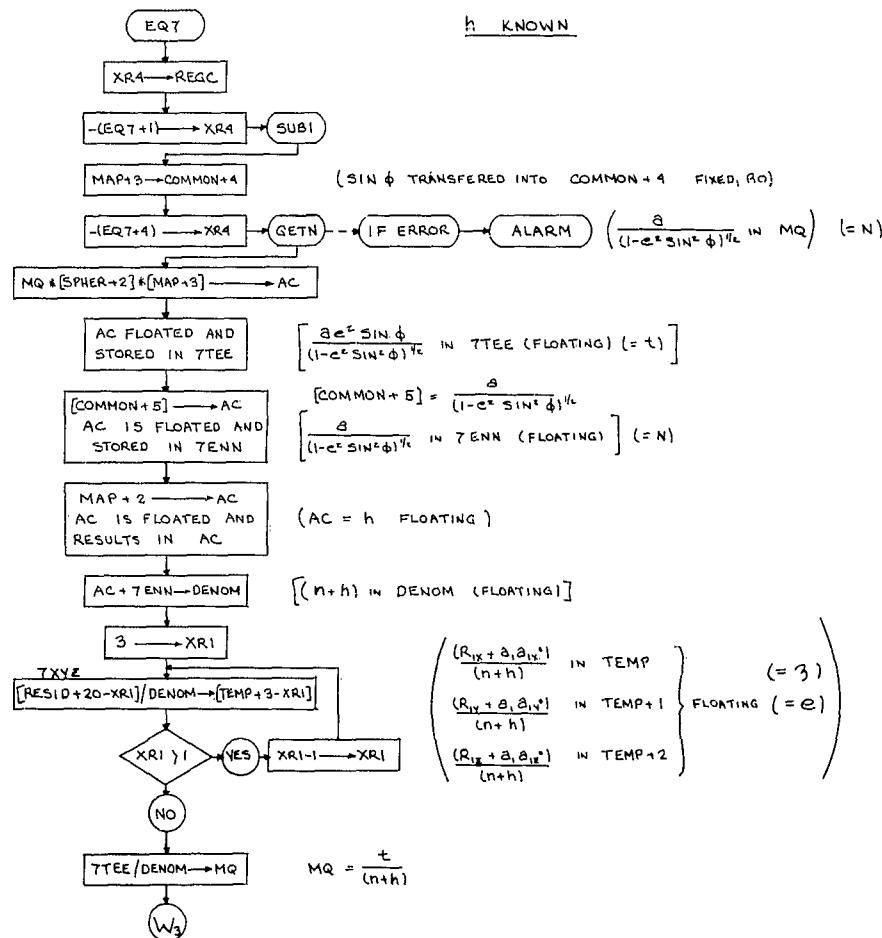


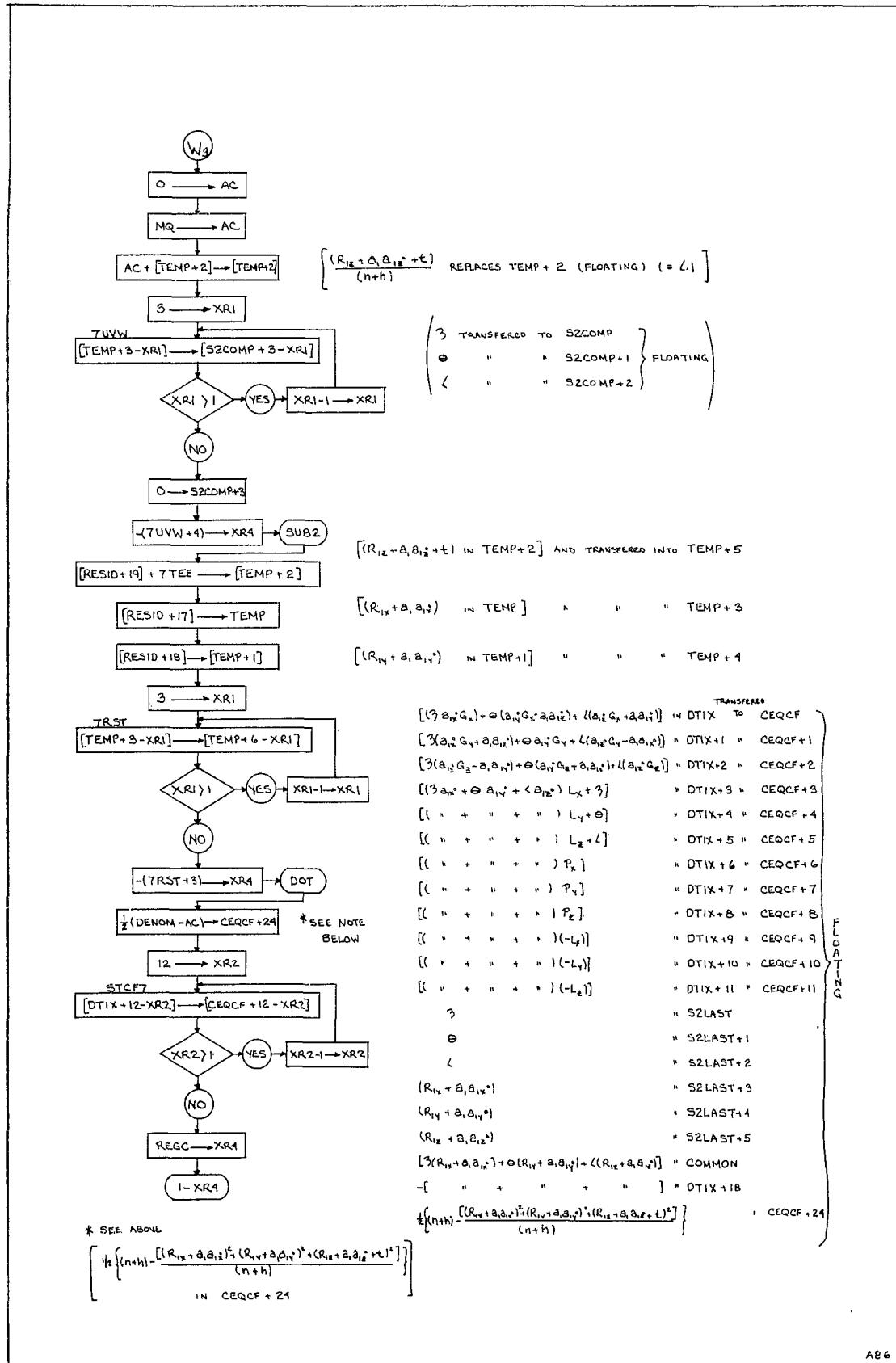




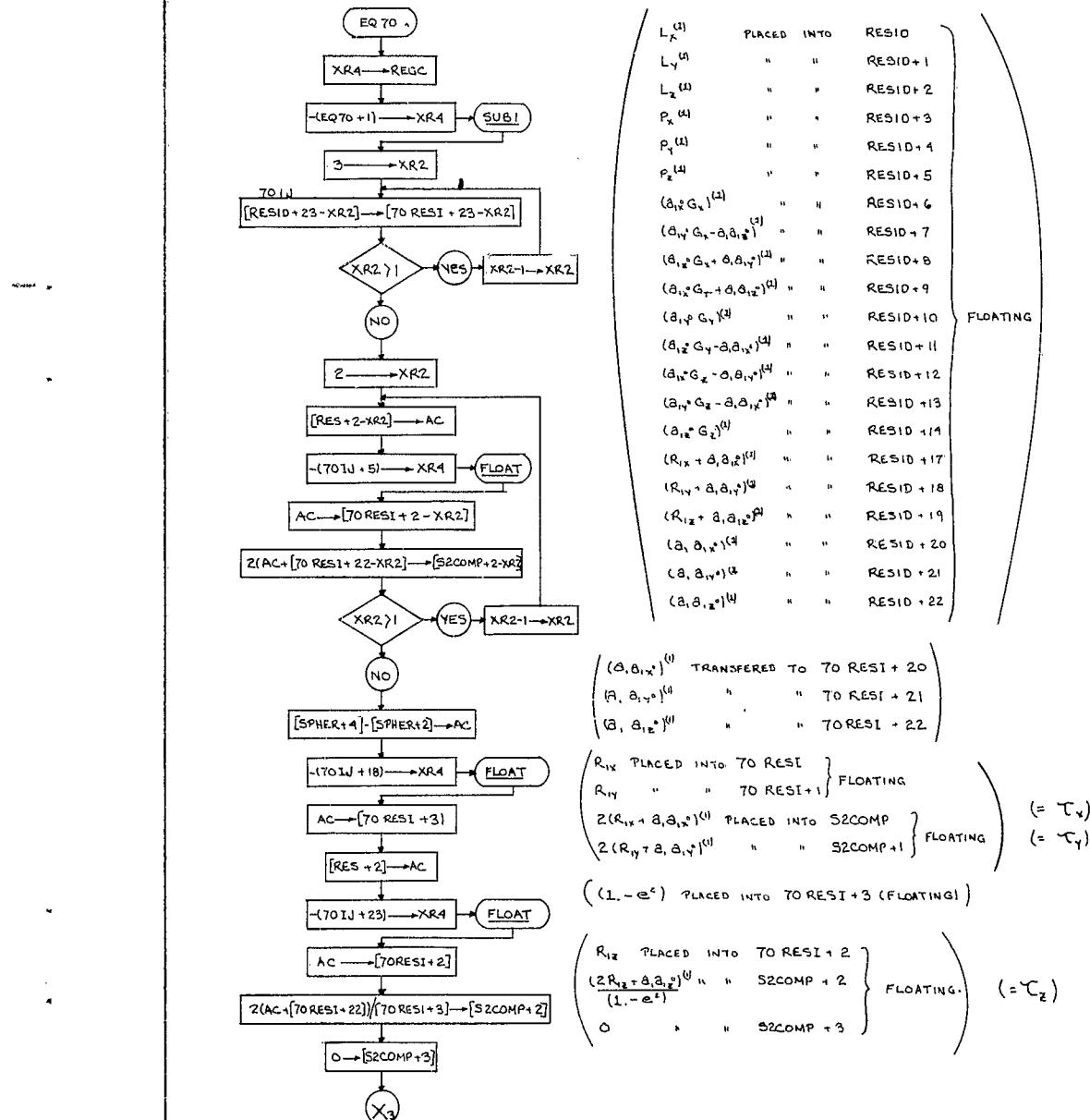
$$\begin{aligned}
& [\Psi \theta_{1x} G_x + \sigma (\theta_{1y} G_y - \theta_{1z} G_z) + W (\theta_{1x}^2 G_x + \theta_{1y}^2 G_y)] dT_{1x} \\
& + [\Psi (\theta_{1x} G_y + \theta_{1z} G_z) + \sigma \theta_{1y} G_y + W (\theta_{1x}^2 G_y - \theta_{1y}^2 G_x)] dT_{1y} \\
& + [\Psi (\theta_{1x} G_z - \theta_{1y} G_y) + \sigma (\theta_{1y} G_x + \theta_{1z} G_y) + W \theta_{1x}^2 G_z] dT_{1z} \\
& + [(\Psi \theta_{1x} + \sigma \theta_{1y} + W \theta_{1z}) L_x + v] dR_{1x} \\
& + [(\theta_{1x} + v + v) L_y + \sigma] dR_{1y} \\
& + [(\theta_{1x} + v + v) L_z + W] dR_{1z} \\
& + [(v + v + v) P_x] dT_{2x} \\
& + [(v + v + v) P_y] dT_{2y} \\
& + [(v + v + v) P_z] dT_{2z} \\
& + [(v + v + v) (-L_x)] dR_{2x} \\
& + [(v + v + v) (-L_y)] dR_{2y} \\
& + [(v + v + v) (-L_z)] dR_{2z}
\end{aligned}$$

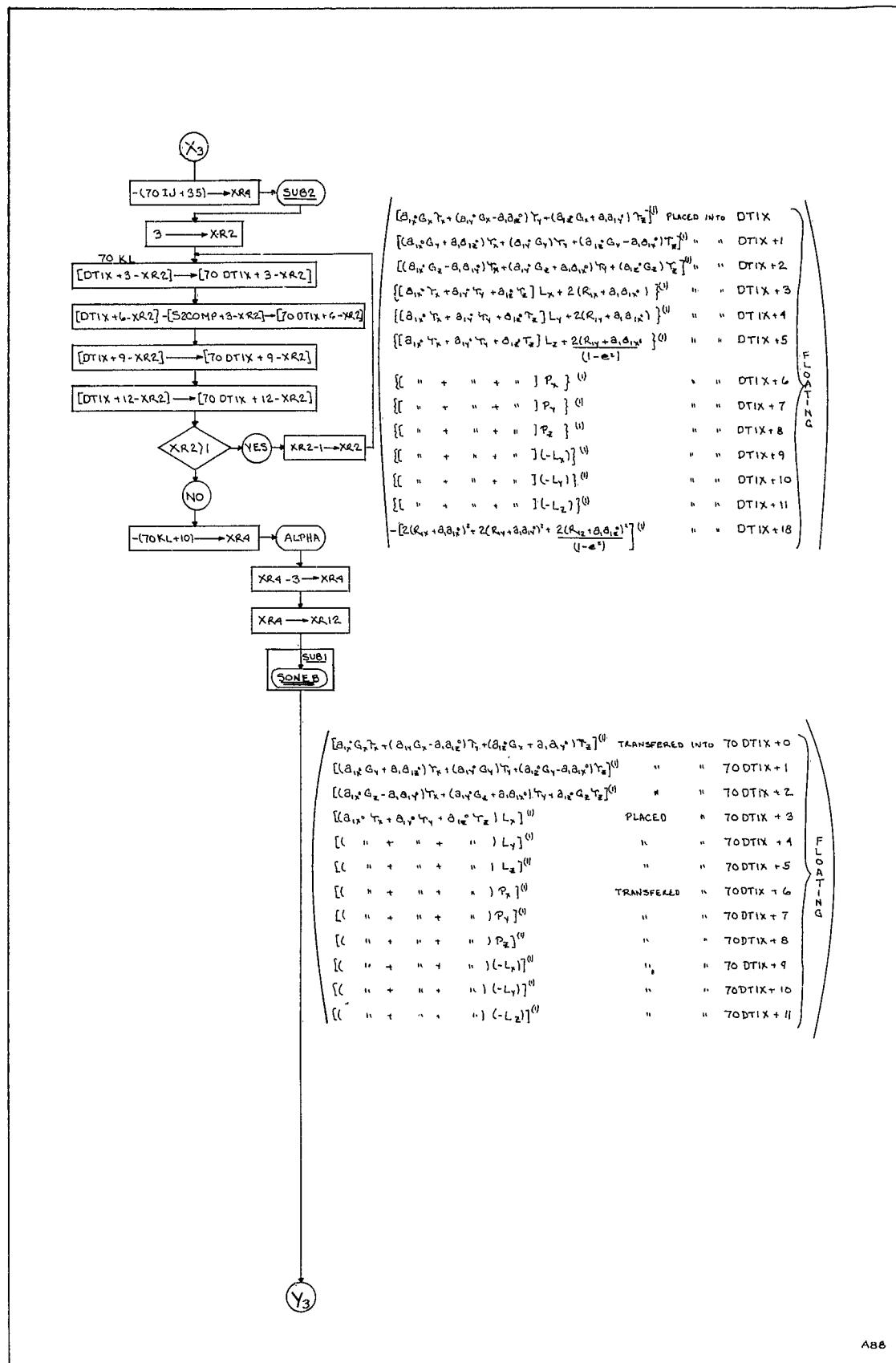
$= \left[\frac{(R_{1x} + \theta_{1x} + v)^2}{\tan^2 \phi} - (R_{1x} + \theta_{1x} + v)^2 - (R_{1y} + \theta_{1y} + v)^2 \right]$

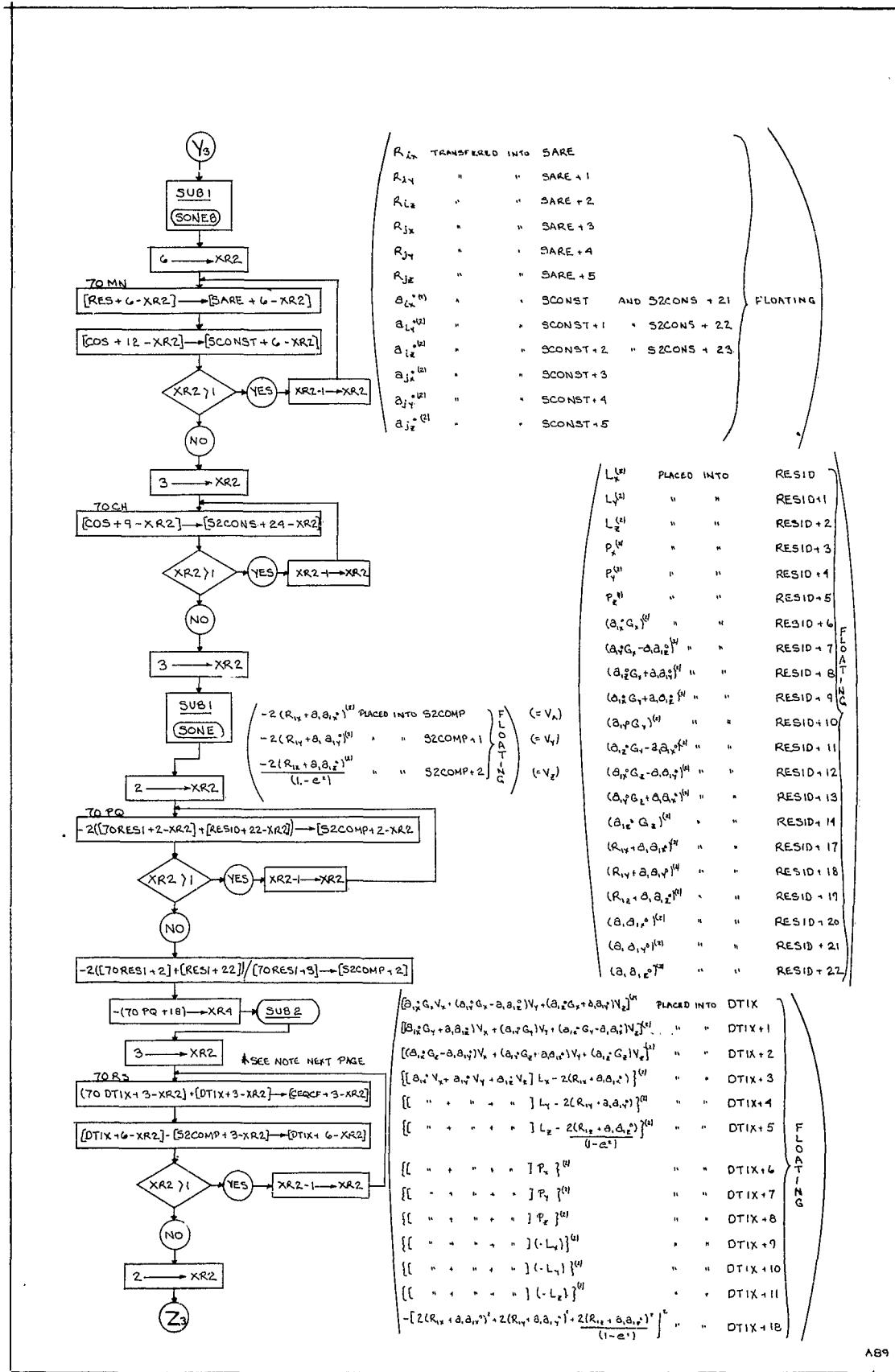


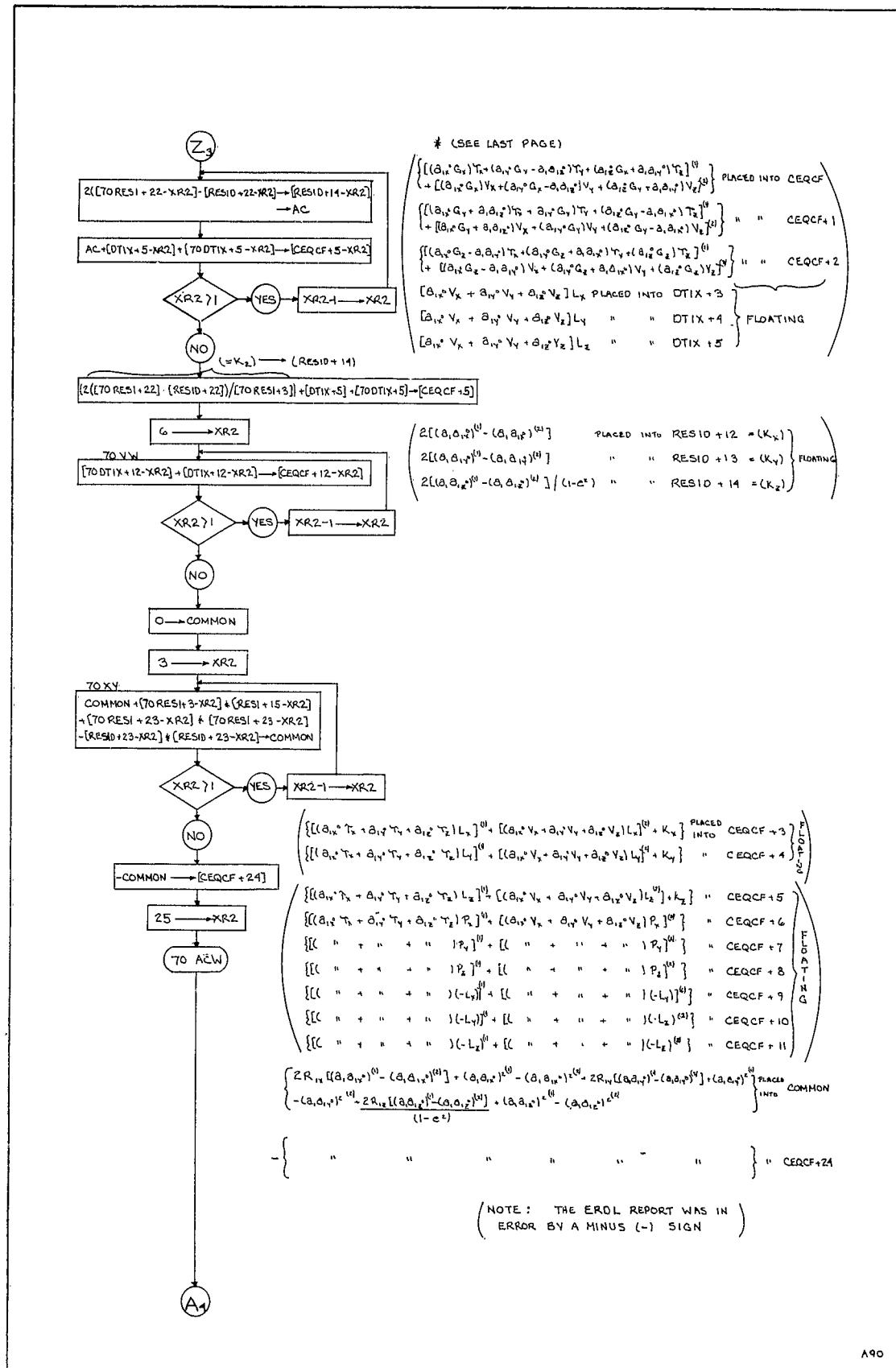


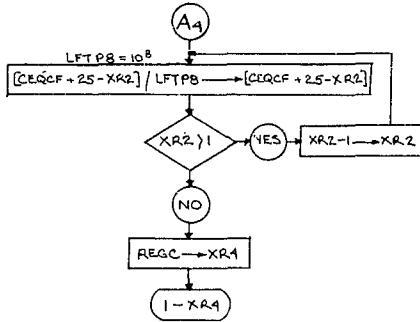
$$\begin{aligned}
& [(3 \alpha_{1x}^* G_x) + \epsilon (\alpha_{1y}^* G_y - \alpha_{1z}^* G_z) + \epsilon (\alpha_{1x}^* G_x + \alpha_{1y}^* G_y)] dT_{1x} + [(3 \alpha_{1y}^* G_y + \alpha_{1z}^* G_z) + \epsilon (\alpha_{1y}^* G_y - \alpha_{1z}^* G_z) + \epsilon (\alpha_{1x}^* G_x + \alpha_{1y}^* G_y)] dT_{1y} + [(3 \alpha_{1z}^* G_z - \alpha_{1x}^* G_x) + \epsilon (\alpha_{1z}^* G_z + \alpha_{1x}^* G_x)] dT_{1z} \\
& + [(3 \alpha_{1x}^* + \epsilon \alpha_{1y}^* + \epsilon \alpha_{1z}^*) L_x + 3] dR_{1x} \\
& + [(3 \alpha_{1y}^* + \epsilon \alpha_{1z}^*) P_x] dT_{2x} \\
& + [(3 \alpha_{1z}^* + \epsilon \alpha_{1x}^* + \epsilon \alpha_{1y}^*) (-L_x)] dR_{2x} \\
& + [(3 \alpha_{1x}^* + \epsilon \alpha_{1y}^* + \epsilon \alpha_{1z}^*) L_y + \epsilon] dR_{1y} \\
& + [(3 \alpha_{1y}^* + \epsilon \alpha_{1z}^*) P_y] dT_{2y} \\
& + [(3 \alpha_{1z}^* + \epsilon \alpha_{1x}^*) (-L_y)] dR_{2y} \\
& + [(3 \alpha_{1x}^* + \epsilon \alpha_{1y}^* + \epsilon \alpha_{1z}^*) L_z + \epsilon] dR_{1z} \\
& + [(3 \alpha_{1y}^* + \epsilon \alpha_{1z}^*) P_z] dT_{2z} \\
& + [(3 \alpha_{1z}^* + \epsilon \alpha_{1x}^*) (-L_z)] dR_{2z} \\
= & \frac{1}{2} \left\{ (n+h) - \frac{[(R_{1x} + \alpha_{1x}^* G_x)^2 + (R_{1y} + \alpha_{1y}^* G_y)^2 + (R_{1z} + \alpha_{1z}^* G_z)^2]}{(n+h)} \right\}
\end{aligned}$$









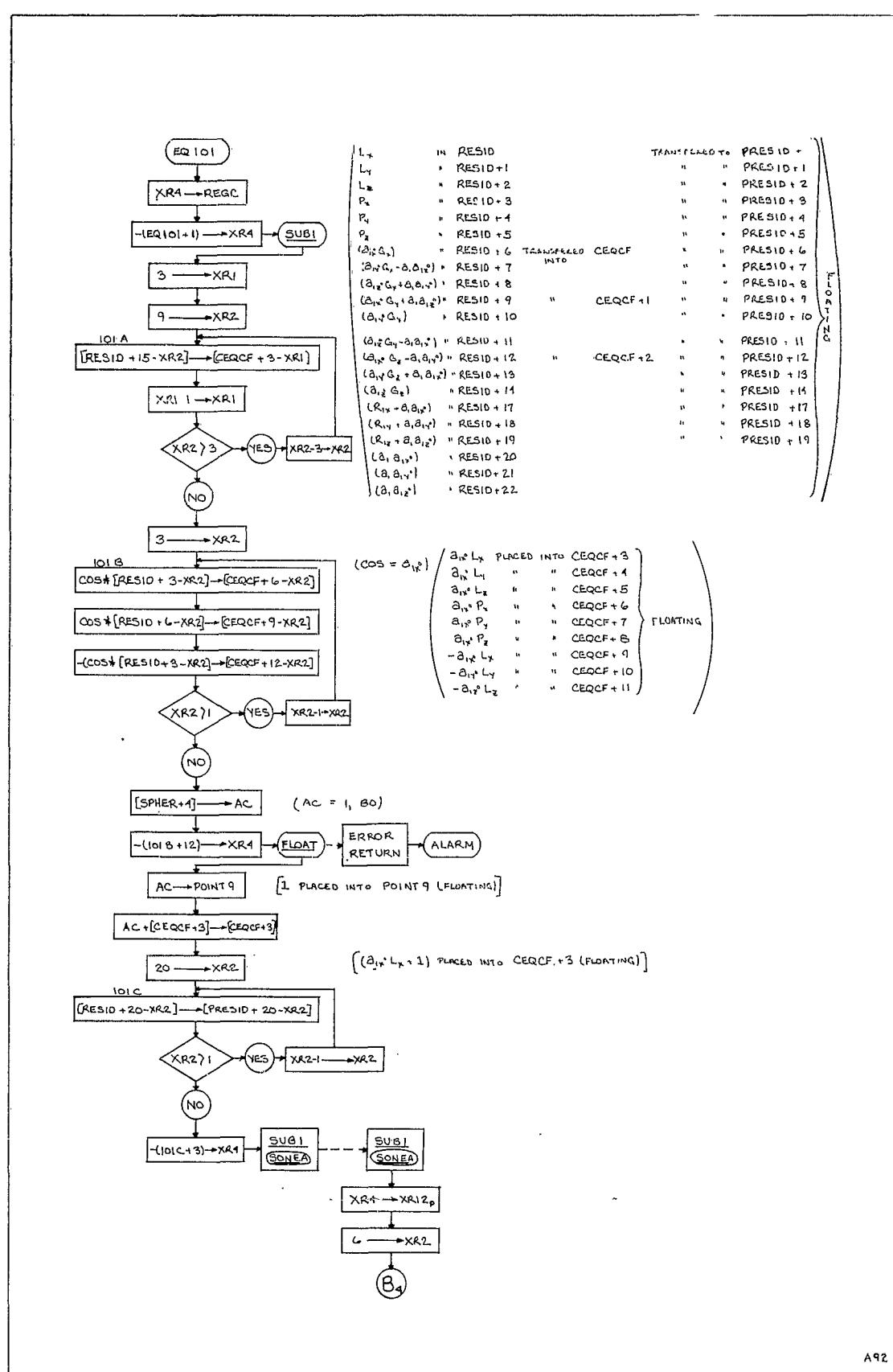


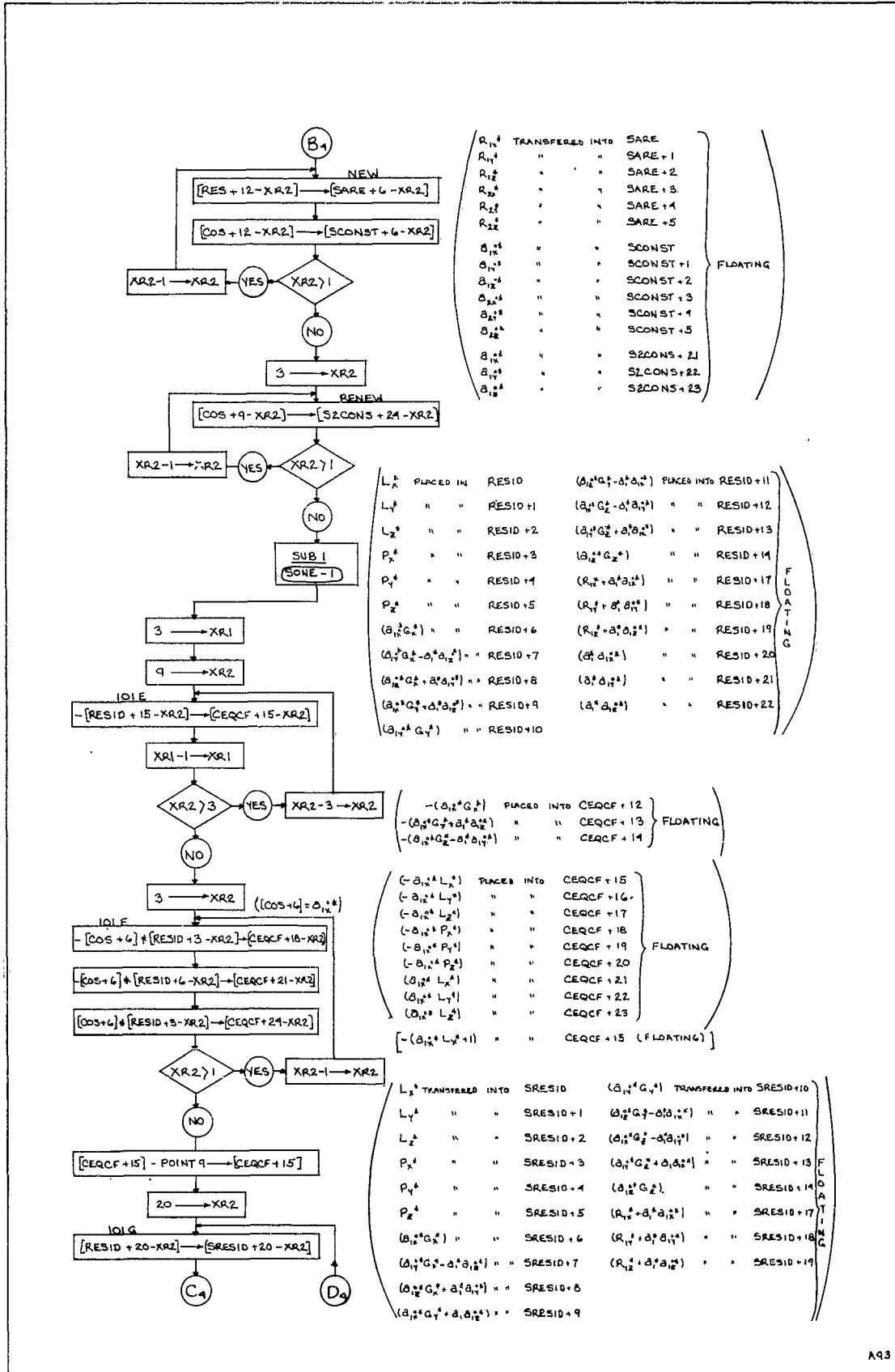
SUMMARY OF EQUATION 70

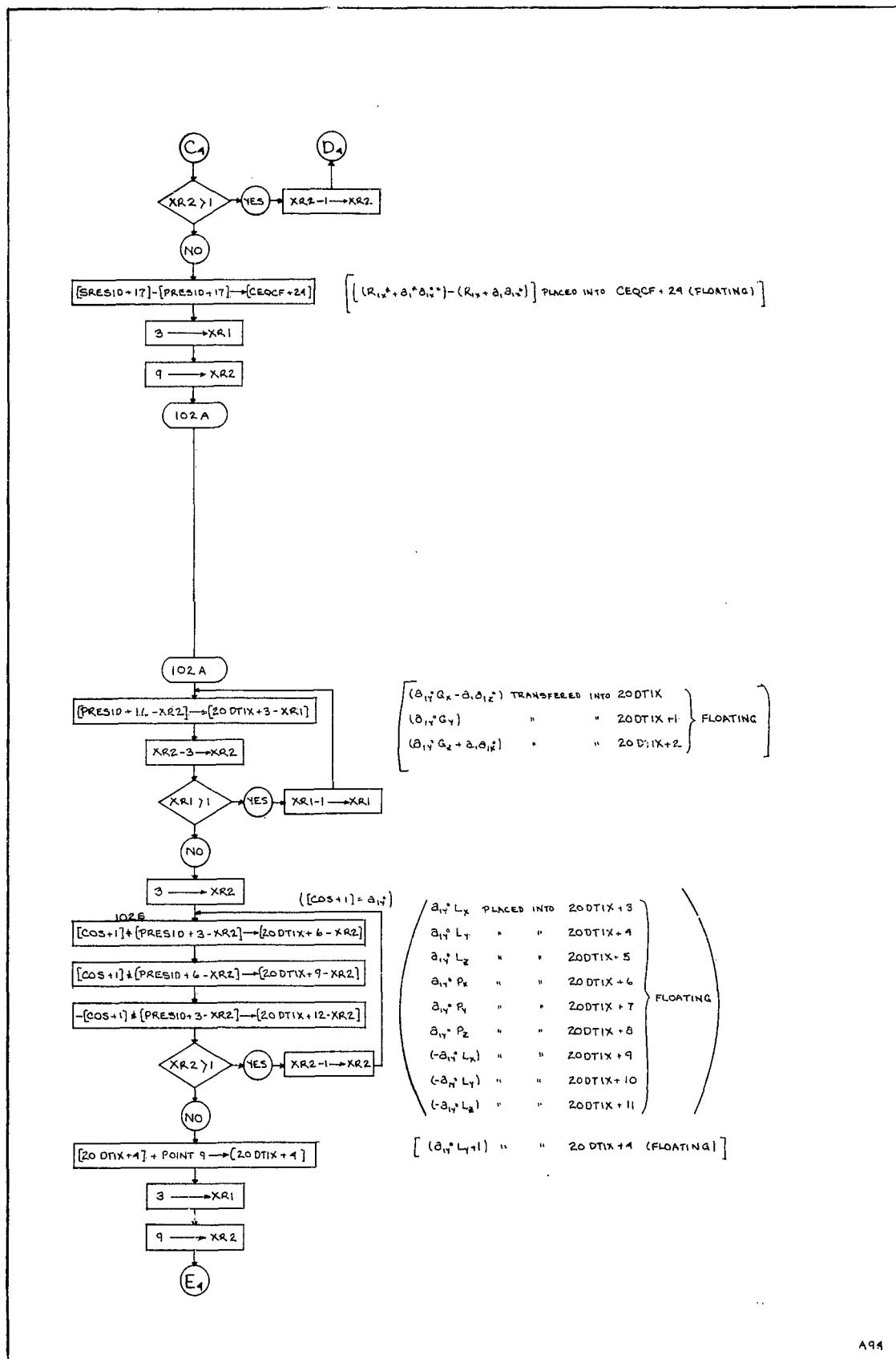
$\left\{ \left[(A_{11} \cdot G_x) T_x + (A_{12} \cdot G_y - A_{13}) T_y + (A_{14} \cdot G_z - A_{15}) T_z \right]^W + \left[(A_{11} \cdot G_x) V_x + (A_{12} \cdot G_y + A_{13}) V_y + (A_{14} \cdot G_z + A_{15}) V_z \right]^W \right\} / 10^8 \quad \text{PLACED INTO CEQCF}$
 $\left\{ (A_{11} \cdot G_x + A_{12} \cdot G_y + A_{13}) T_x + (A_{12} \cdot G_y - A_{13}) T_z \right\}^W + \left\{ (A_{11} \cdot G_y + A_{12} \cdot G_z + A_{14}) V_x + (A_{12} \cdot G_z - A_{14}) V_y + (A_{13} \cdot G_x + A_{15}) V_z \right\} / 10^8 \quad " \quad \text{CEQCF + 1}$
 $\left\{ (A_{11} \cdot G_x - A_{13}) T_y + (A_{12} \cdot G_z + A_{14}) T_z \right\}^W + \left\{ (A_{11} \cdot G_x - A_{13}) V_x + (A_{12} \cdot G_z + A_{14}) V_y + (A_{13} \cdot G_x) V_z \right\} / 10^8 \quad " \quad \text{CEQCF + 2}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (L_x) \right\}^W + K_x \} / 10^8 \quad " \quad \text{CEQCF + 3}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (L_y) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (L_y) \right\}^W + K_y \} / 10^8 \quad " \quad \text{CEQCF + 4}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (L_z) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (L_z) \right\}^W + K_z \} / 10^8 \quad " \quad \text{CEQCF + 5}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (P_x) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (P_x) \right\}^W / 10^8 \quad " \quad \text{CEQCF + 6}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (P_y) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (P_y) \right\}^W / 10^8 \quad " \quad \text{CEQCF + 7}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (P_z) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (P_z) \right\}^W / 10^8 \quad " \quad \text{CEQCF + 8}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (-L_x) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (-L_x) \right\}^W / 10^8 \quad " \quad \text{CEQCF + 9}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (-L_y) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (-L_y) \right\}^W / 10^8 \quad " \quad \text{CEQCF + 10}$
 $\left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (-L_z) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (-L_z) \right\}^W / 10^8 \quad " \quad \text{CEQCF + 11}$
 $- \left\{ 2 R_{1x} K_x + (A_{11} \cdot V_x)^W (A_{12} \cdot V_y)^W + 2 R_{1y} K_y + (A_{11} \cdot V_y)^W (A_{13} \cdot V_z)^W - (A_{12} \cdot V_x)^W (A_{13} \cdot V_z)^W \right\} / 10^8 \quad " \quad \text{CEQCF + 24}$

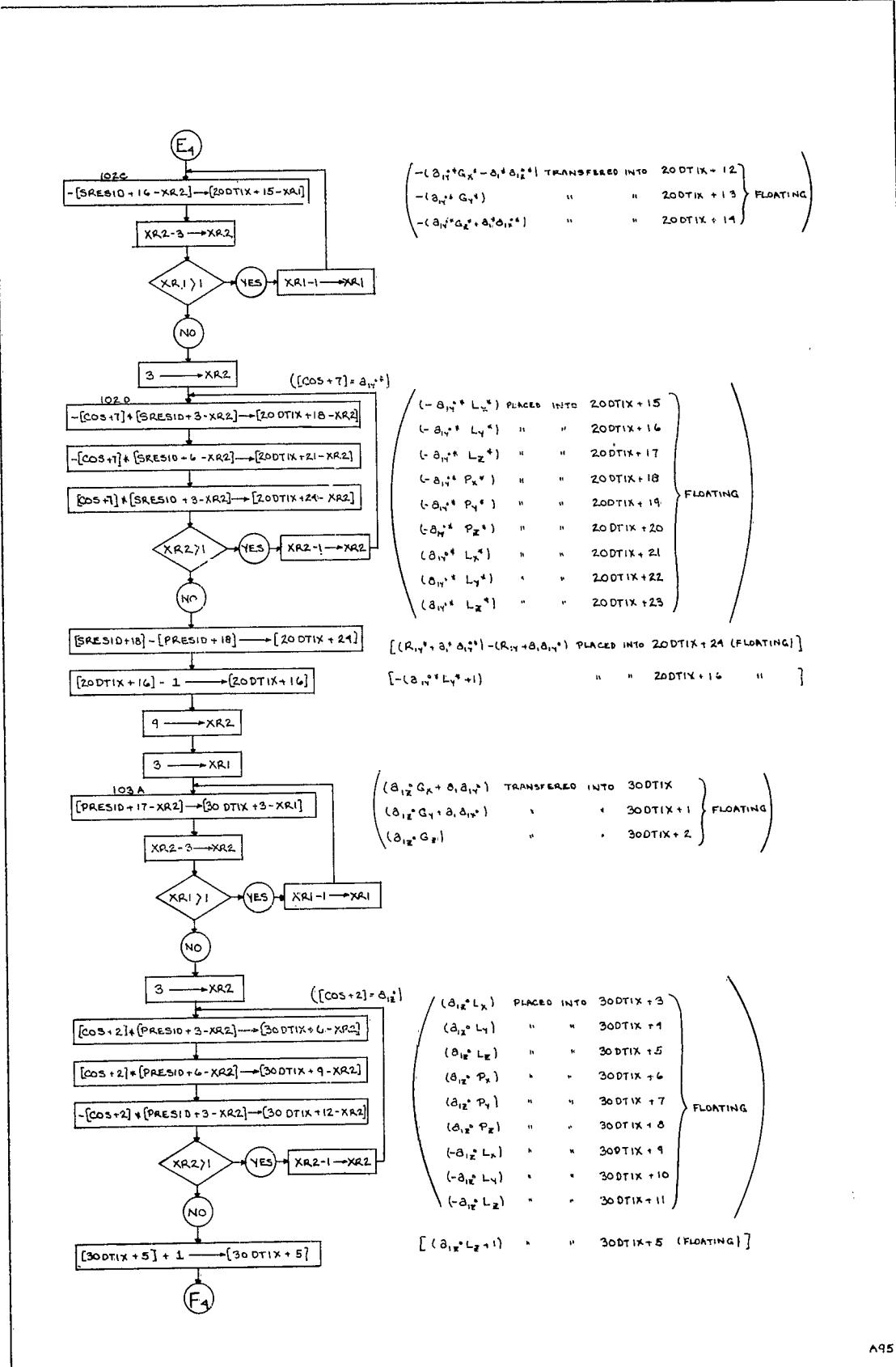
* NOTE THE / 10⁸ WORKING FACTOR

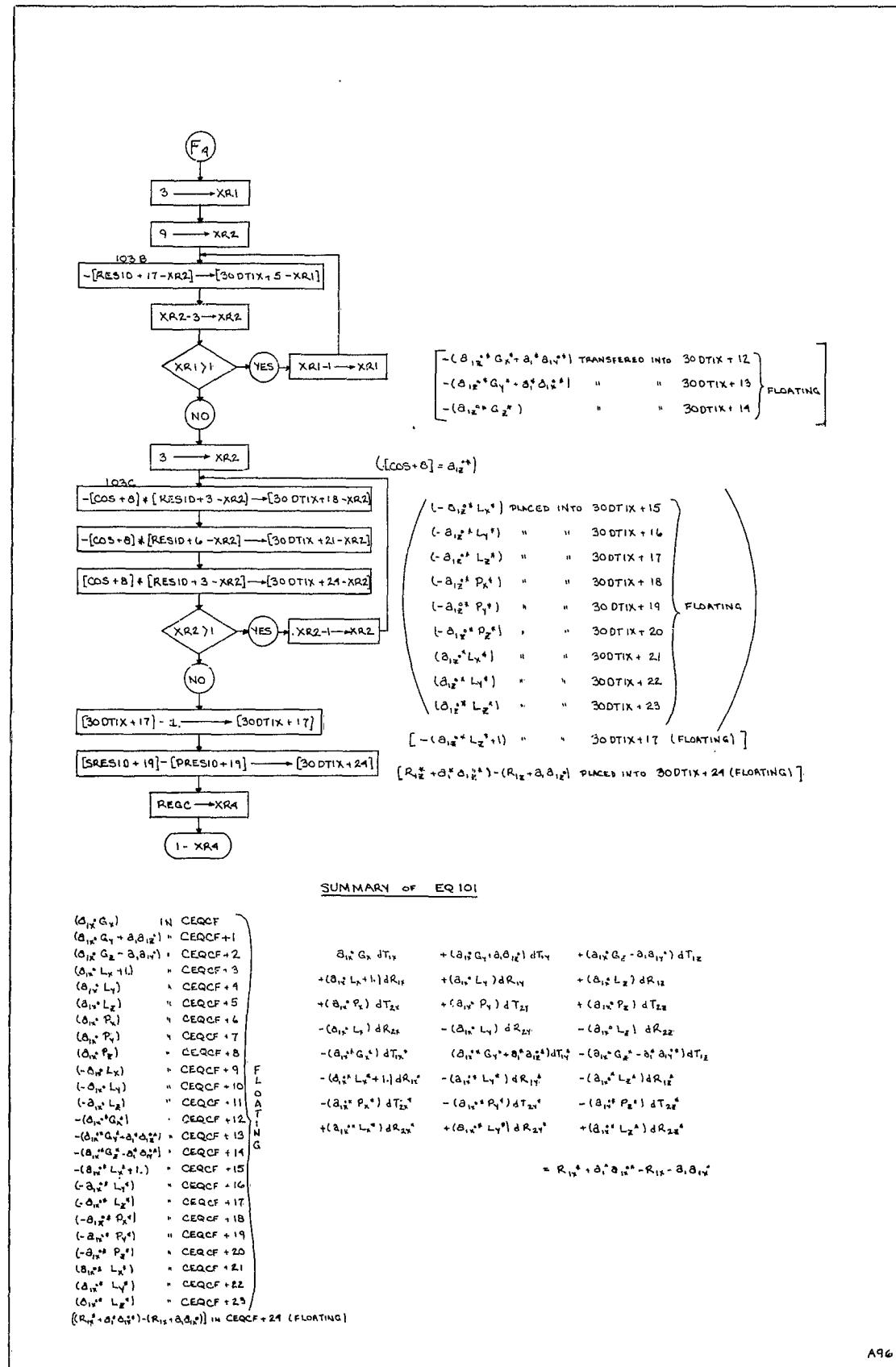
$$\begin{aligned}
& \left\{ (A_{11} \cdot G_x) T_x + (A_{12} \cdot G_y - A_{13}) T_y + (A_{14} \cdot G_z - A_{15}) T_z \right\}^W + \left\{ (A_{11} \cdot G_x) V_x + (A_{12} \cdot G_y + A_{13}) V_y + (A_{14} \cdot G_z + A_{15}) V_z \right\}^W dT_{1x} \\
& + \left\{ (A_{11} \cdot G_y + A_{12}) T_x + (A_{13} \cdot G_y + A_{14}) T_y + (A_{15} \cdot G_y - A_{11}) T_z \right\}^W + \left\{ (A_{11} \cdot G_y + A_{12}) V_x + (A_{13} \cdot G_y + A_{14}) V_y + (A_{15} \cdot G_y - A_{11}) V_z \right\}^W dT_{1y} \\
& + \left\{ (A_{11} \cdot G_z - A_{14}) T_x + (A_{12} \cdot G_z + A_{13}) T_y + (A_{15} \cdot G_z + A_{11}) T_z \right\}^W + \left\{ (A_{11} \cdot G_z - A_{14}) V_x + (A_{12} \cdot G_z + A_{13}) V_y + (A_{15} \cdot G_z + A_{11}) V_z \right\}^W dT_{1z} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) L_x \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) L_x \right\}^W + K_x \} dR_{1x} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) L_y \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) L_y \right\}^W + K_y \} dR_{1y} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) L_z \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) L_z \right\}^W + K_z \} dR_{1z} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) P_x \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) P_x \right\}^W dT_{2x} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) P_y \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) P_y \right\}^W dT_{2y} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) P_z \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) P_z \right\}^W dT_{2z} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (-L_x) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (-L_x) \right\}^W dR_{2x} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (-L_y) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (-L_y) \right\}^W dR_{2y} \\
& + \left\{ (A_{11} \cdot T_x + A_{12} \cdot T_y + A_{13} \cdot T_z) (-L_z) \right\}^W + \left\{ (A_{11} \cdot V_x + A_{12} \cdot V_y + A_{13} \cdot V_z) (-L_z) \right\}^W dR_{2z} \\
& = \left\{ R_{1x} K_x + (A_{11})^W - (A_{12})^W + R_{1y} K_y + (A_{11})^W - (A_{13})^W + R_{1z} K_z + (A_{11})^W - (A_{14})^W \right\}
\end{aligned}$$









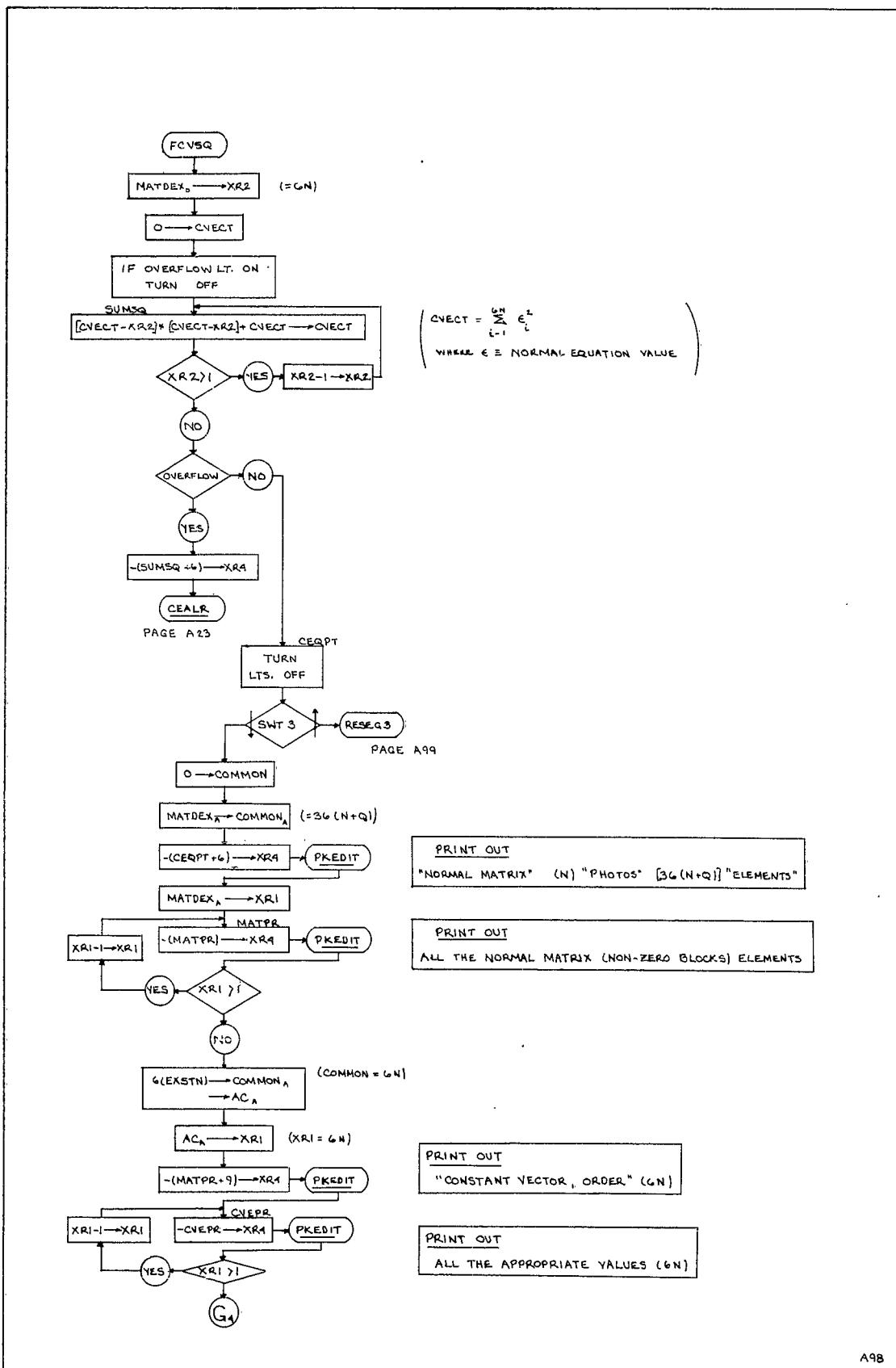


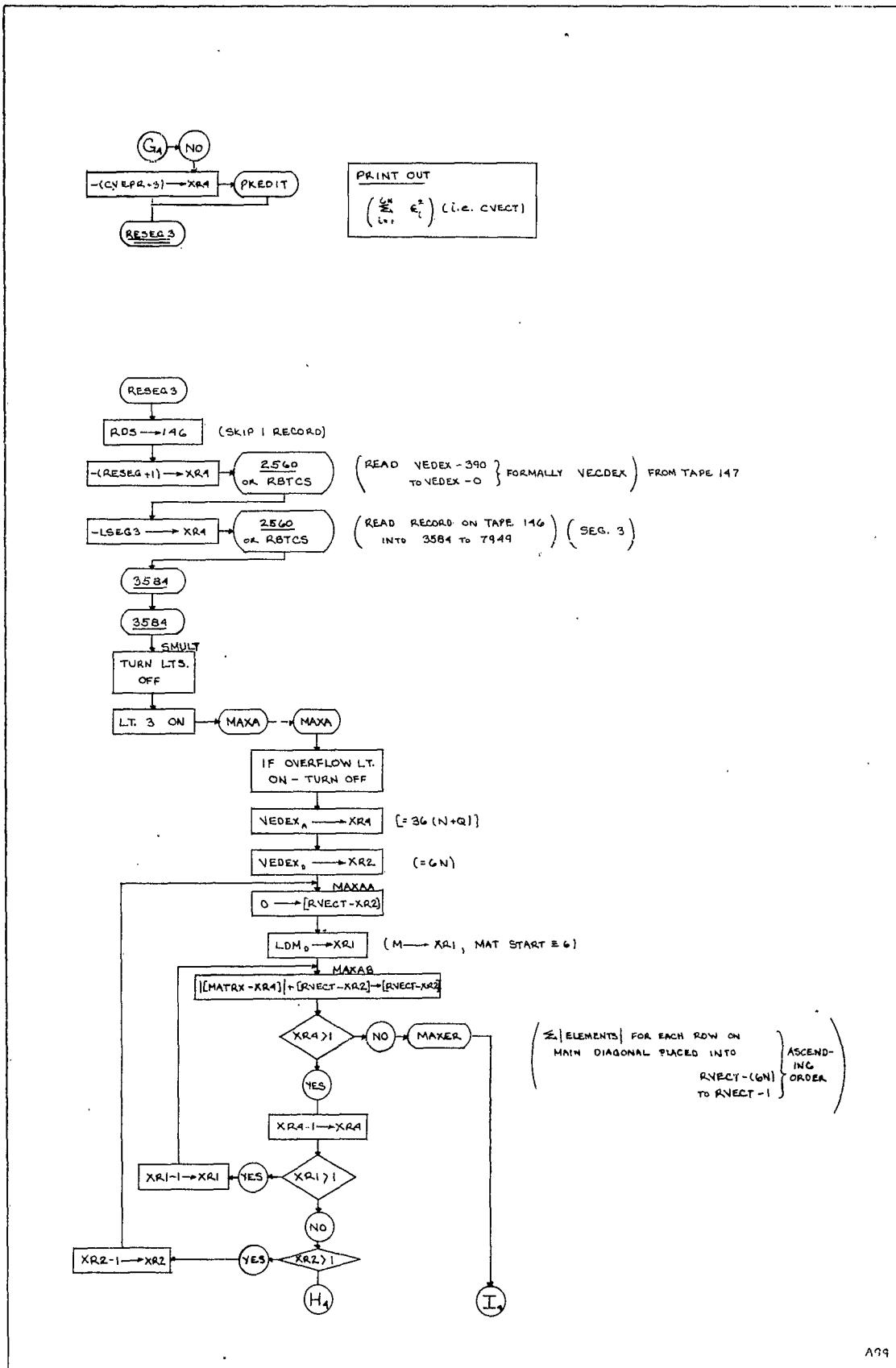
SUMMARY OF EQ 102

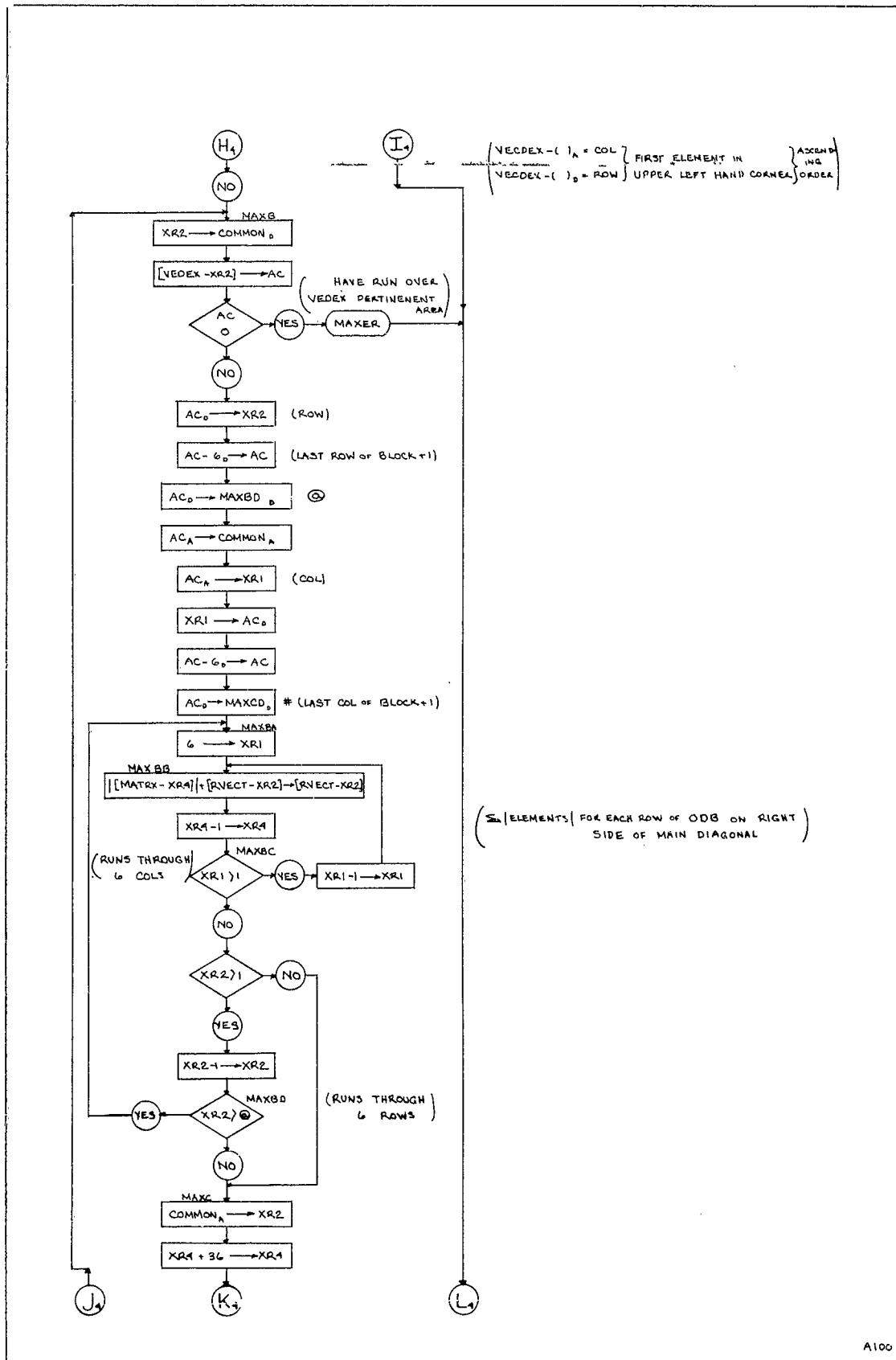
$(\partial_{11}^* G_x - \partial_1 \partial_{11}^*)$ IN	20DTIX	TRANSFERRED	CEQCF
$(\partial_{11}^* G_y)$	"	20DTIX+1	LATER INTO
$(\partial_{11}^* G_z)$	"	20DTIX+2	CEQCF+1
$(\partial_{11}^* L_x)$	"	20DTIX+3	CEQCF+2
$(\partial_{11}^* L_y + 1)$	"	20DTIX+4	CEQCF+3
$(\partial_{11}^* L_z)$	"	20DTIX+5	CEQCF+4
$(\partial_{11}^* P_x)$	"	20DTIX+6	CEQCF+5
$(\partial_{11}^* P_y)$	"	20DTIX+7	CEQCF+6
$(\partial_{11}^* P_z)$	"	20DTIX+8	CEQCF+7
$(-\partial_{11}^* L_x)$	"	20DTIX+9	CEQCF+8
$(-\partial_{11}^* L_y)$	"	20DTIX+10	CEQCF+9
$(-\partial_{11}^* L_z)$	"	20DTIX+11	CEQCF+10
$(-\partial_{11}^* G_x^2 - \partial_1^2 \partial_{11}^2)$	"	20DTIX+12	CEQCF+11
$(-\partial_{11}^* G_y^2)$	"	20DTIX+13	CEQCF+12
$(-\partial_{11}^* G_z^2)$	"	20DTIX+14	CEQCF+13
$(-\partial_{11}^* G_x^2 - \partial_1^2 \partial_{11}^2)$	"	20DTIX+15	CEQCF+14
$(-\partial_{11}^* G_y^2)$	"	20DTIX+16	CEQCF+15
$(-\partial_{11}^* G_z^2)$	"	20DTIX+17	CEQCF+16
$(-\partial_{11}^* P_x)$	"	20DTIX+18	CEQCF+17
$(-\partial_{11}^* P_y)$	"	20DTIX+19	CEQCF+18
$(-\partial_{11}^* P_z)$	"	20DTIX+20	CEQCF+19
$(\partial_{11}^* L_x^2)$	"	20DTIX+21	CEQCF+20
$(\partial_{11}^* L_y^2)$	"	20DTIX+22	CEQCF+21
$(\partial_{11}^* L_z^2)$	"	20DTIX+23	CEQCF+22
$[(R_{11}^* + \partial_1^* \partial_{11}^*) - (R_{11} + \partial_1 \partial_{11})]$ IN	20DTIX+24	CEQCF+23	
		20DTIX+24	CEQCF+24

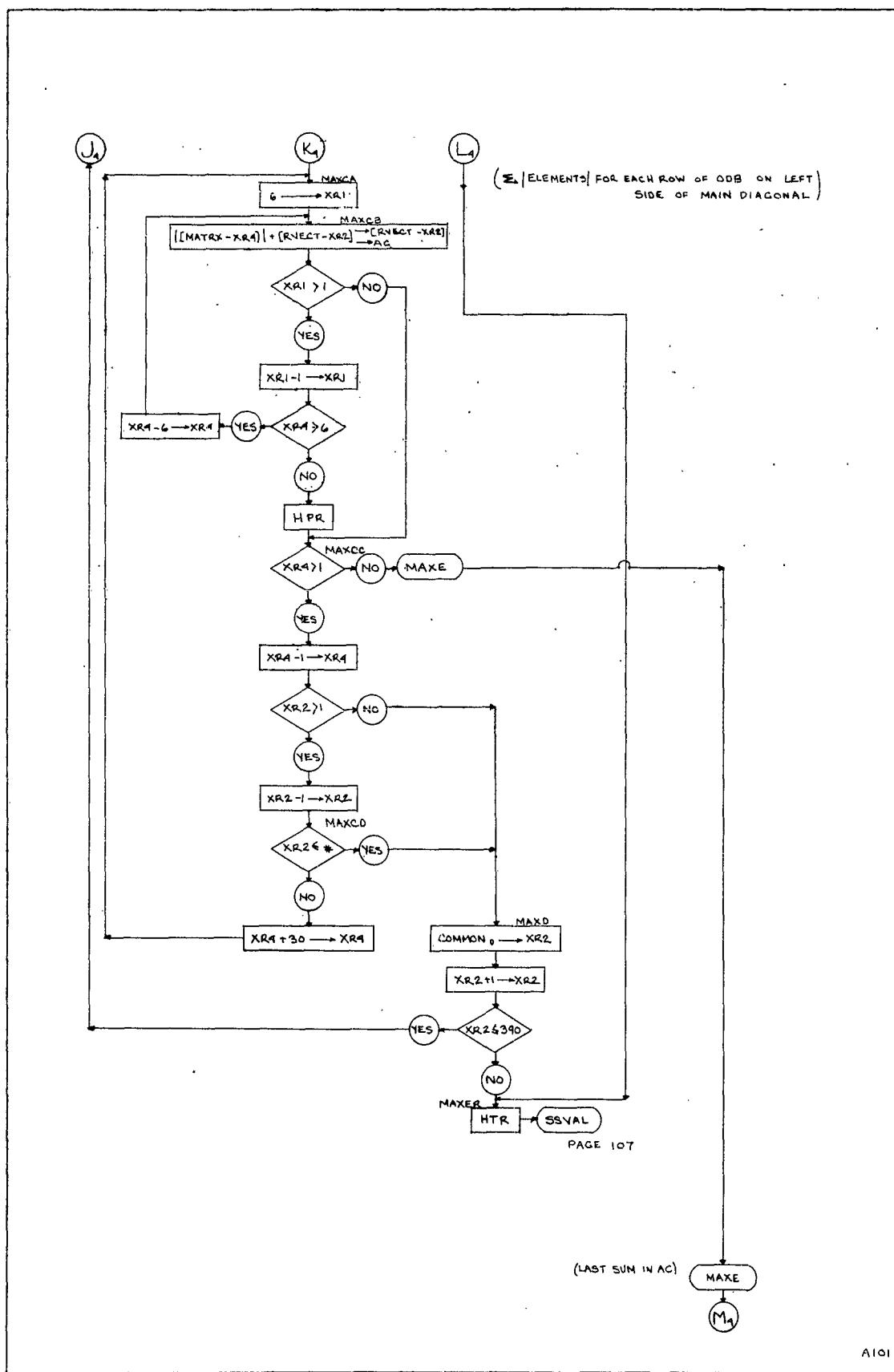
SUMMARY OF EQ 103

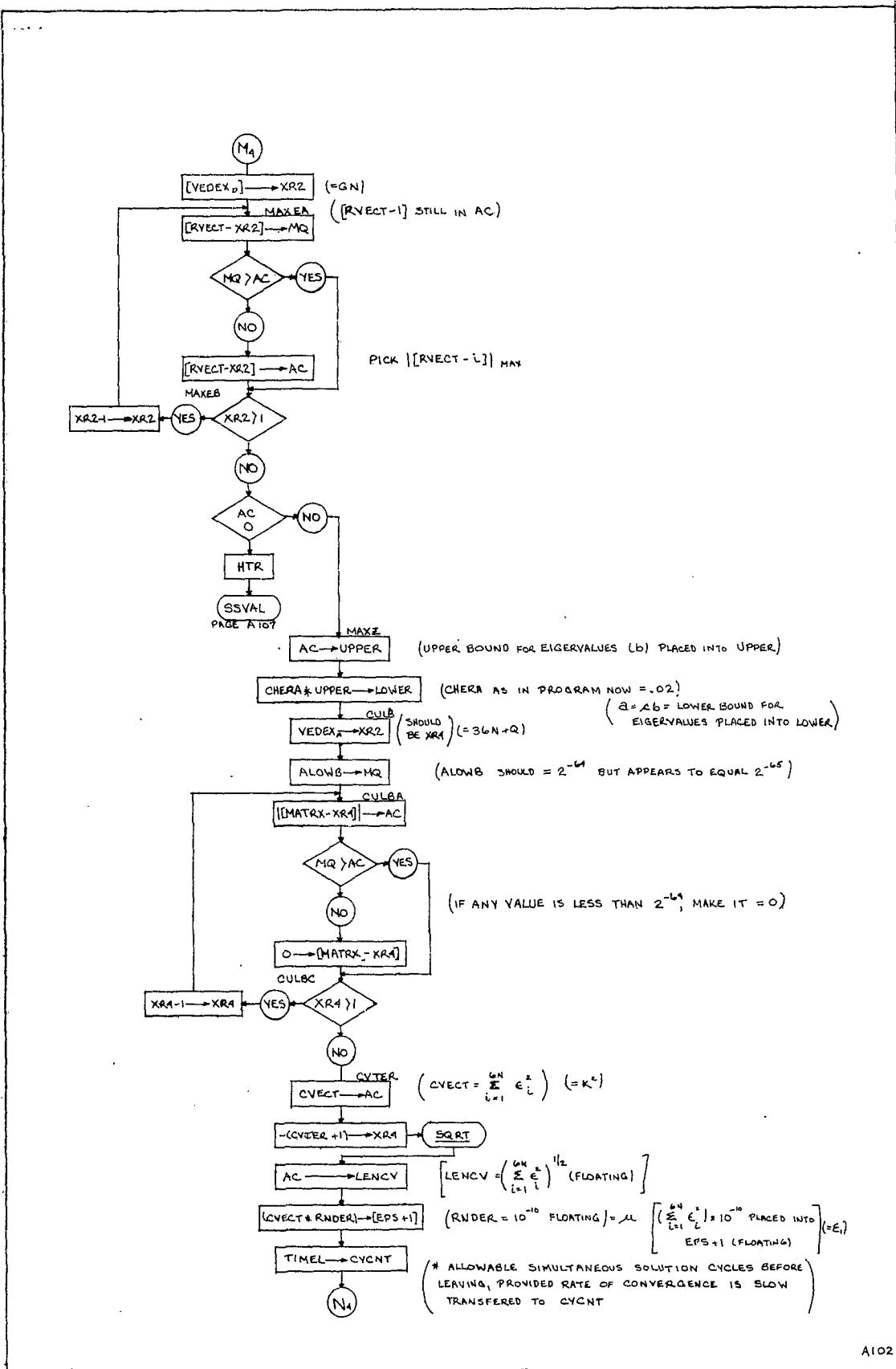
$(\partial_{11}^* G_x + \partial_1 \partial_{11}^*)$ IN	30DTIX	TRANSFERRED	CEQCF
$(\partial_{11}^* G_y - \partial_1 \partial_{11}^*)$	"	30DTIX+1	CEQCF+1
$(\partial_{11}^* G_z)$	"	30DTIX+2	CEQCF+2
$(\partial_{11}^* L_x)$	"	30DTIX+3	CEQCF+3
$(\partial_{11}^* L_y)$	"	30DTIX+4	CEQCF+4
$(\partial_{11}^* L_z + 1)$	"	30DTIX+5	CEQCF+5
$(\partial_{11}^* P_x)$	"	30DTIX+6	CEQCF+6
$(\partial_{11}^* P_y)$	"	30DTIX+7	CEQCF+7
$(\partial_{11}^* P_z)$	"	30DTIX+8	CEQCF+8
$(-\partial_{11}^* L_x)$	"	30DTIX+9	CEQCF+9
$(-\partial_{11}^* L_y)$	"	30DTIX+10	CEQCF+10
$(-\partial_{11}^* L_z)$	"	30DTIX+11	CEQCF+11
$(-\partial_{11}^* G_x^2 + \partial_1^2 \partial_{11}^2)$	"	30DTIX+12	CEQCF+12
$(-\partial_{11}^* G_y^2 + \partial_1^2 \partial_{11}^2)$	"	30DTIX+13	CEQCF+13
$(-\partial_{11}^* G_z^2 + \partial_1^2 \partial_{11}^2)$	"	30DTIX+14	CEQCF+14
$(-\partial_{11}^* G_x^2 + \partial_1^2 \partial_{11}^2)$	"	30DTIX+15	CEQCF+15
$(-\partial_{11}^* G_y^2 + \partial_1^2 \partial_{11}^2)$	"	30DTIX+16	CEQCF+16
$(-\partial_{11}^* G_z^2 + \partial_1^2 \partial_{11}^2)$	"	30DTIX+17	CEQCF+17
$(-\partial_{11}^* P_x)$	"	30DTIX+18	CEQCF+18
$(-\partial_{11}^* P_y)$	"	30DTIX+19	CEQCF+19
$(-\partial_{11}^* P_z)$	"	30DTIX+20	CEQCF+20
$(\partial_{11}^* L_x^2)$	"	30DTIX+21	CEQCF+21
$(\partial_{11}^* L_y^2)$	"	30DTIX+22	CEQCF+22
$(\partial_{11}^* L_z^2)$	"	30DTIX+23	CEQCF+23
$[(R_{11}^* + \partial_1^* \partial_{11}^*) - (R_{11} + \partial_1 \partial_{11})]$ IN	30DTIX+24	CEQCF+24	

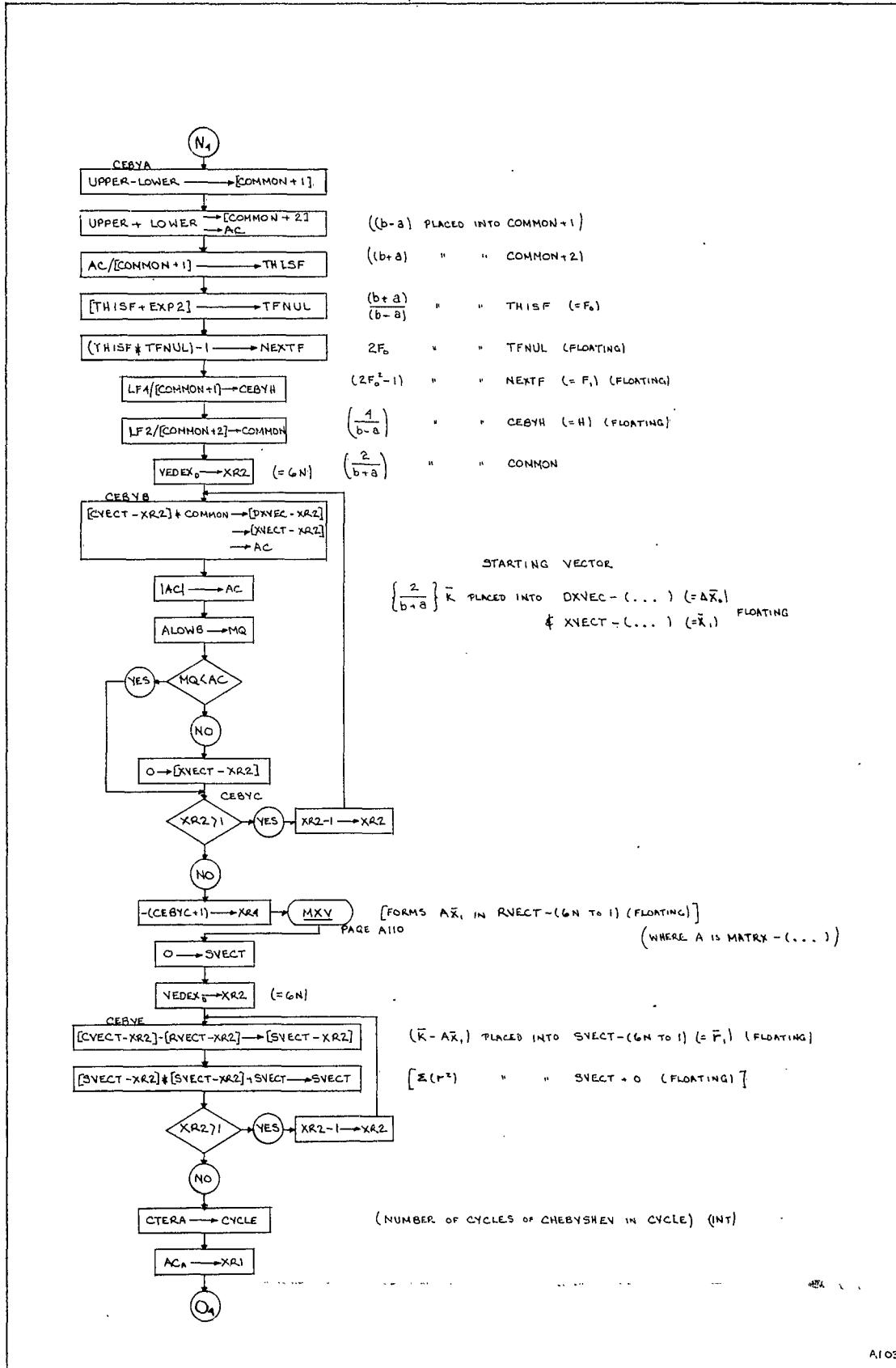


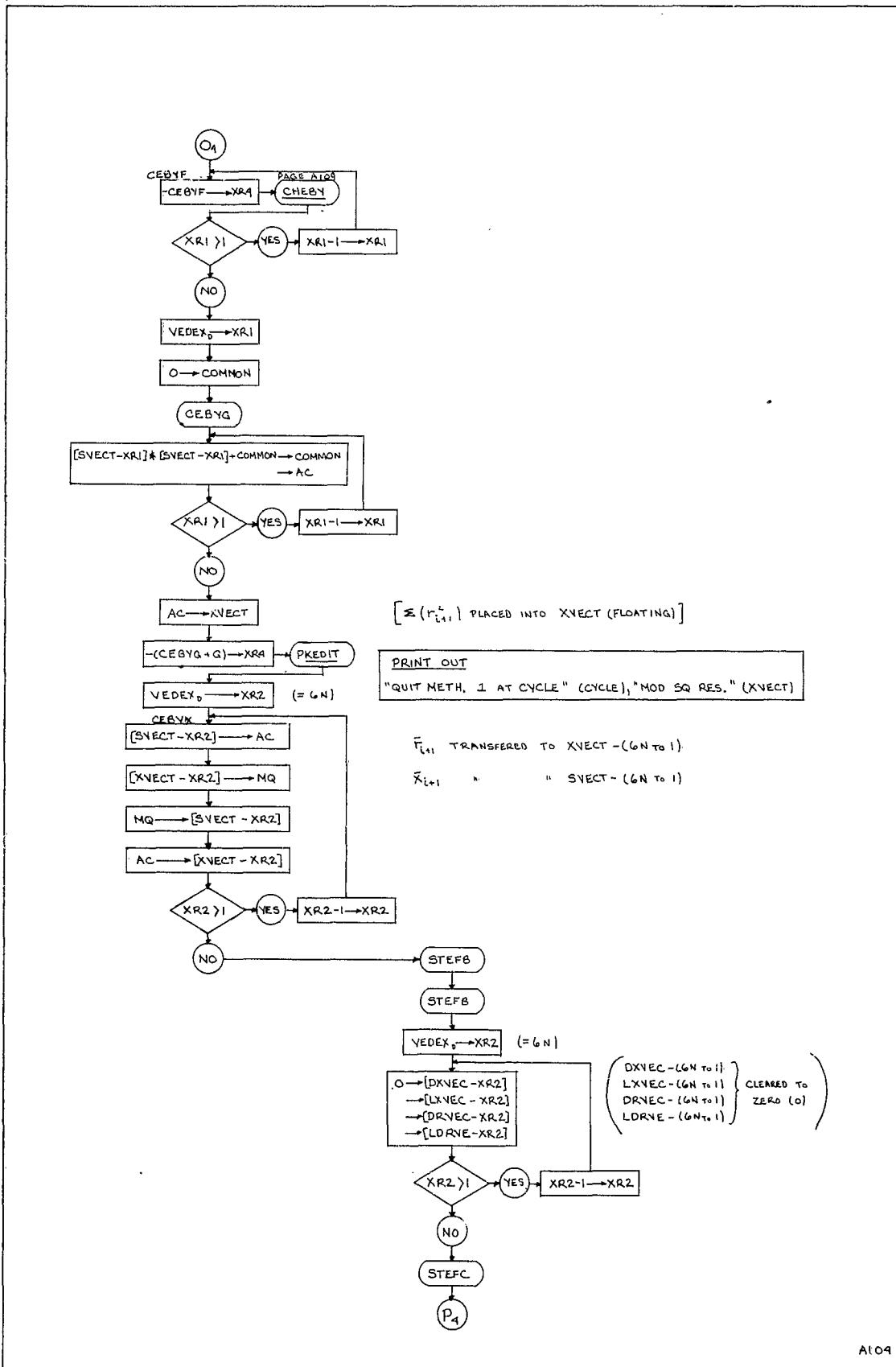


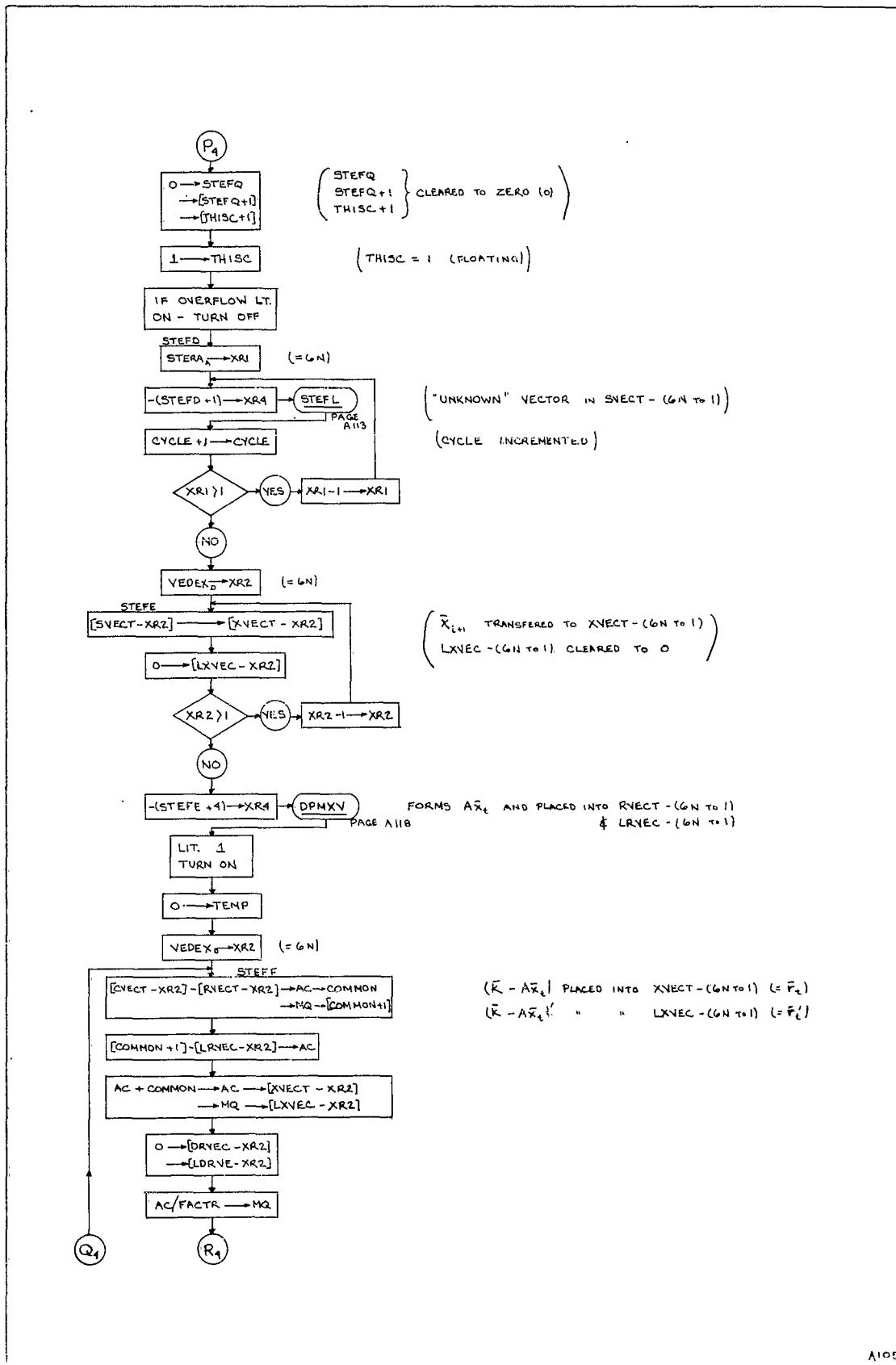


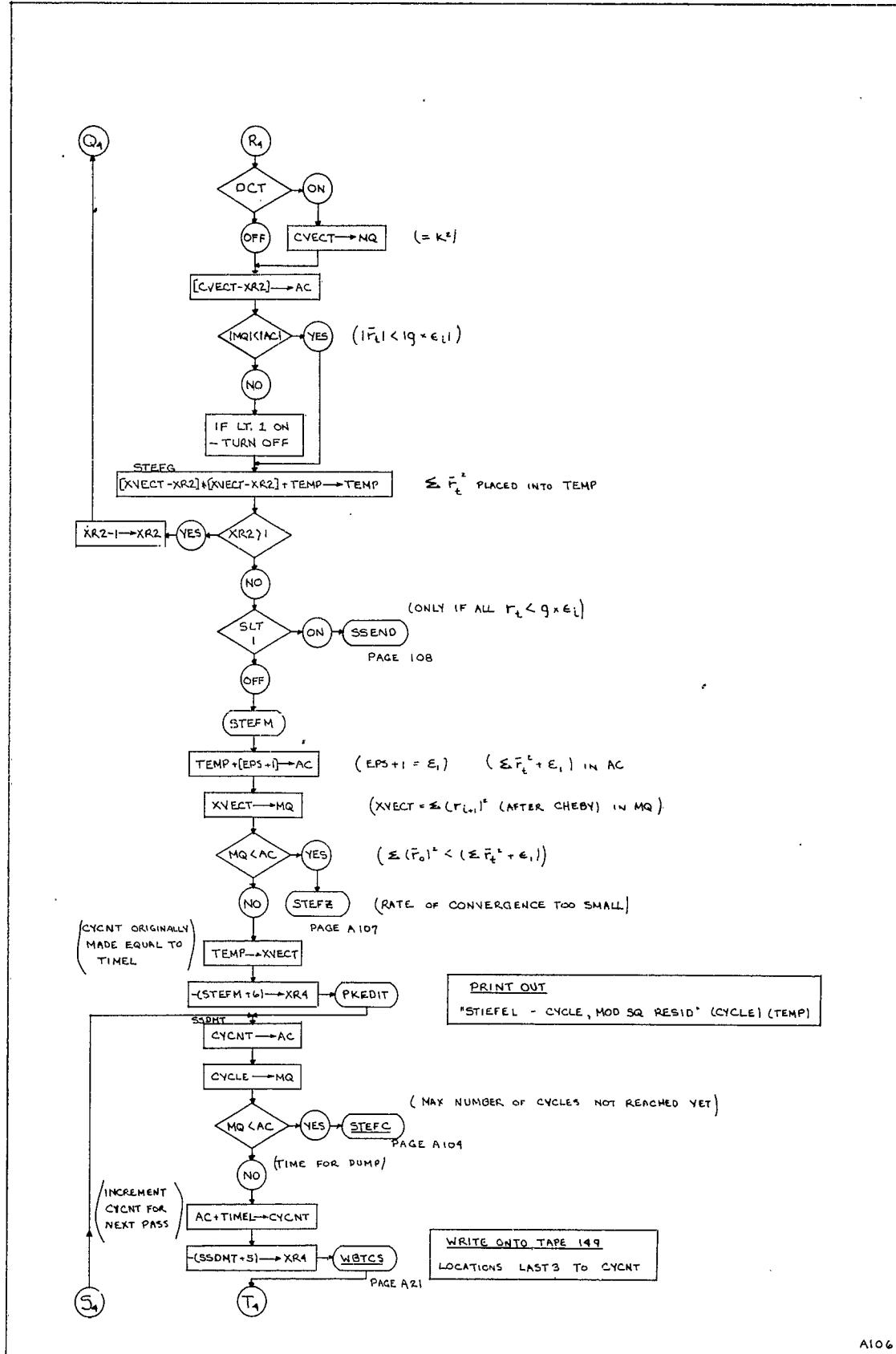


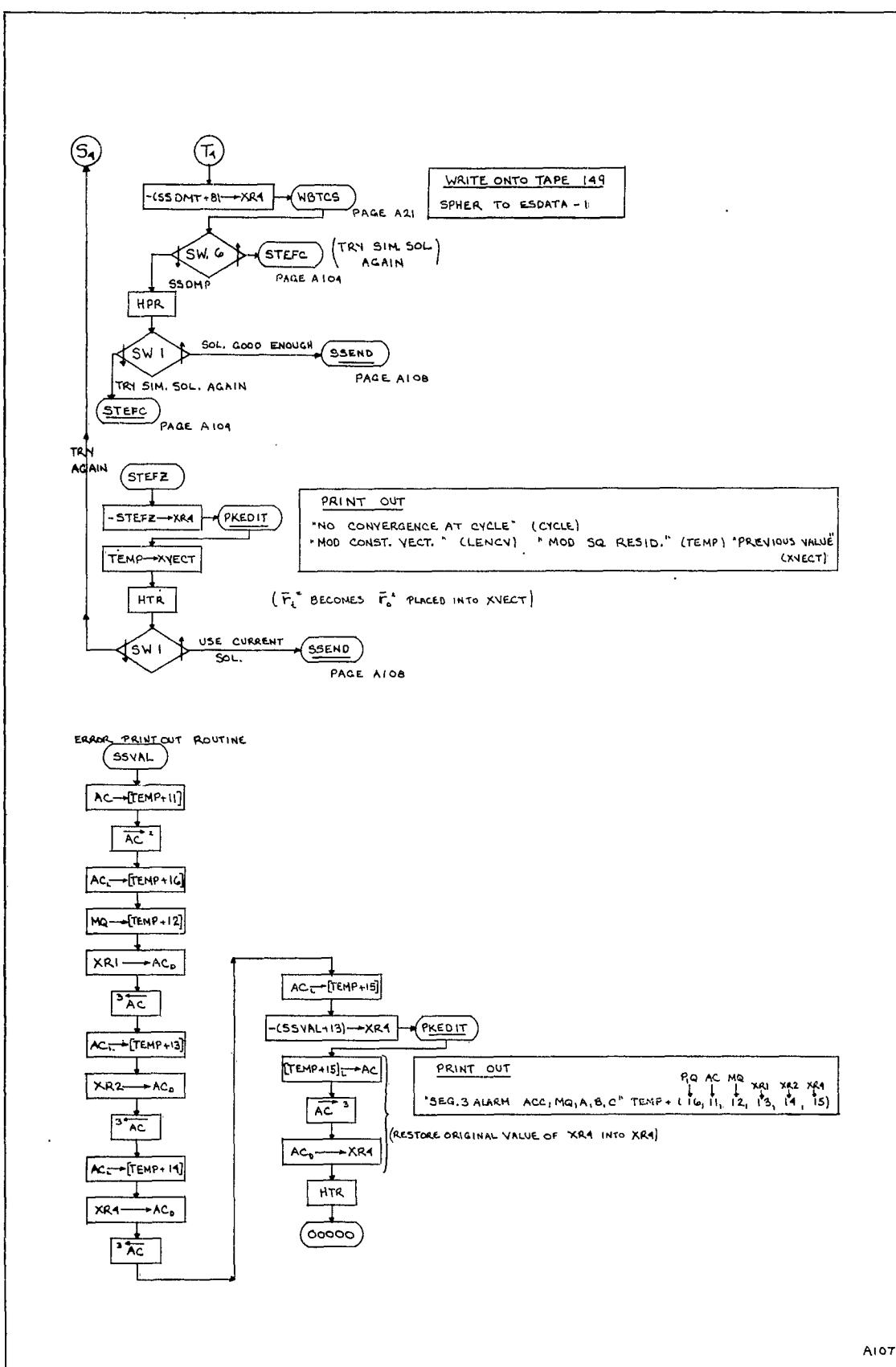


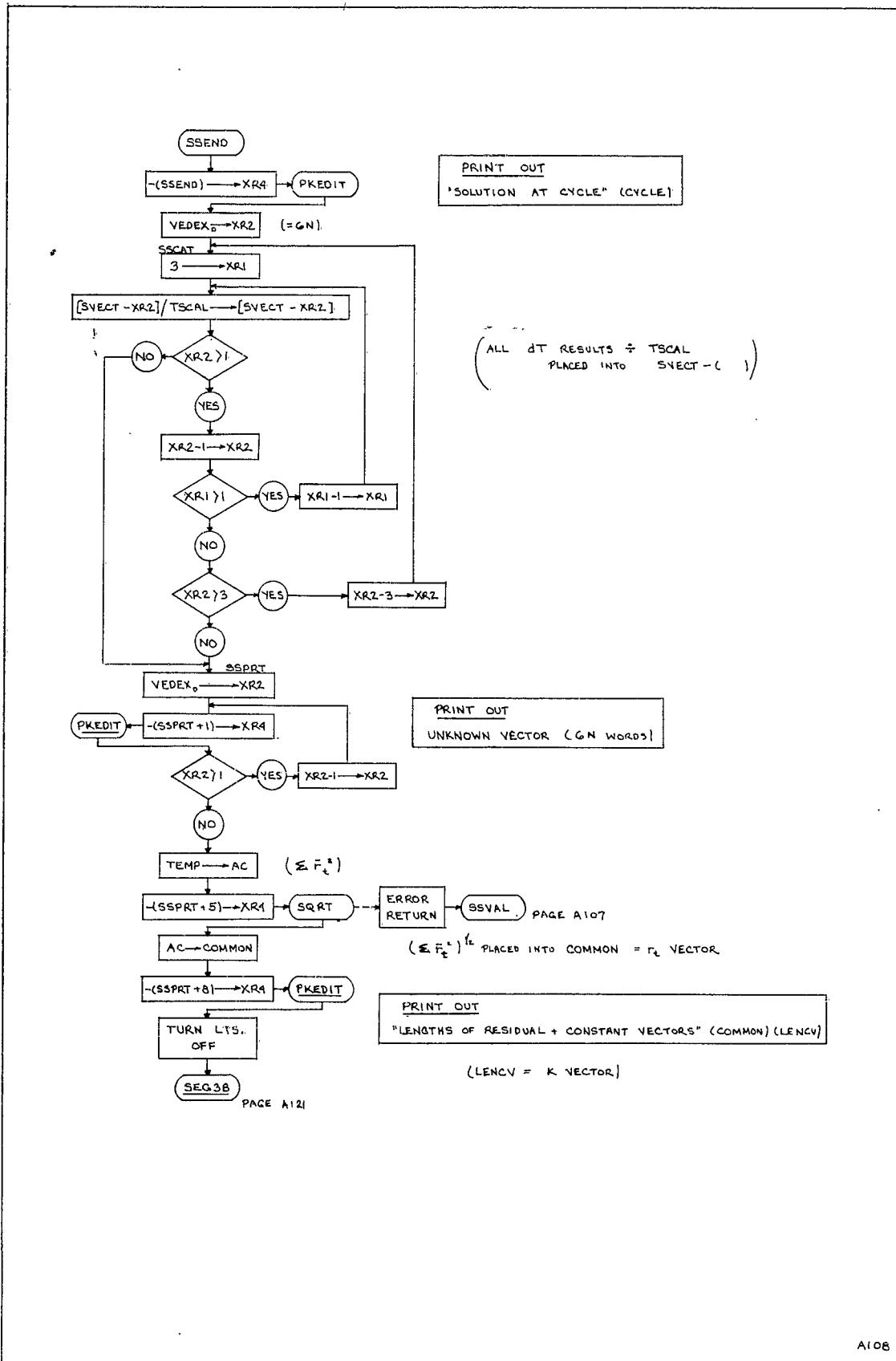


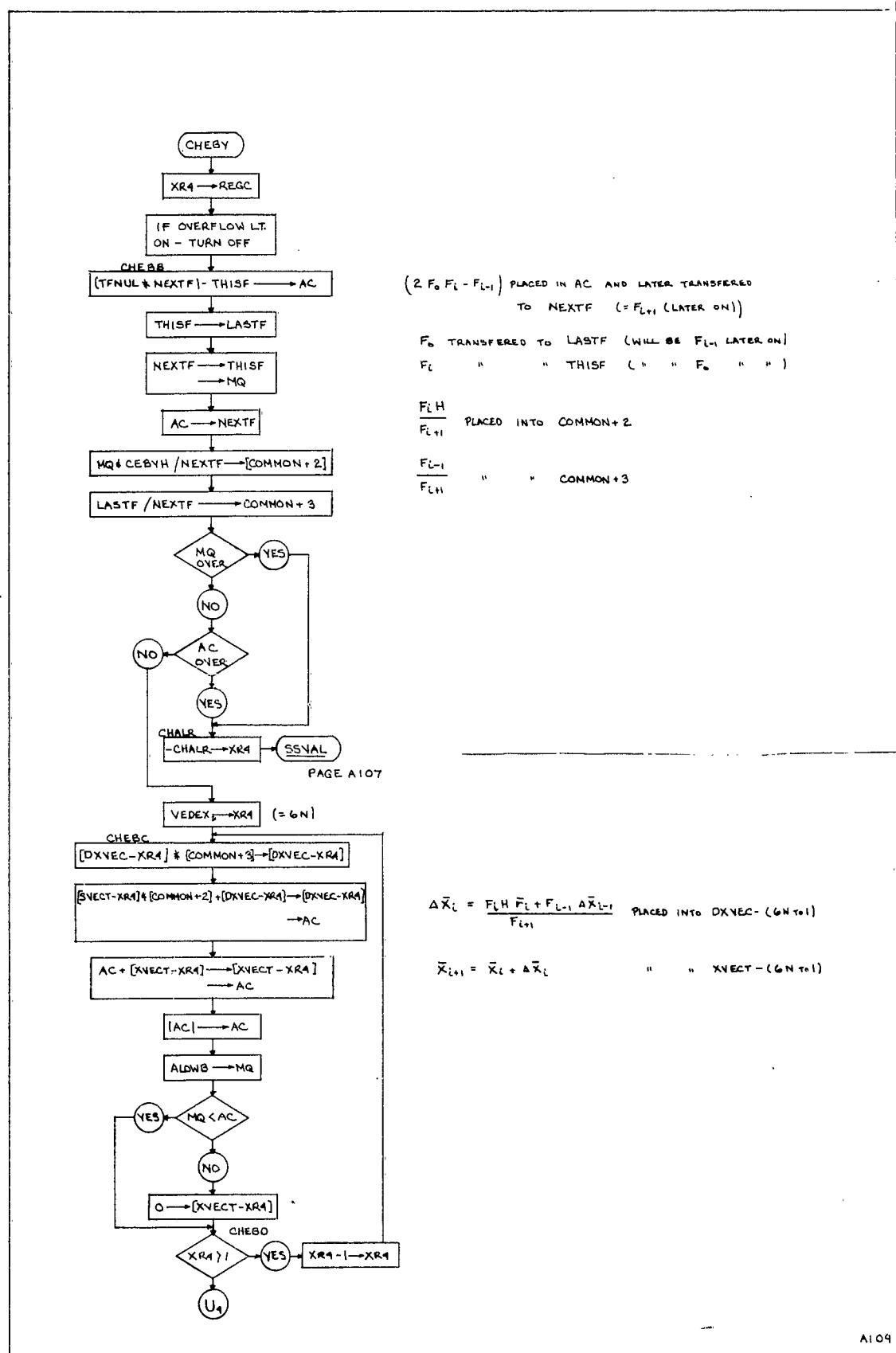


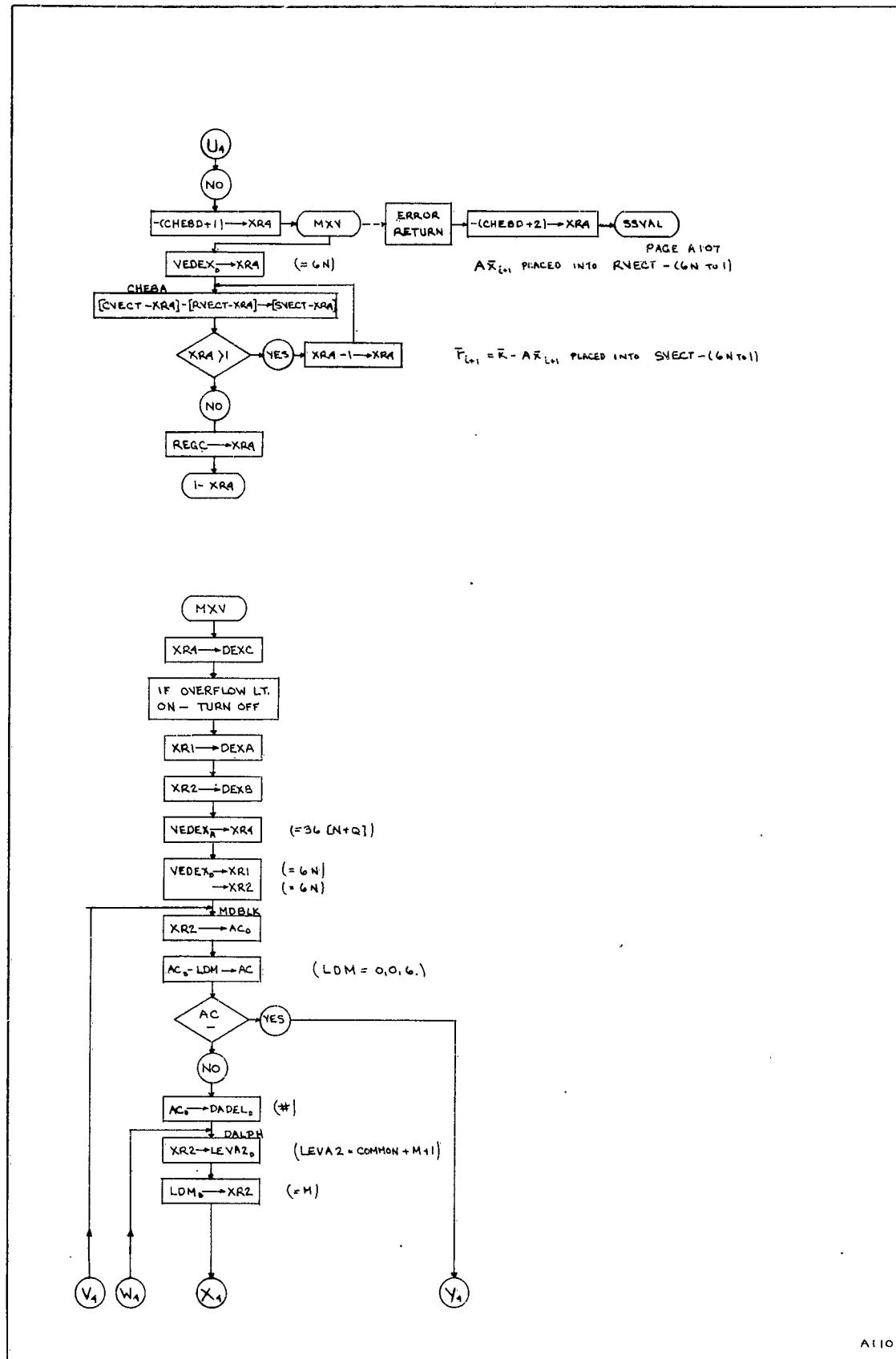


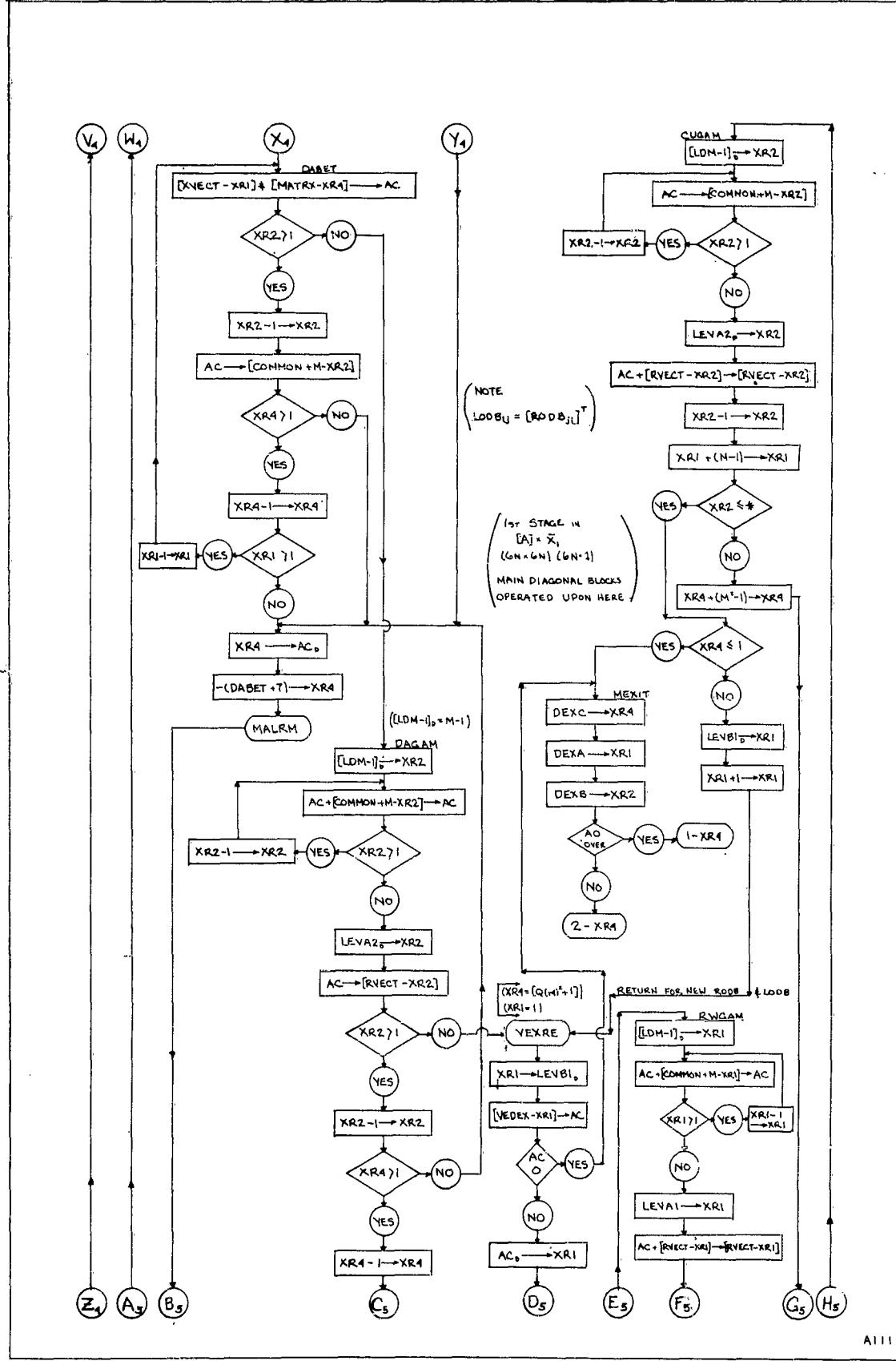


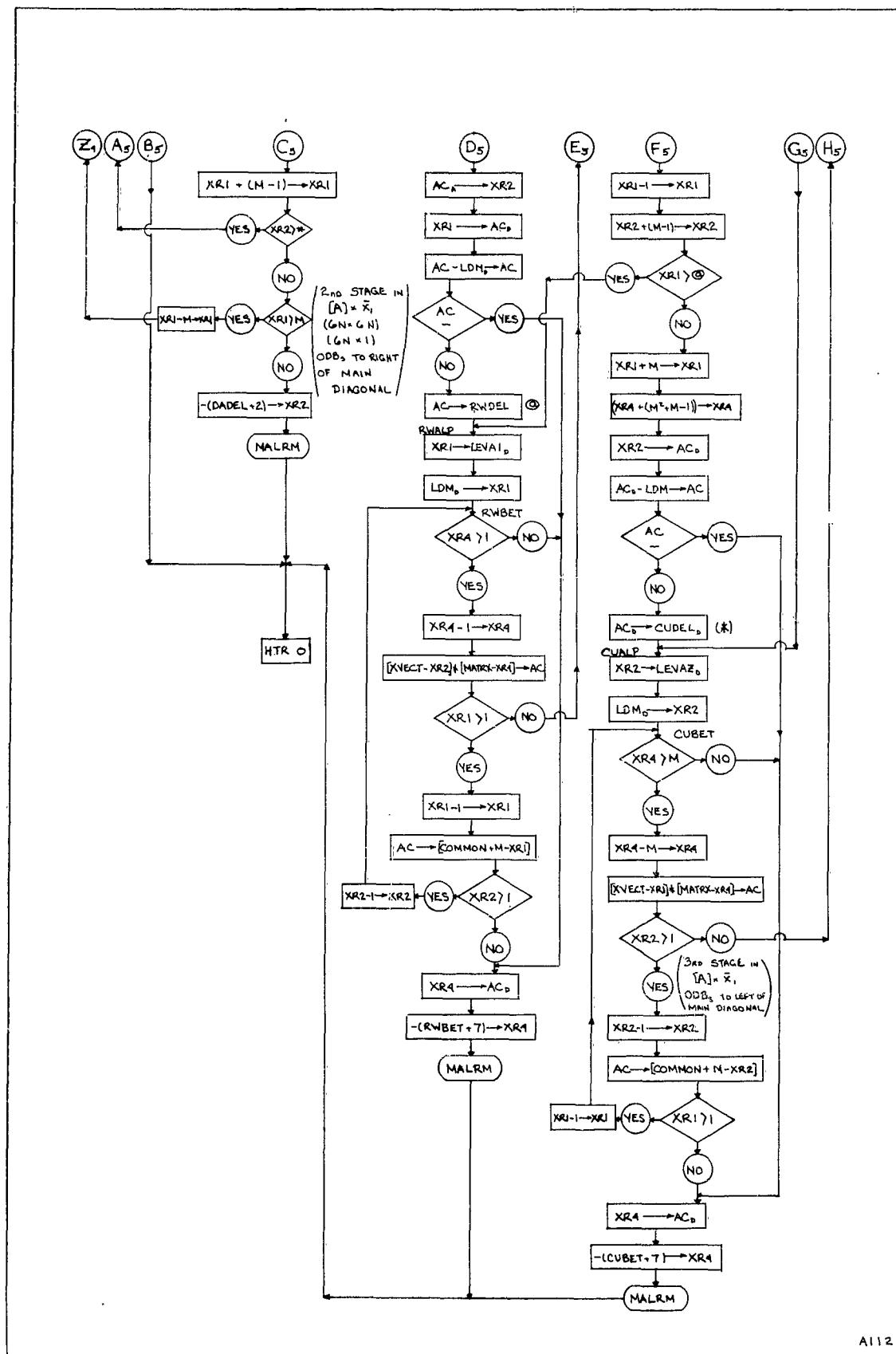


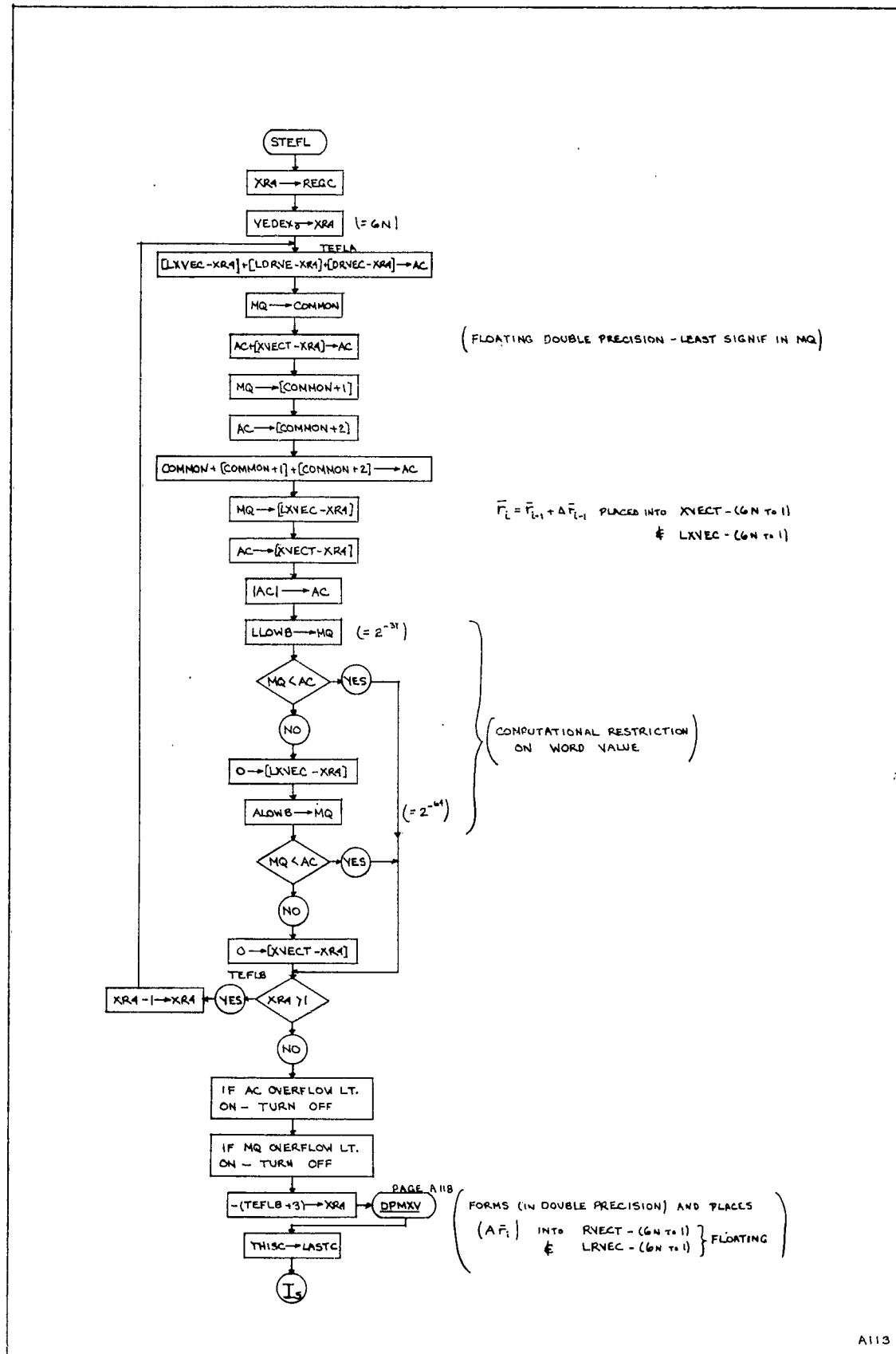


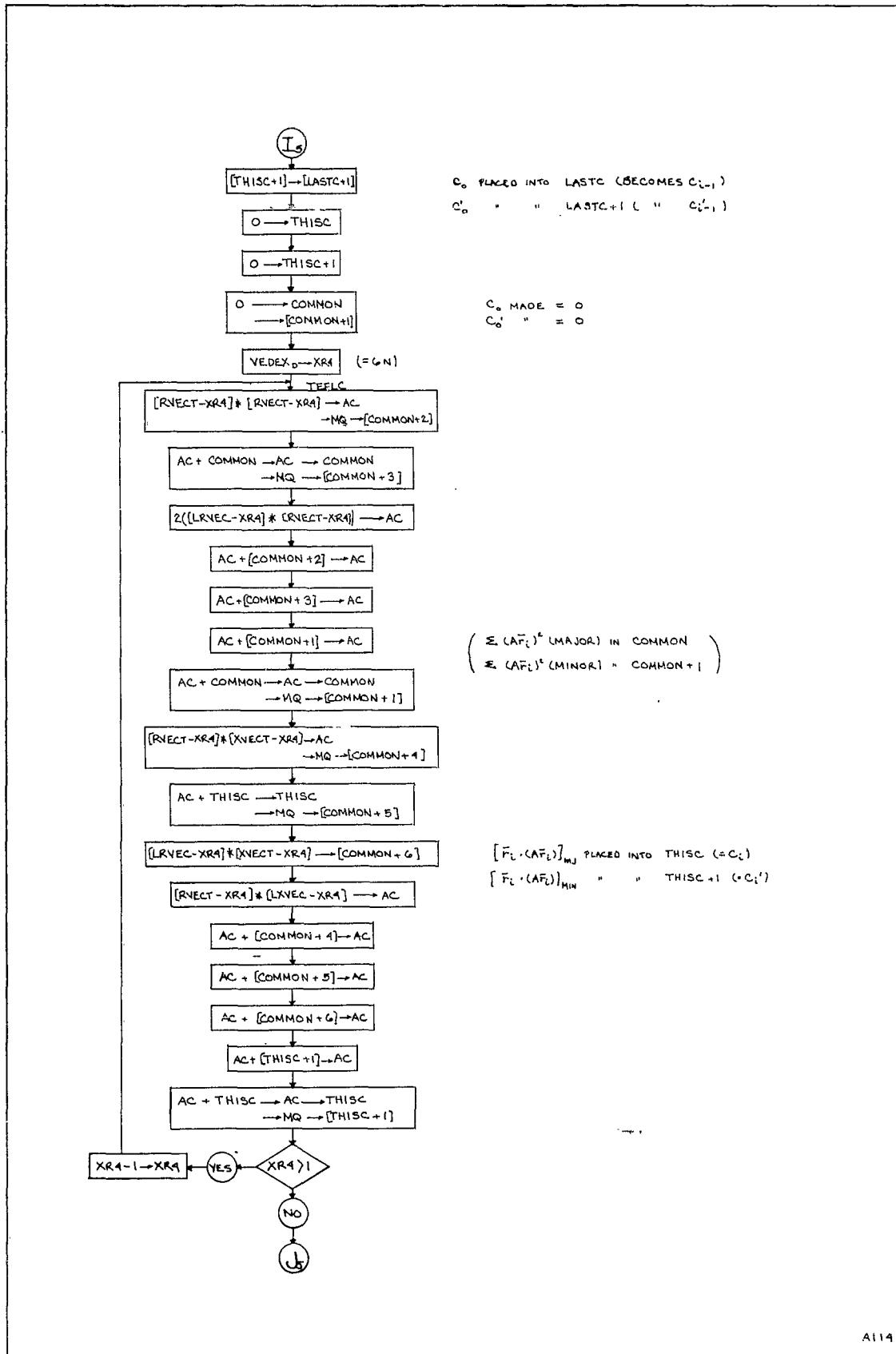


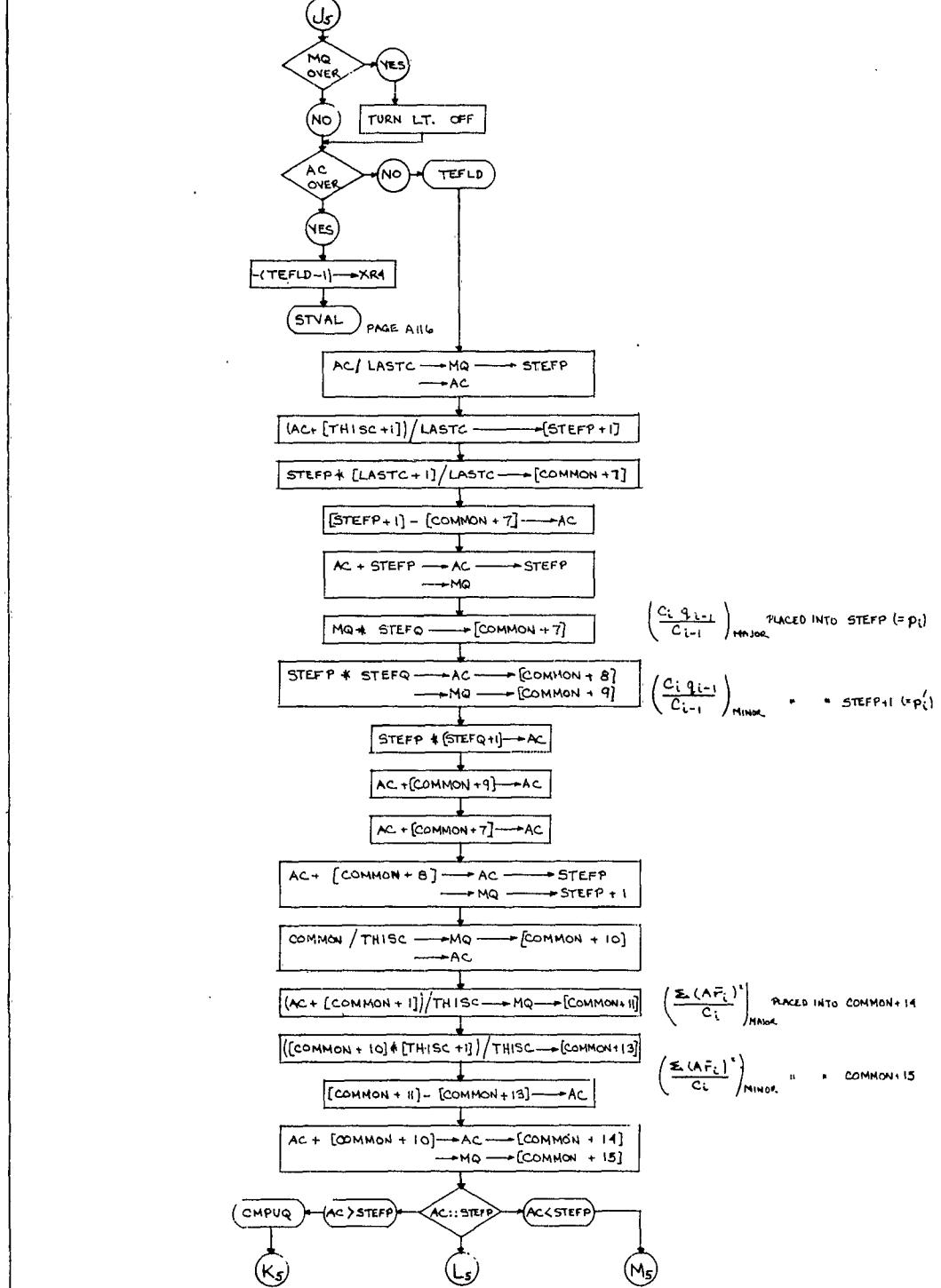


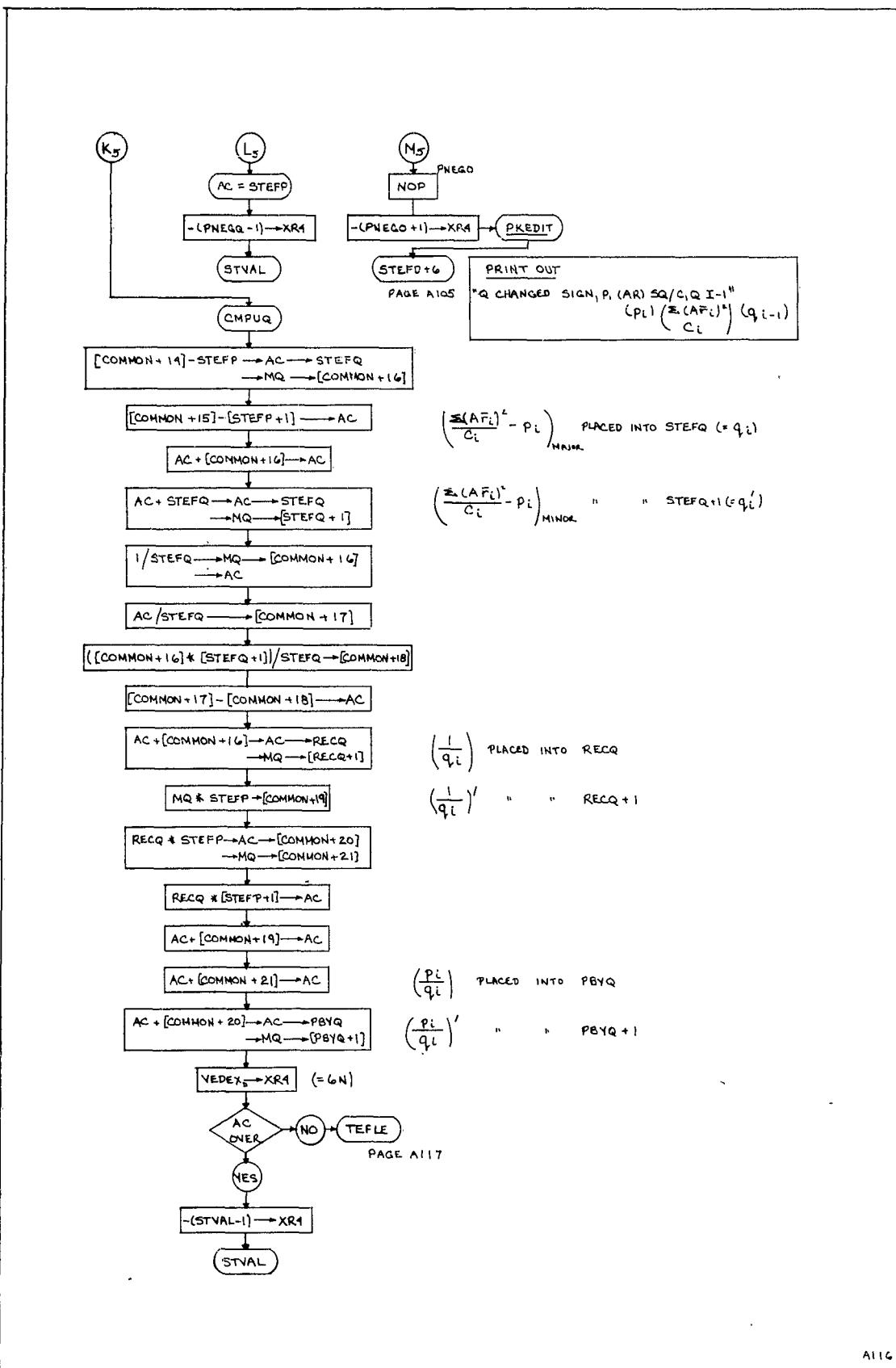


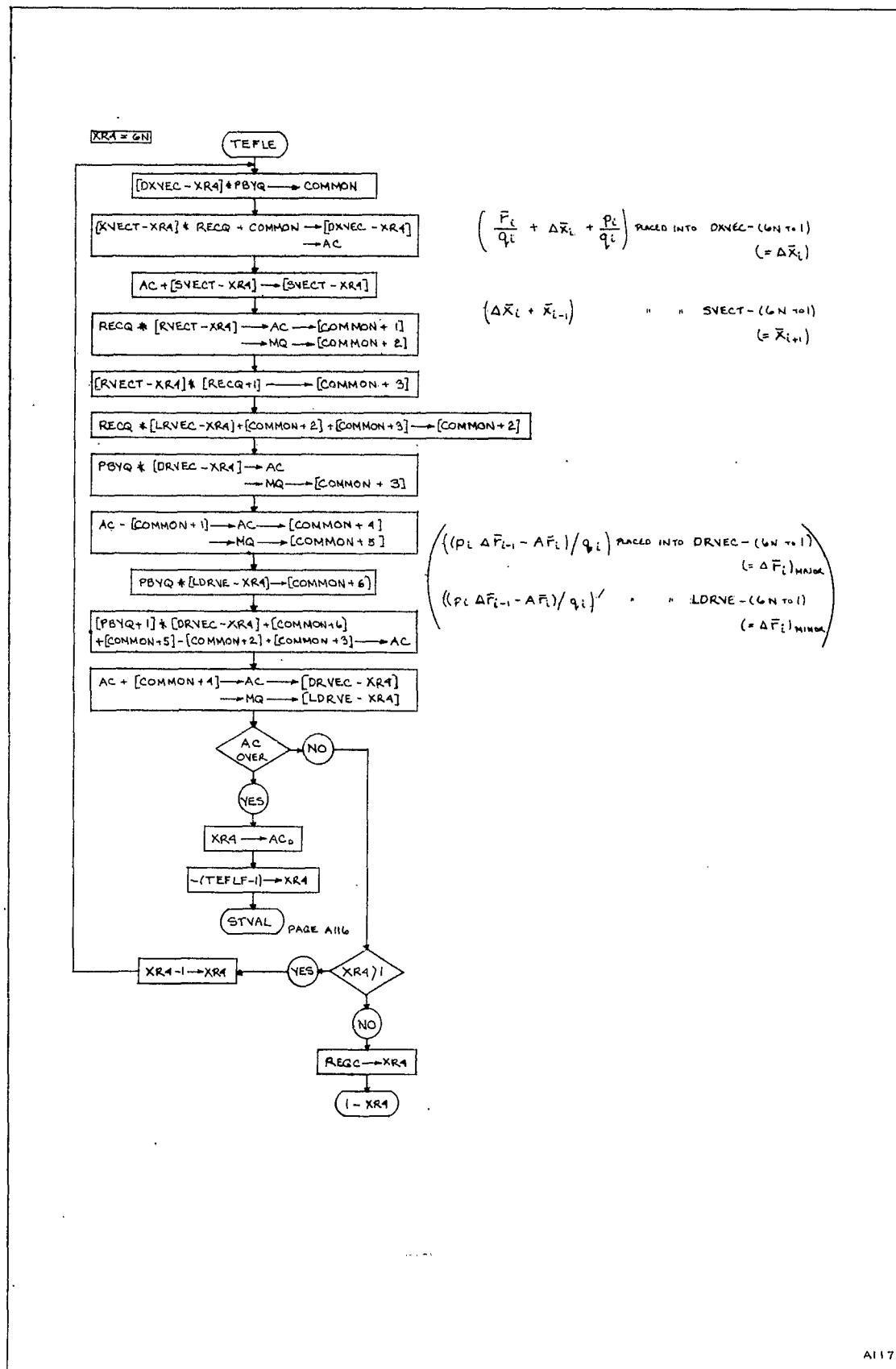


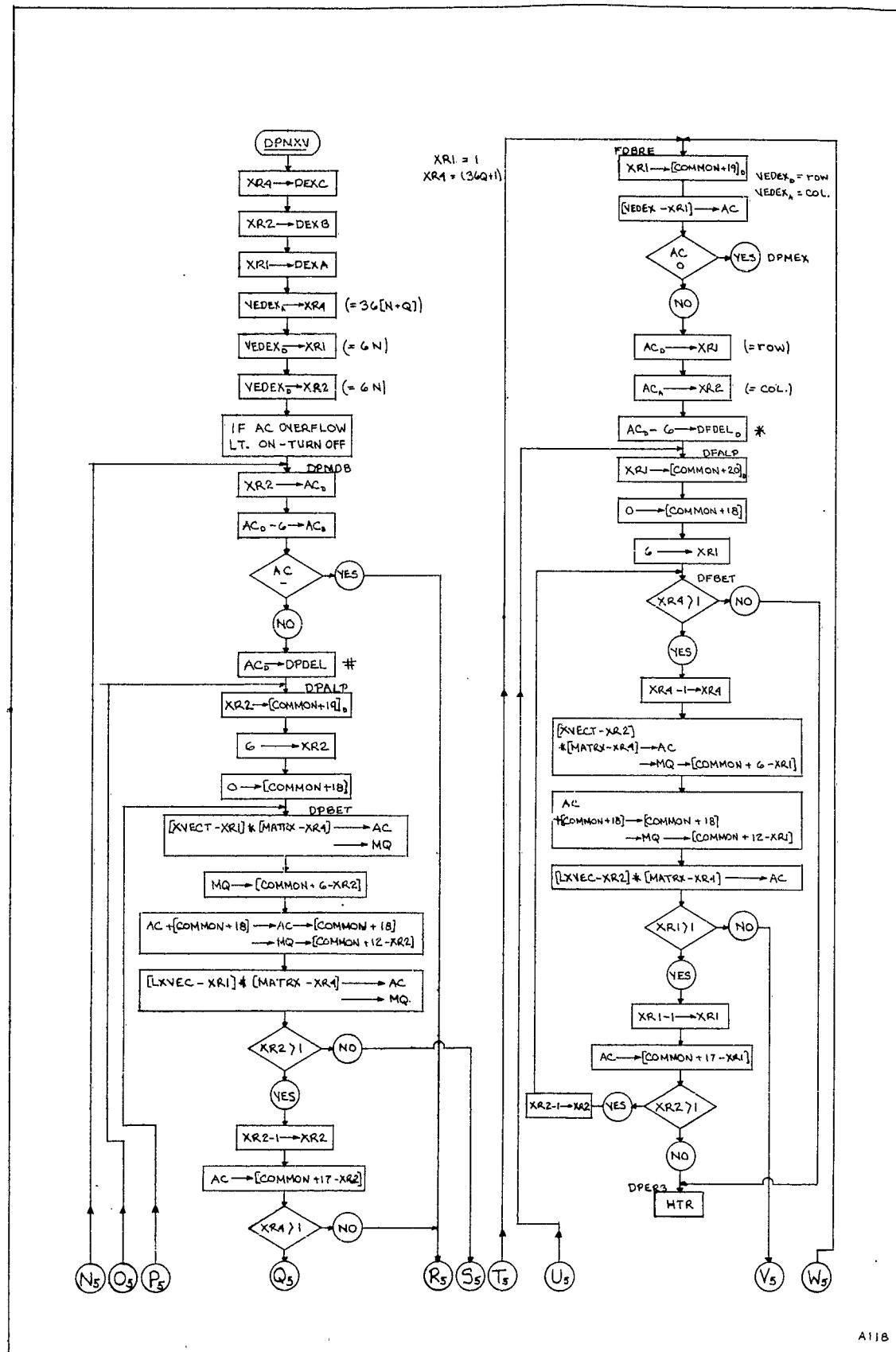


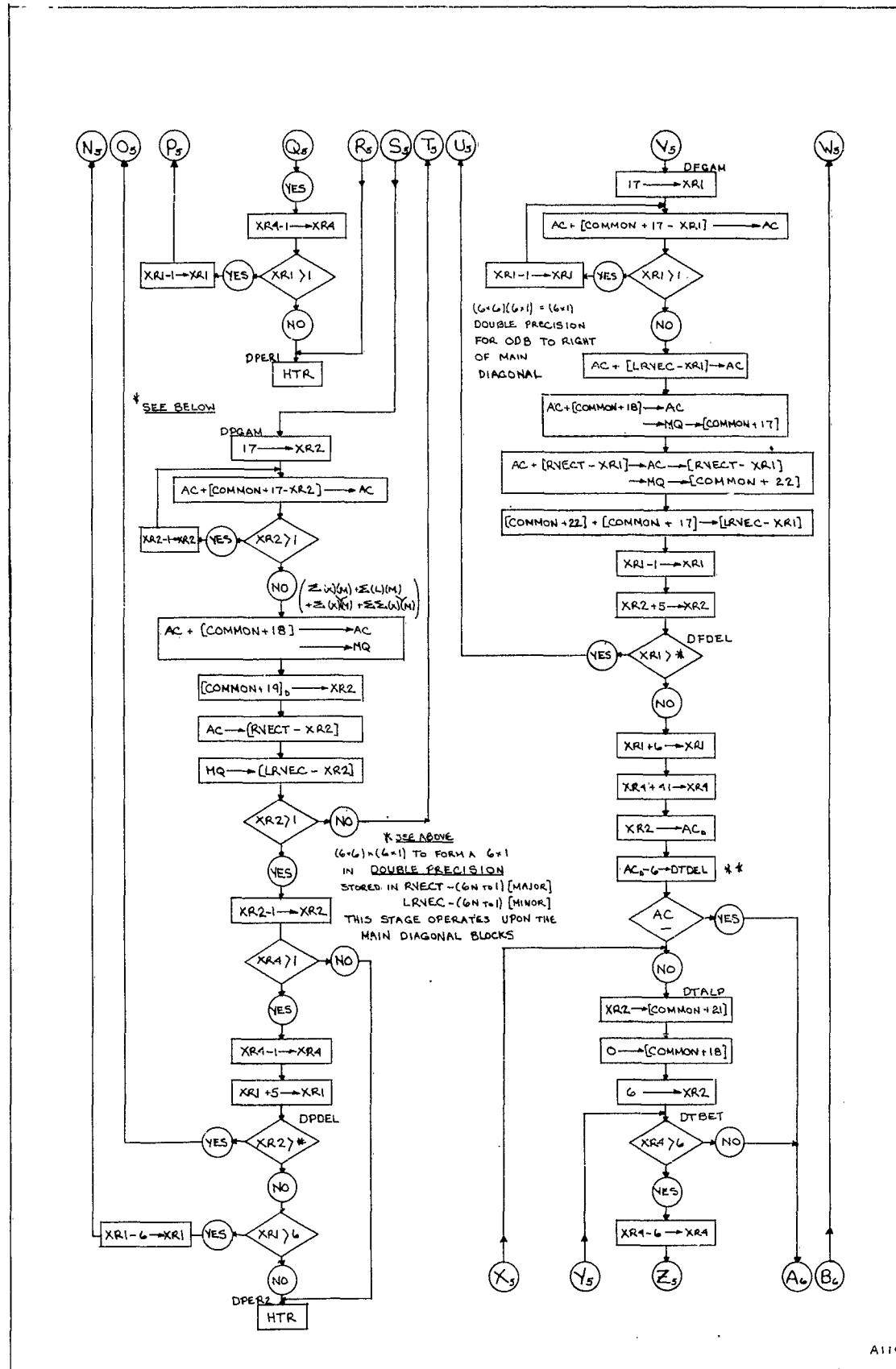


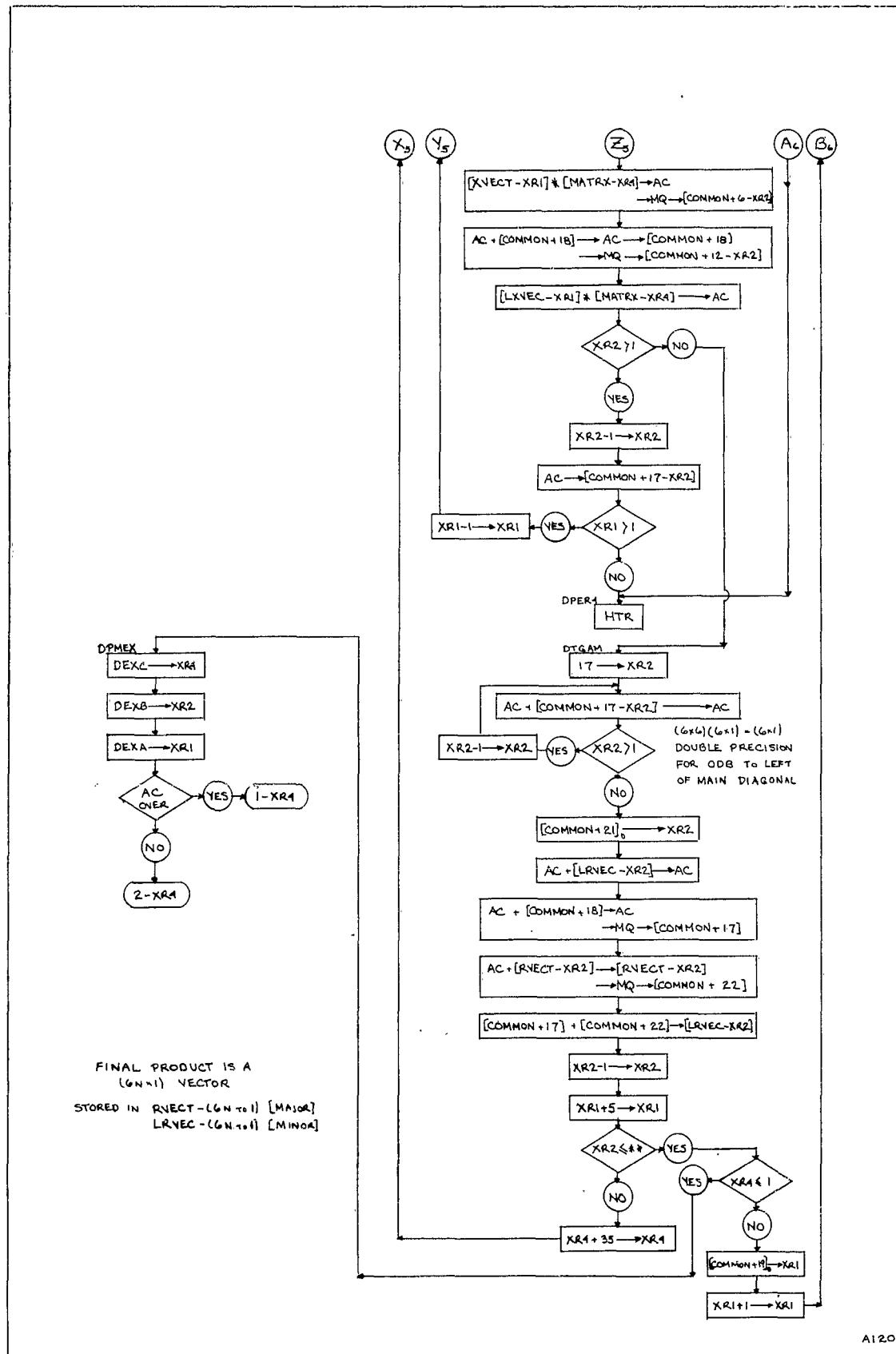


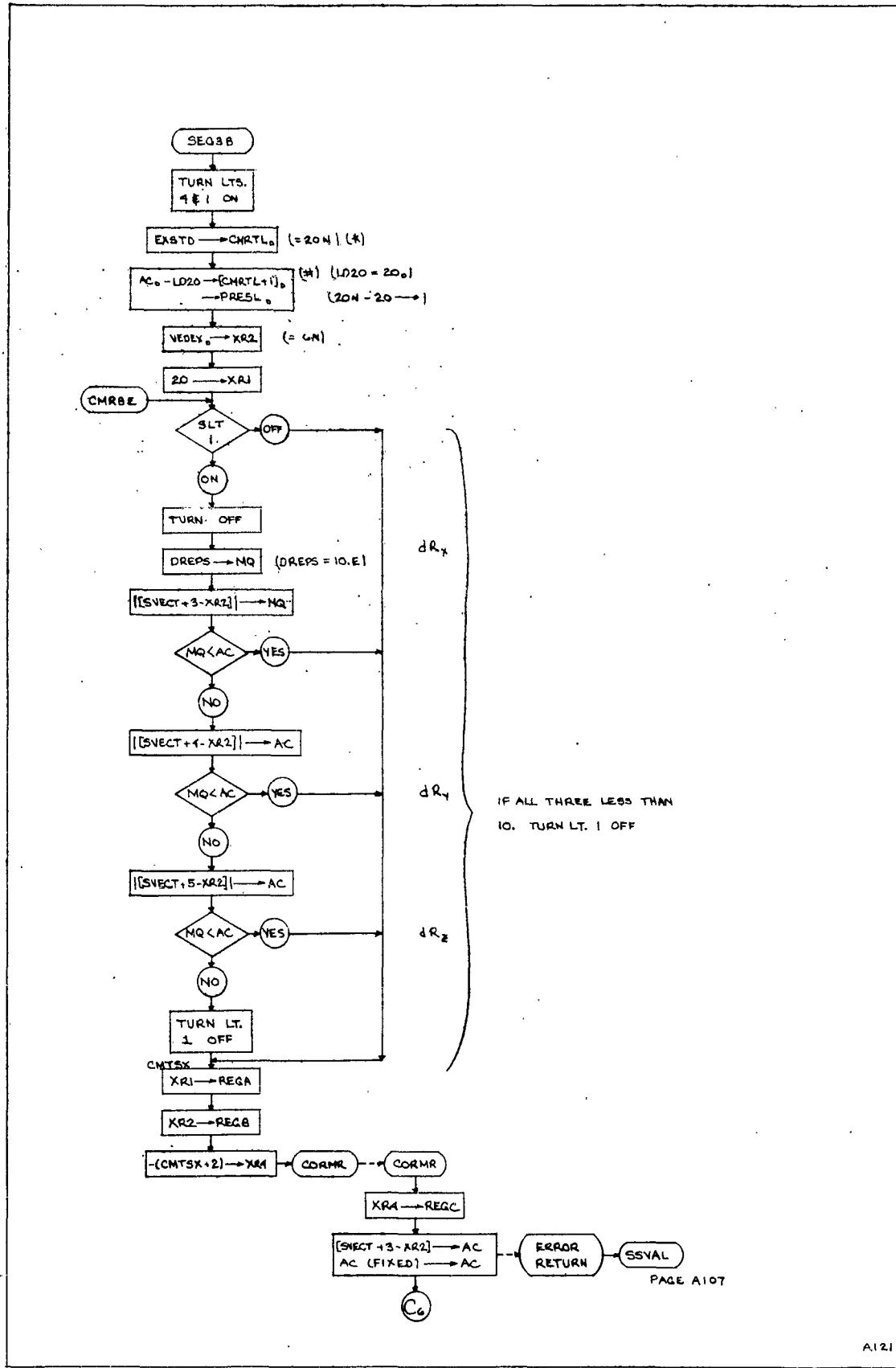


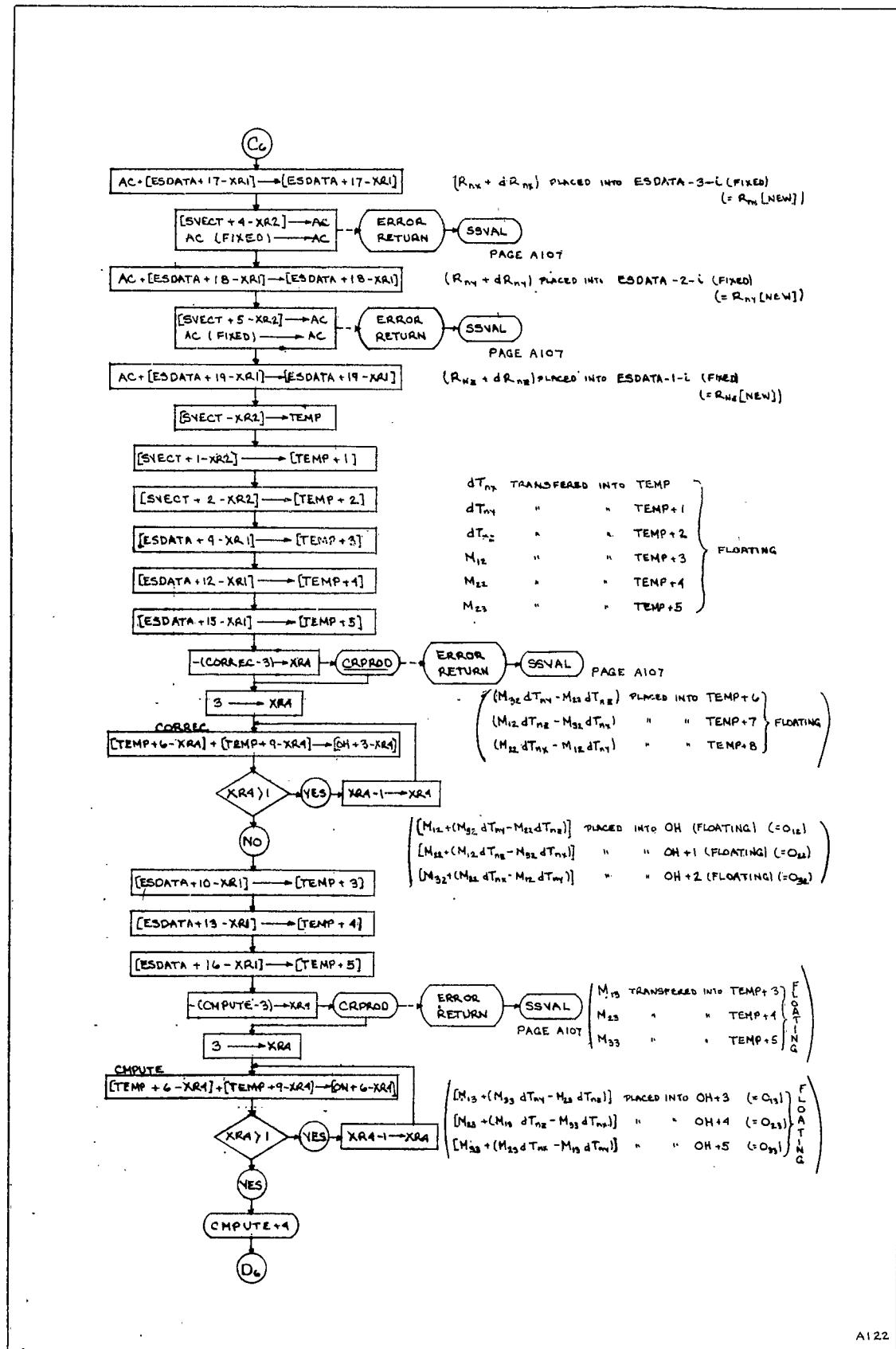


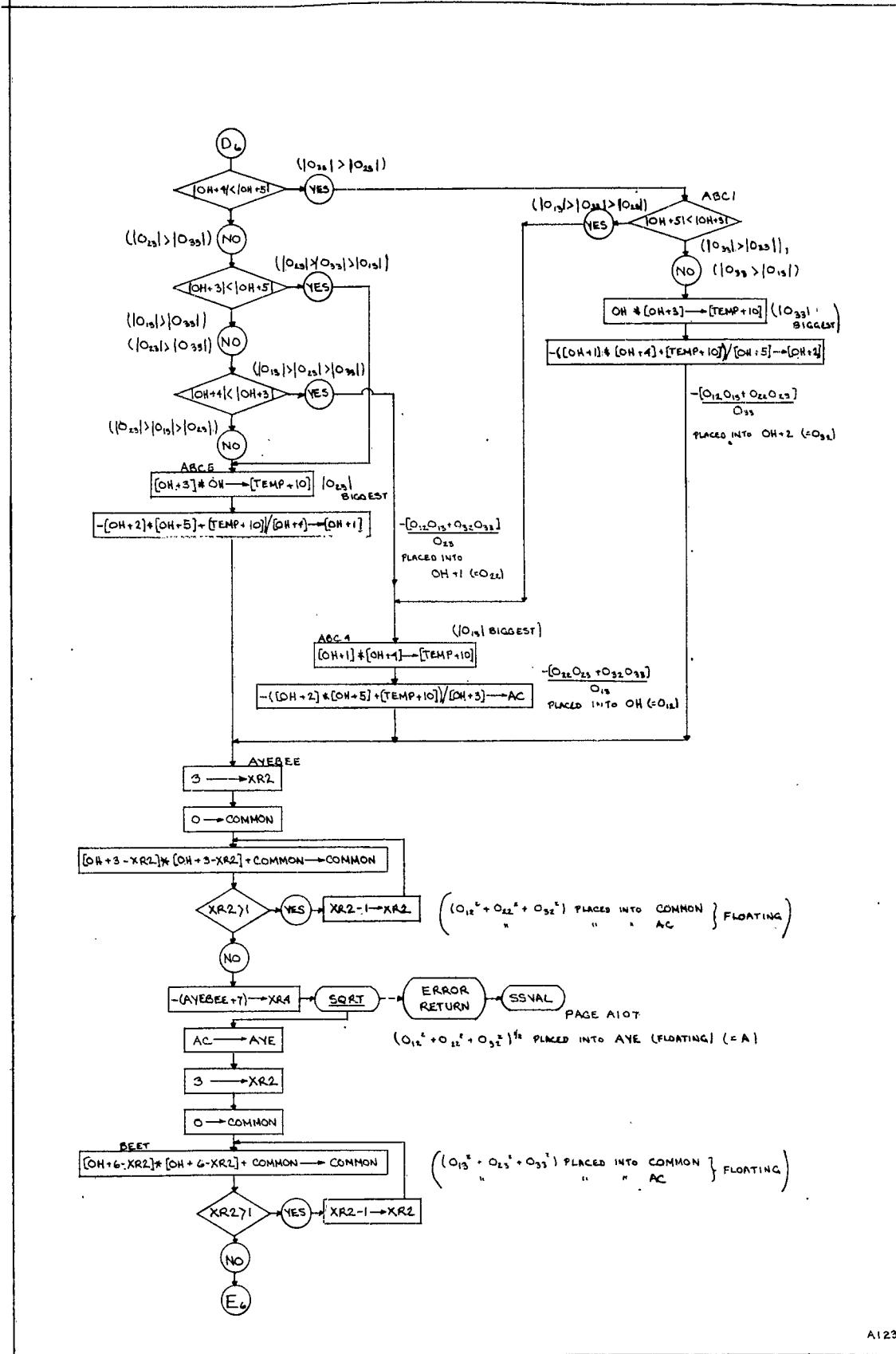


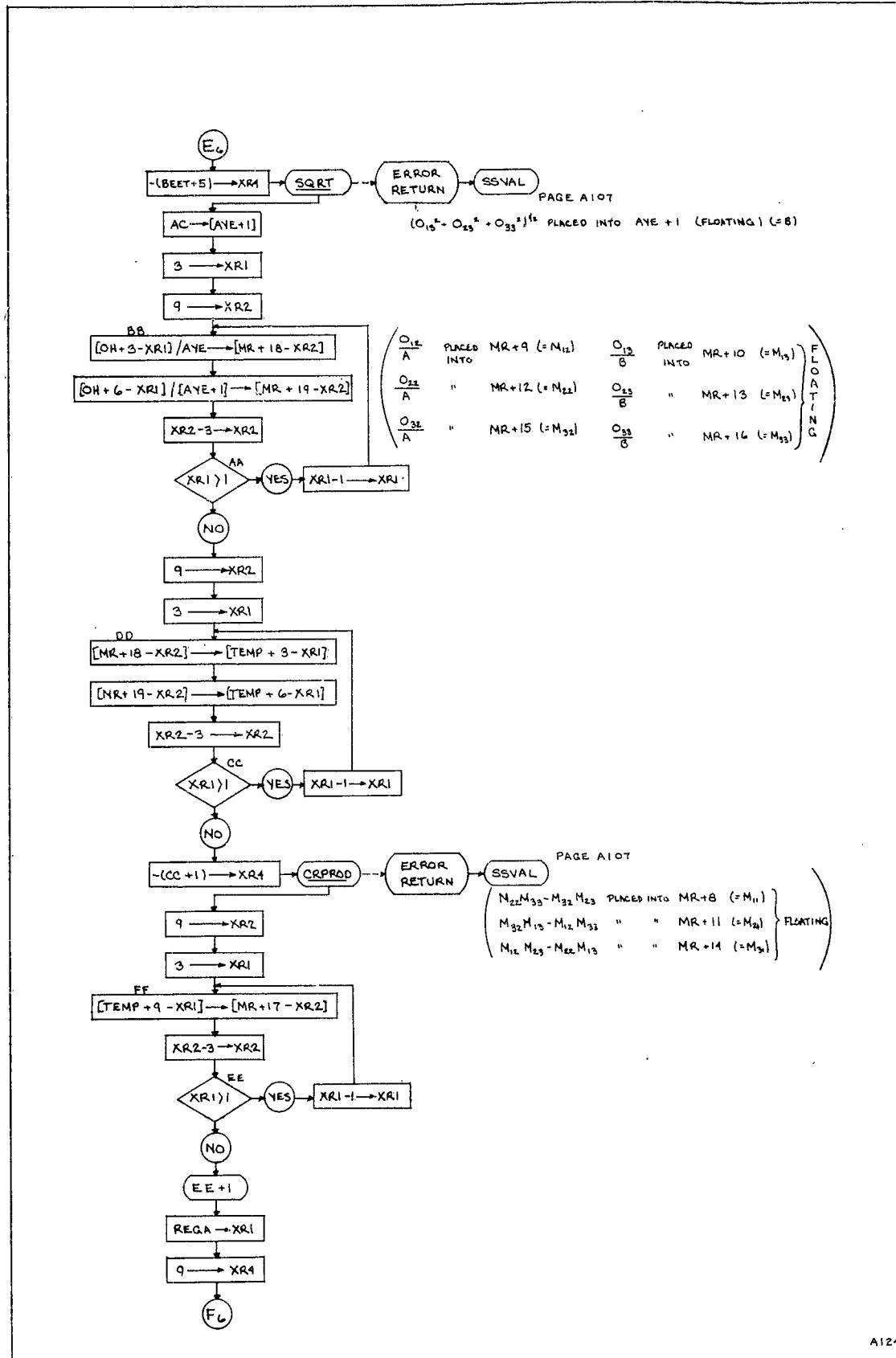


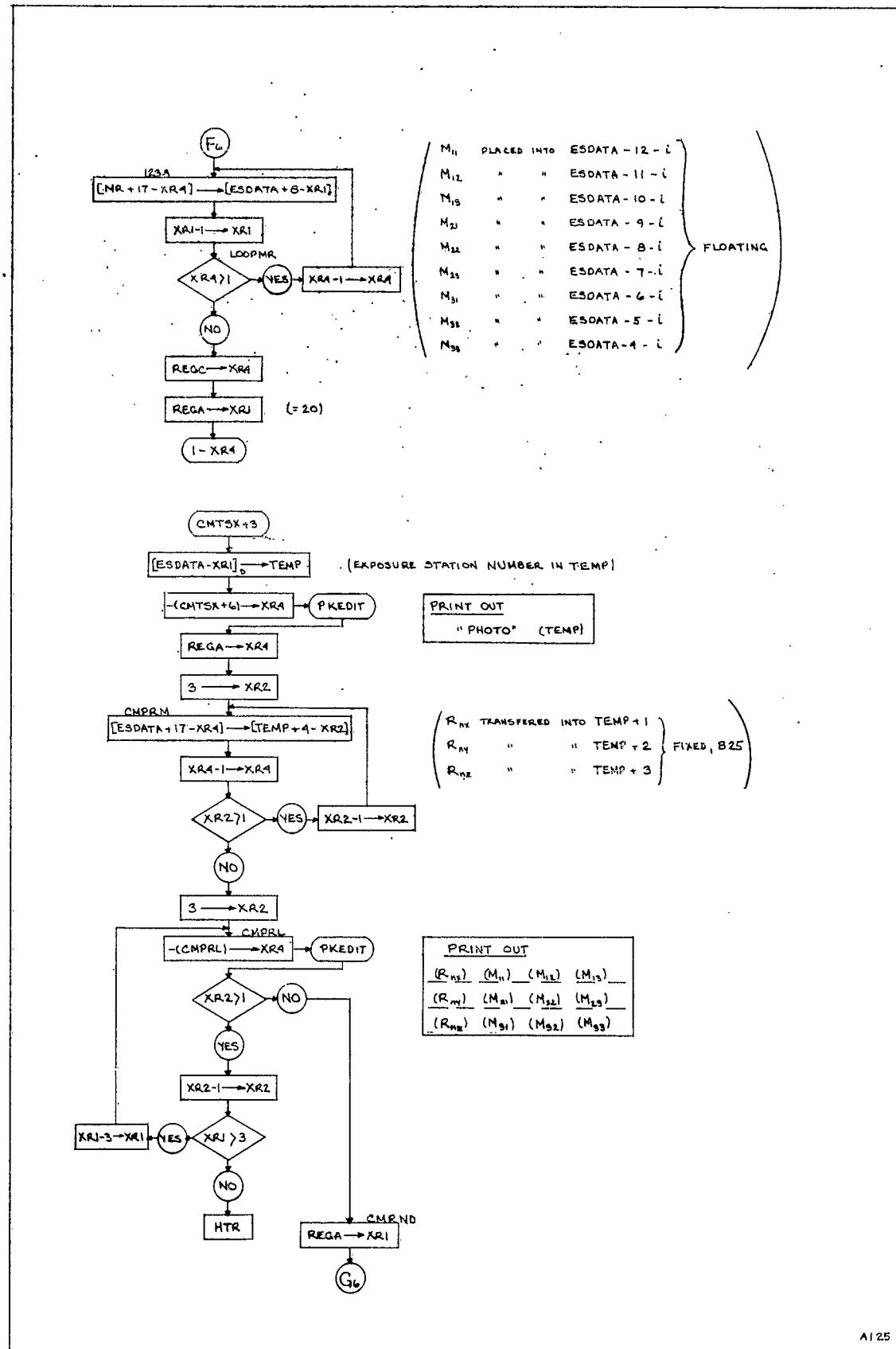


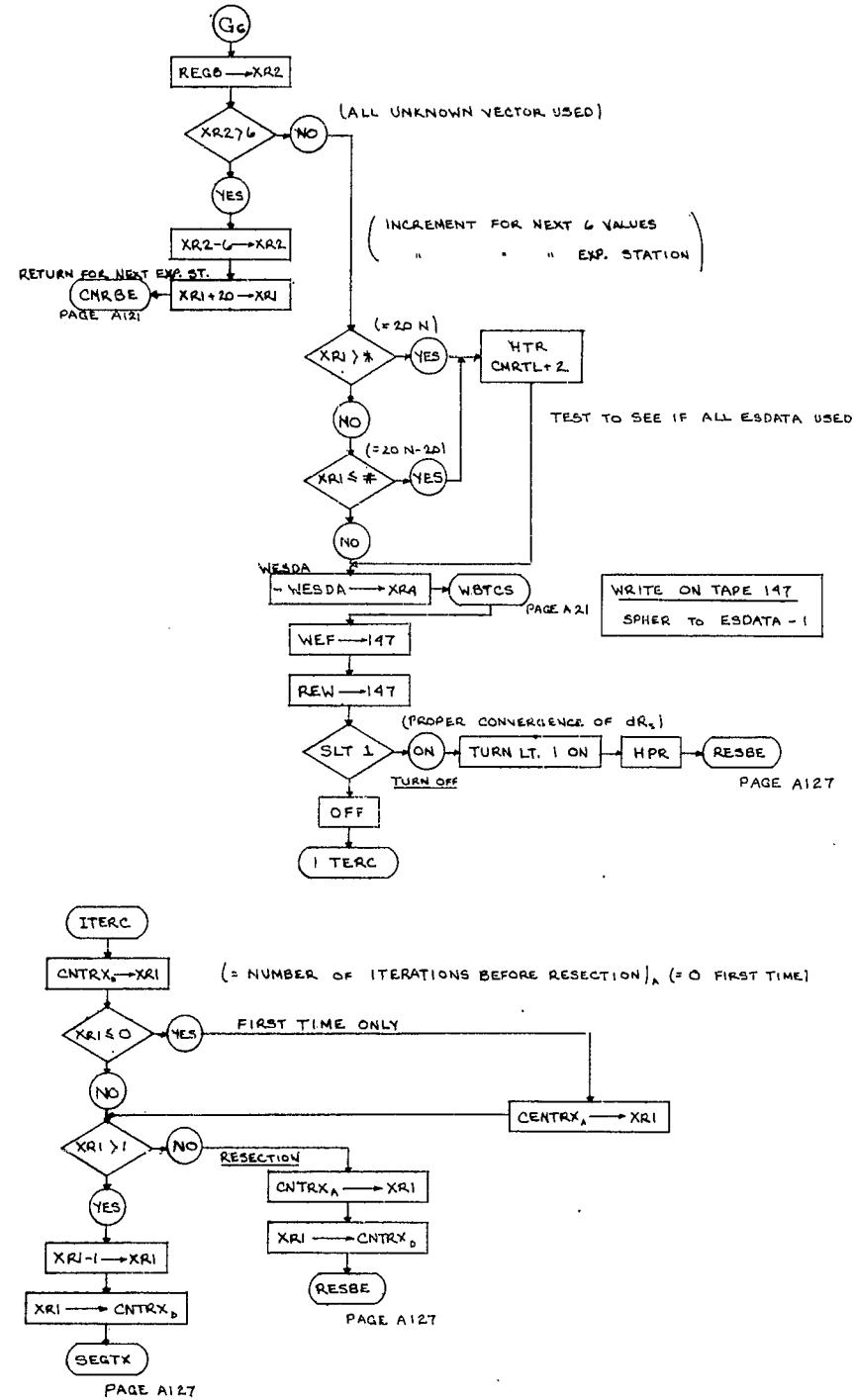


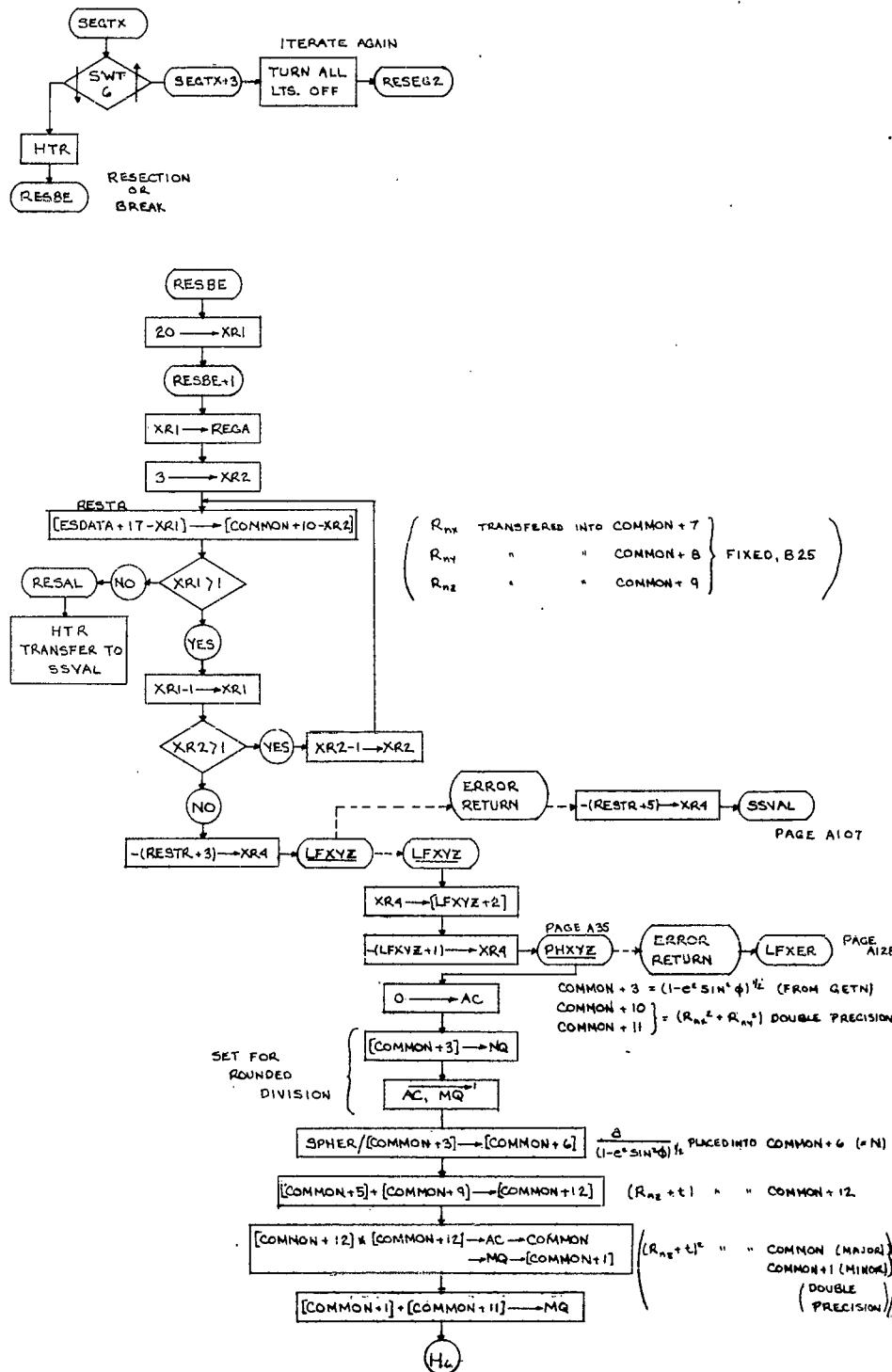


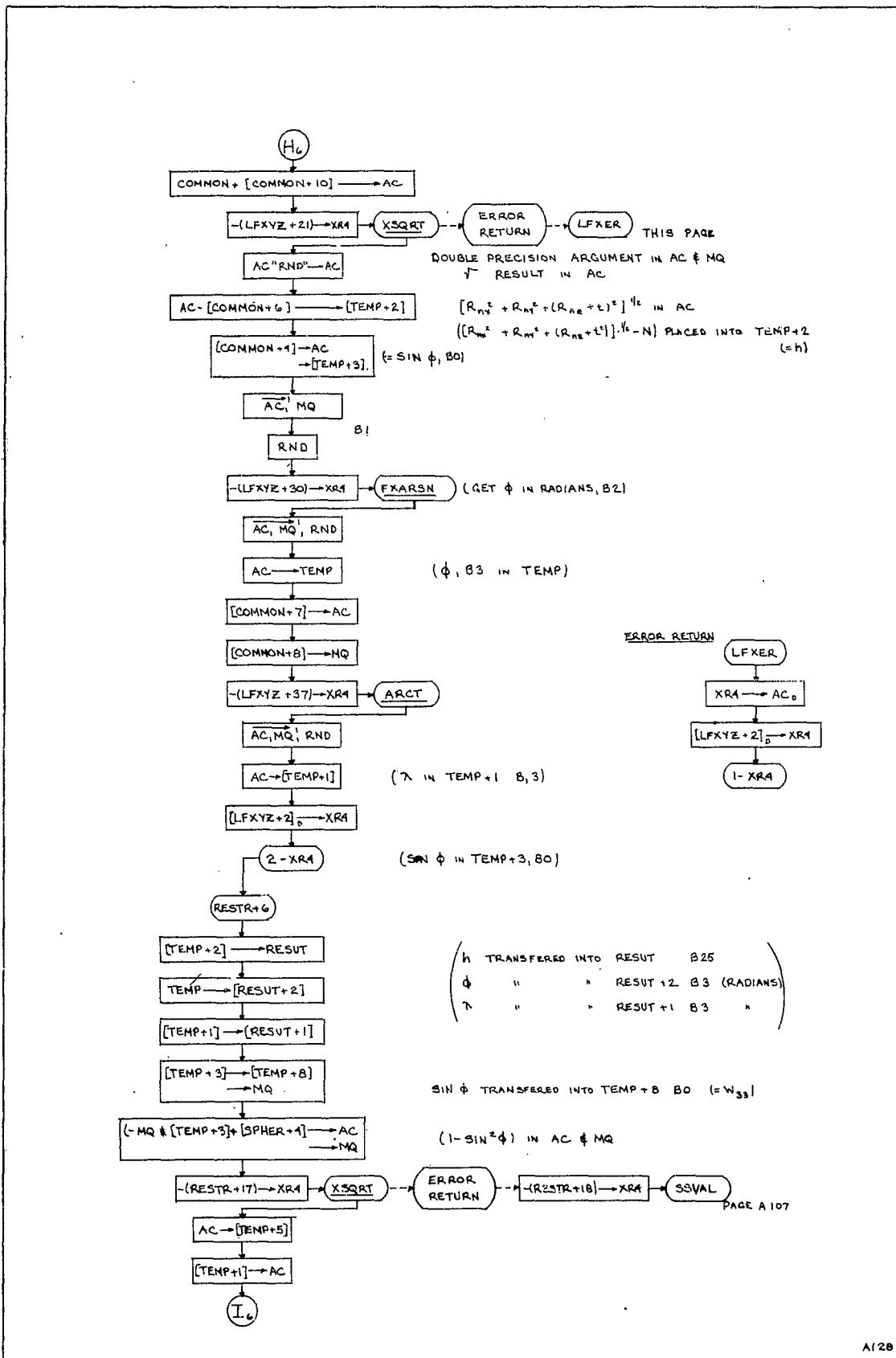


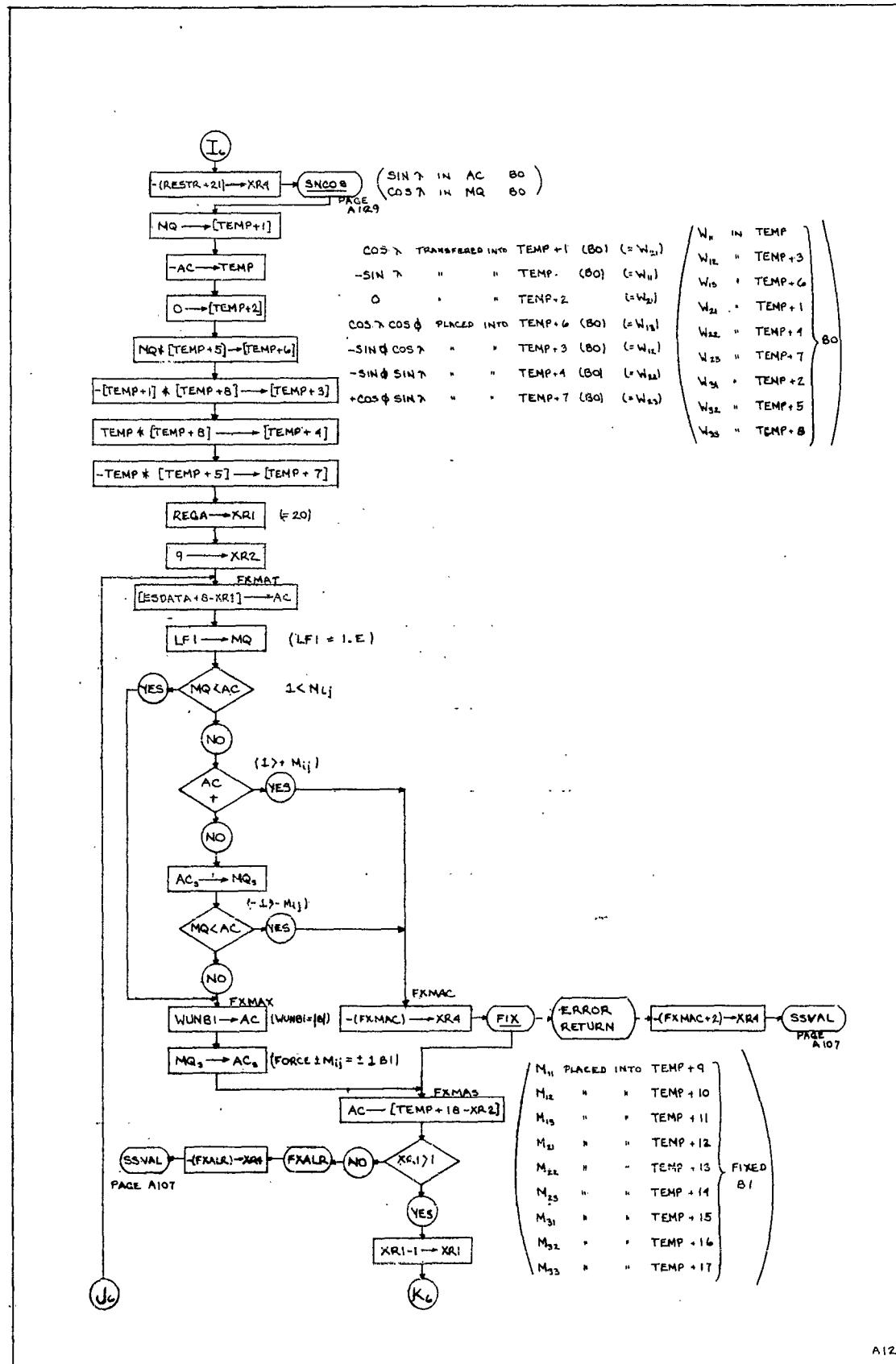


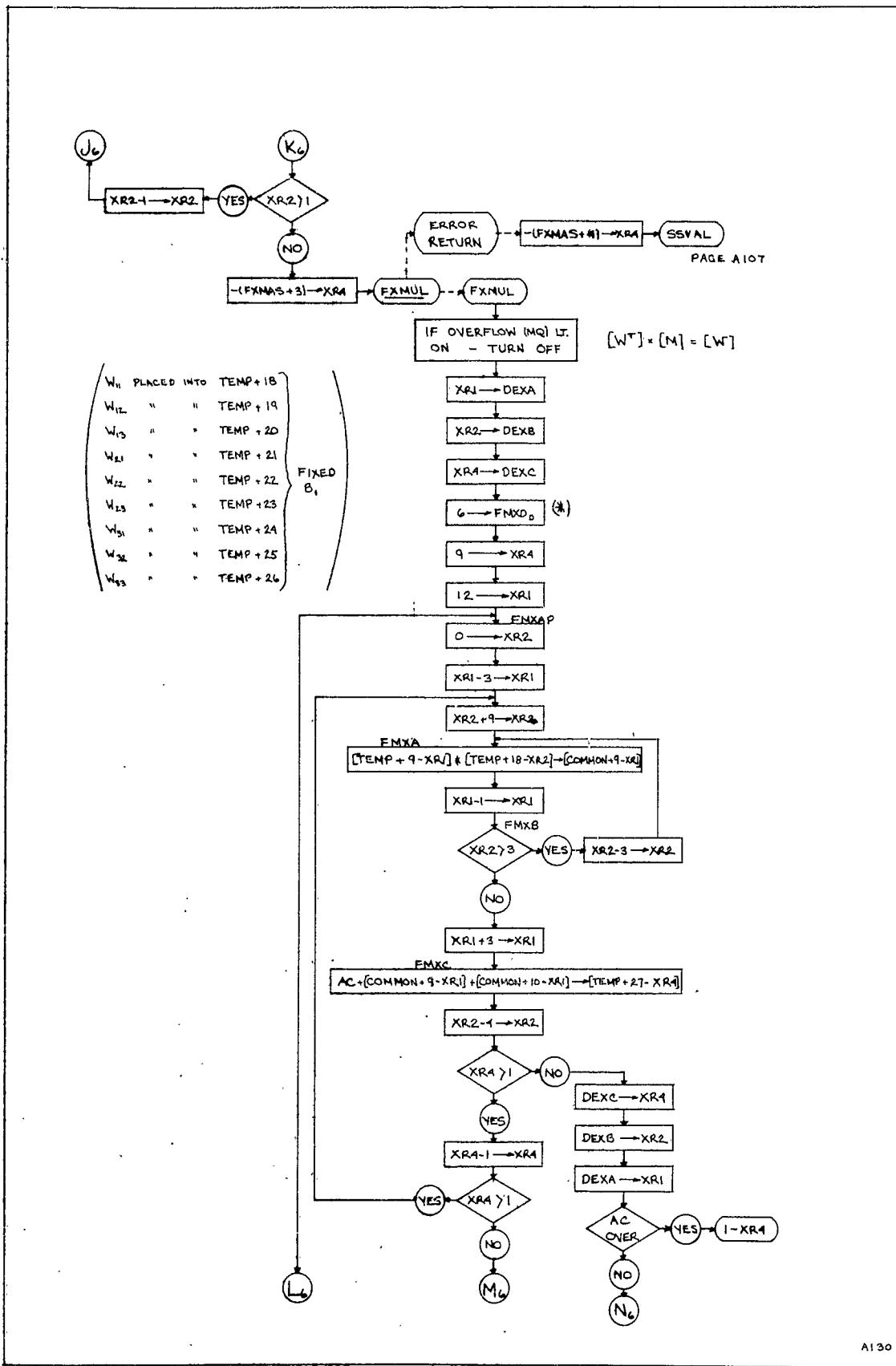


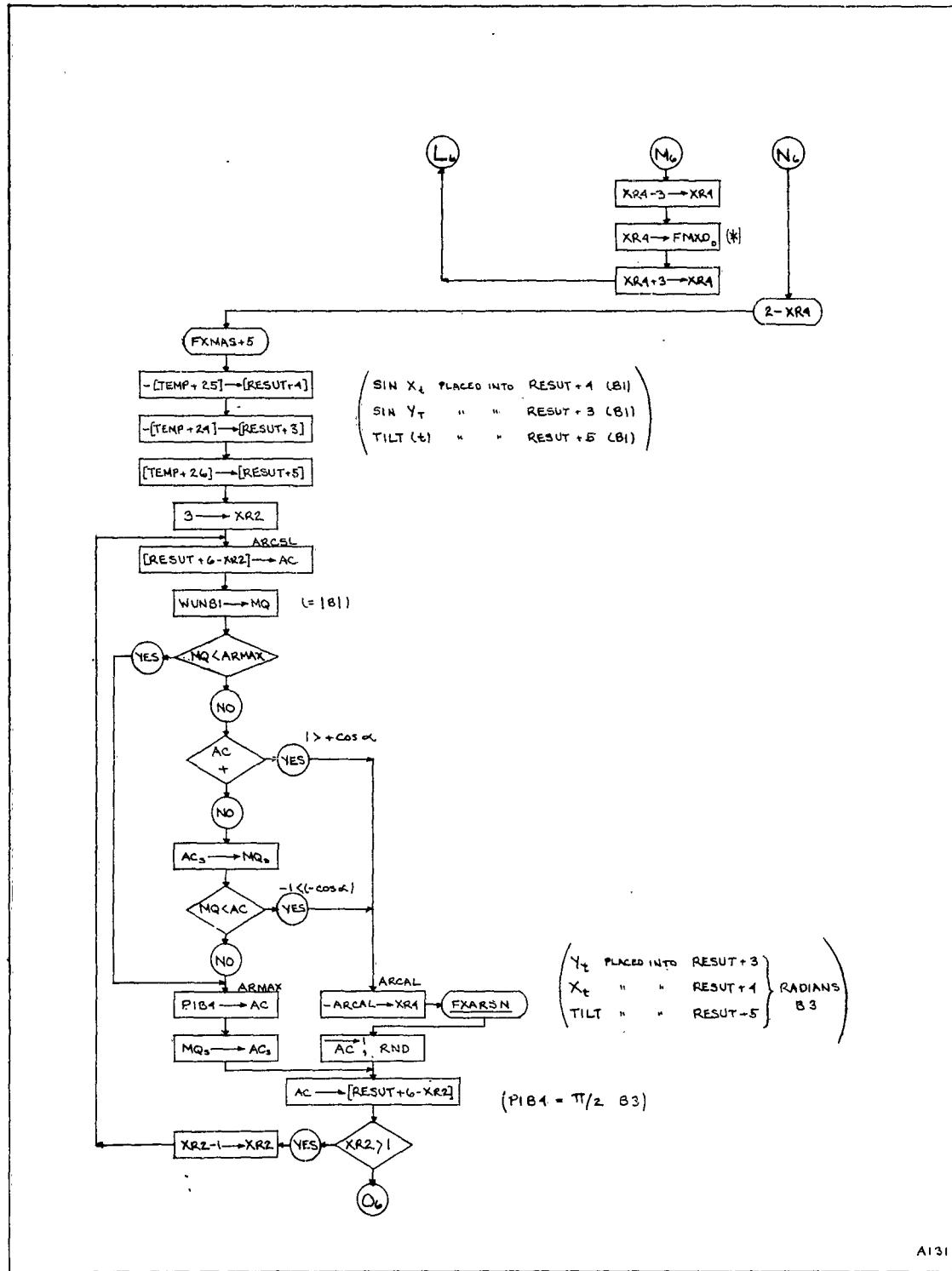


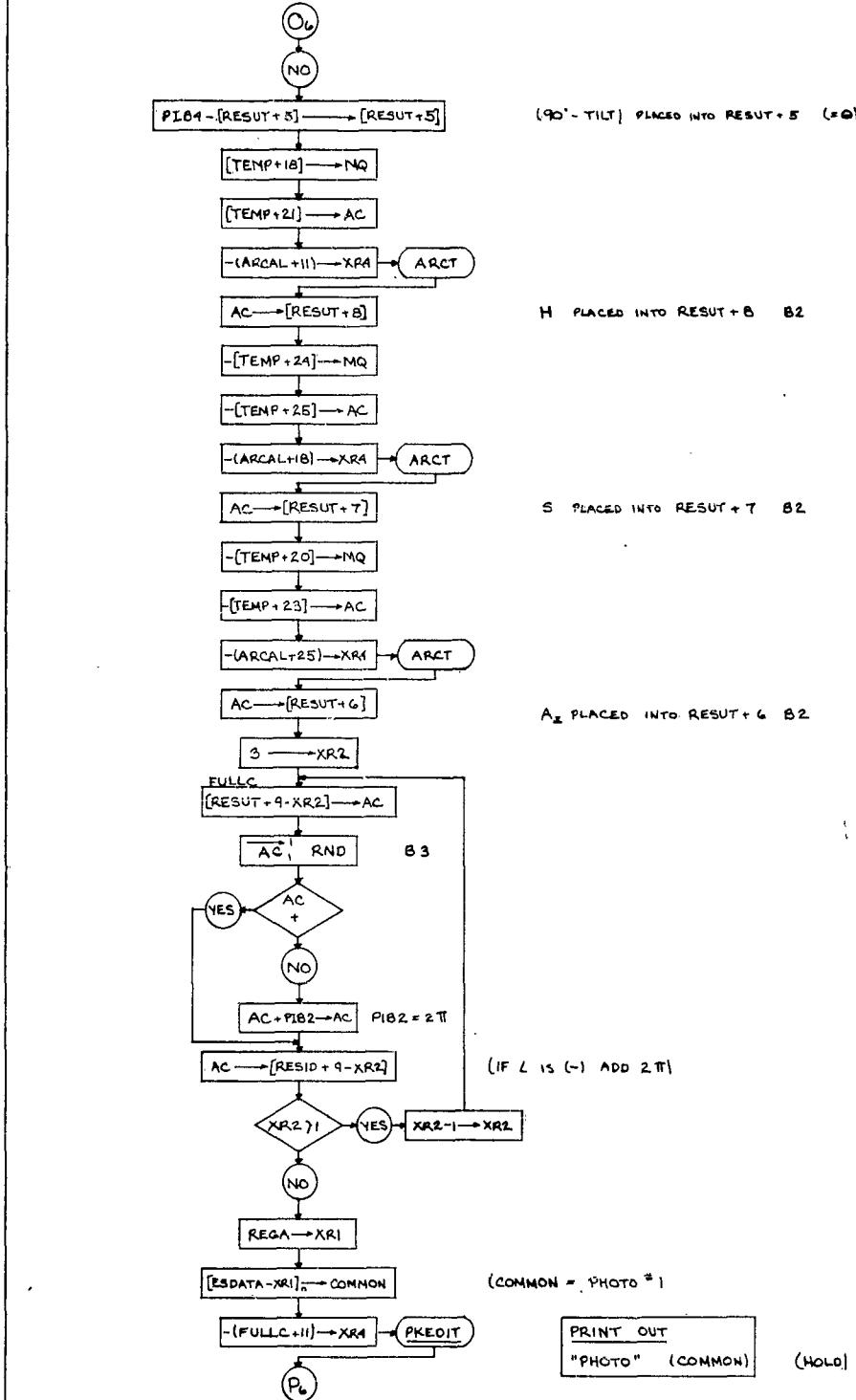


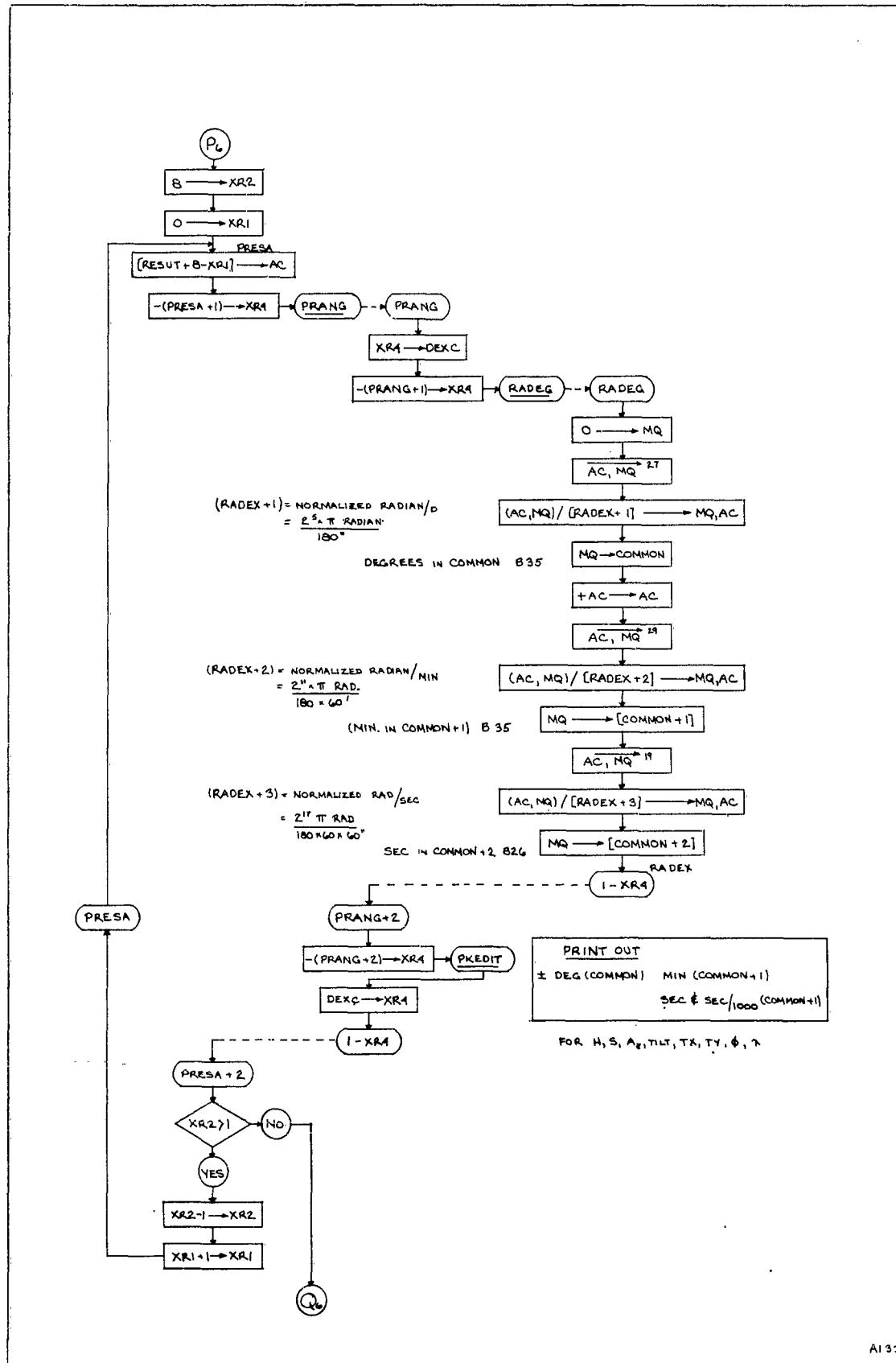


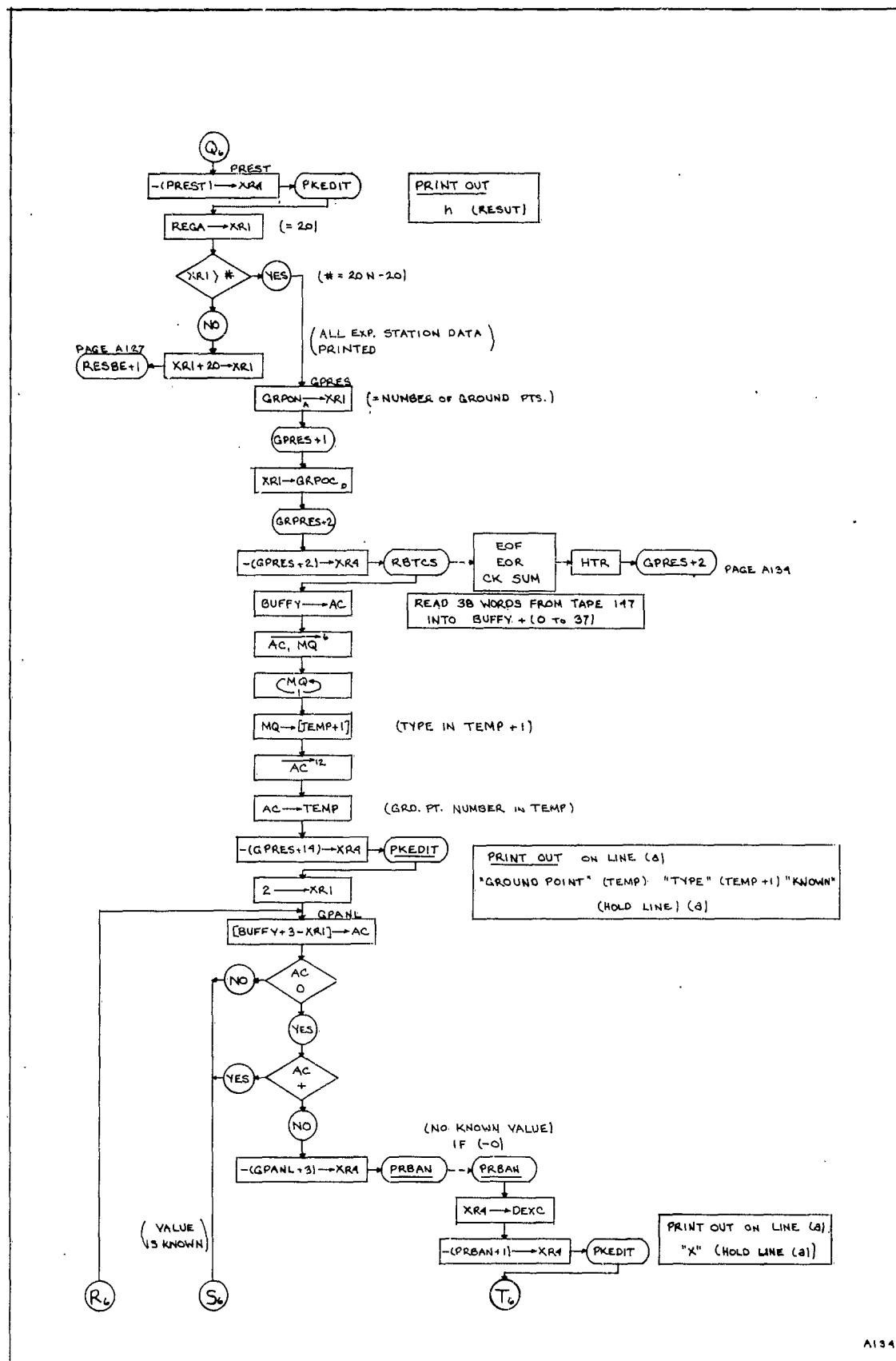


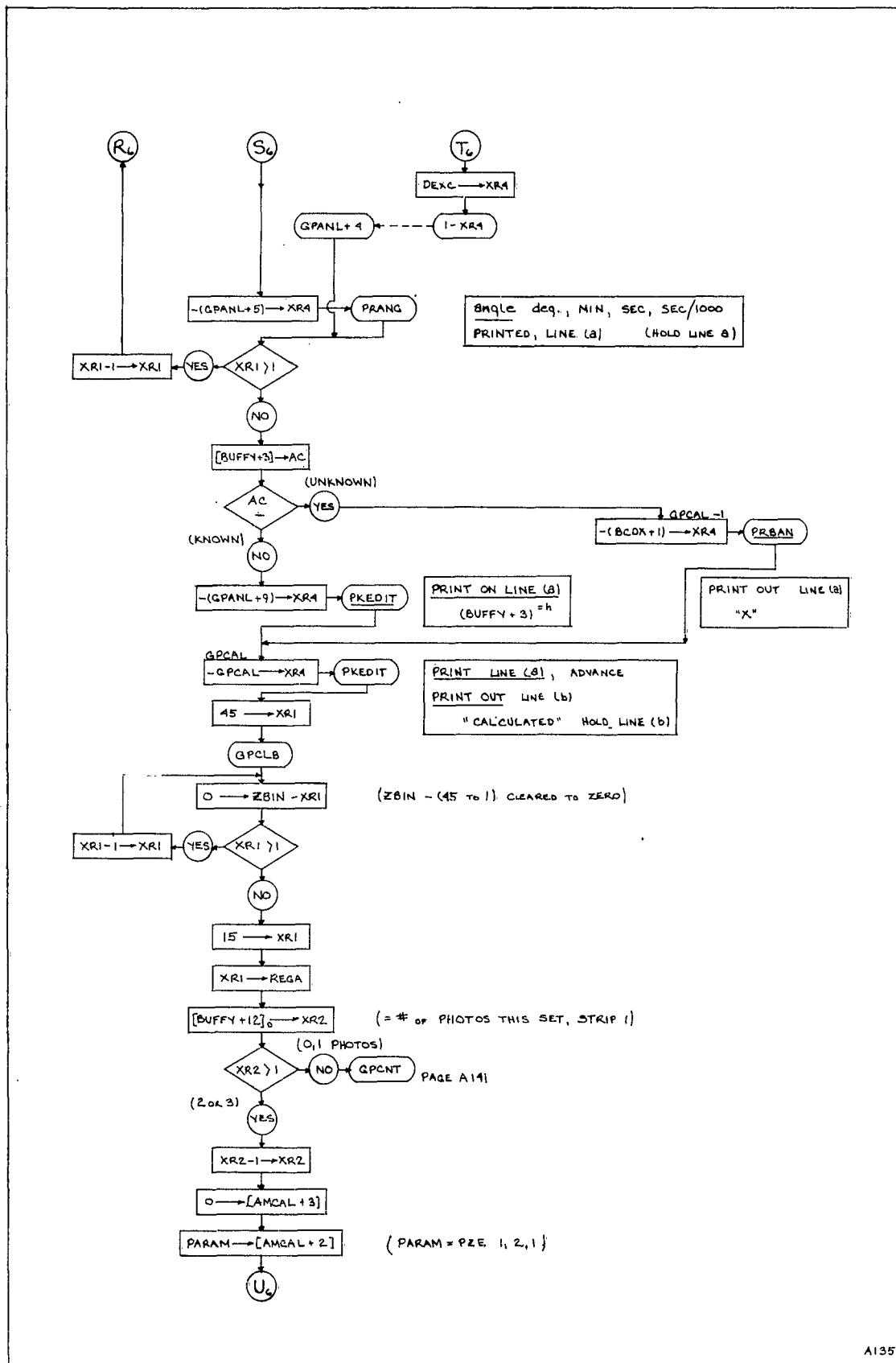


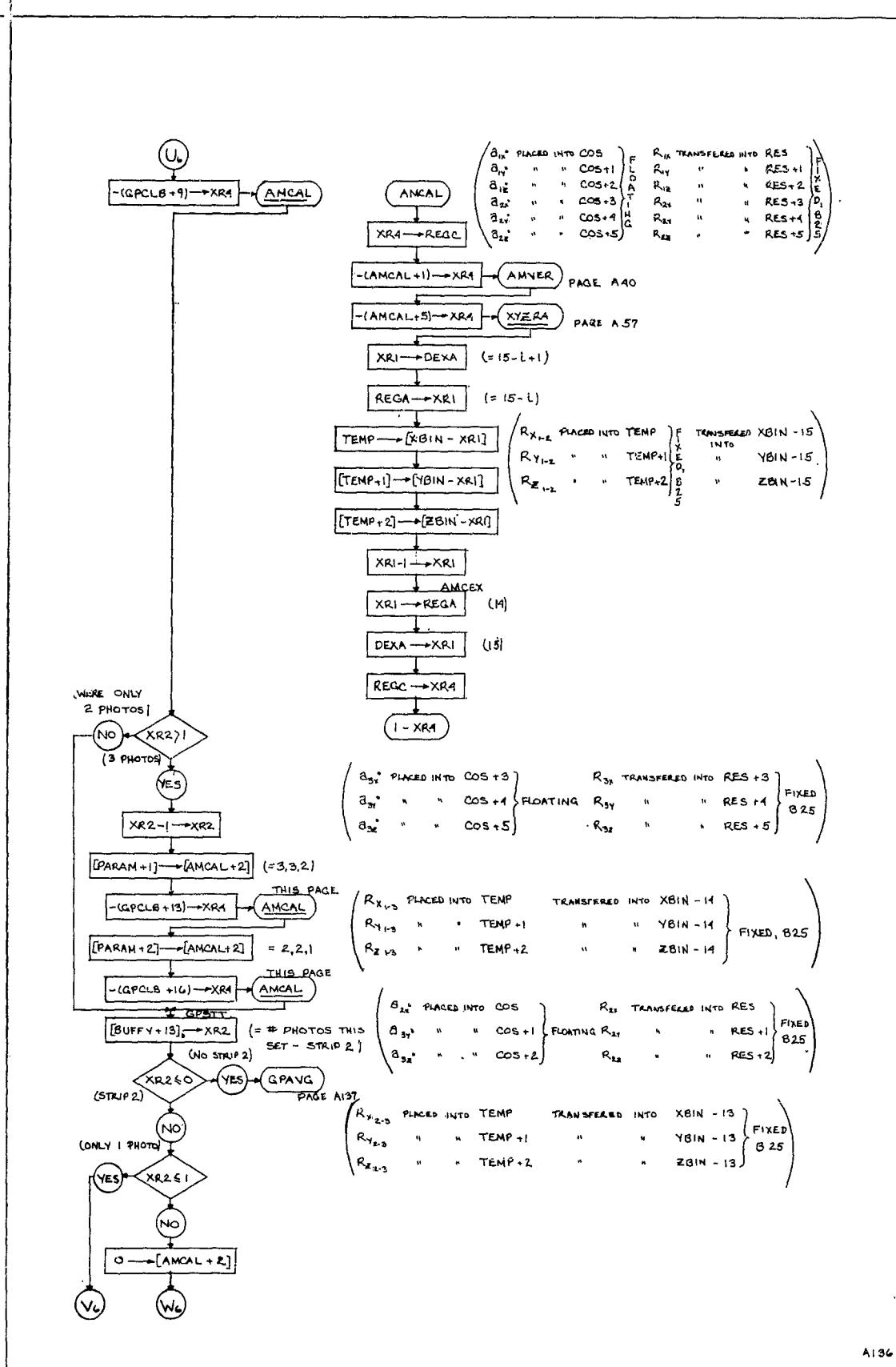


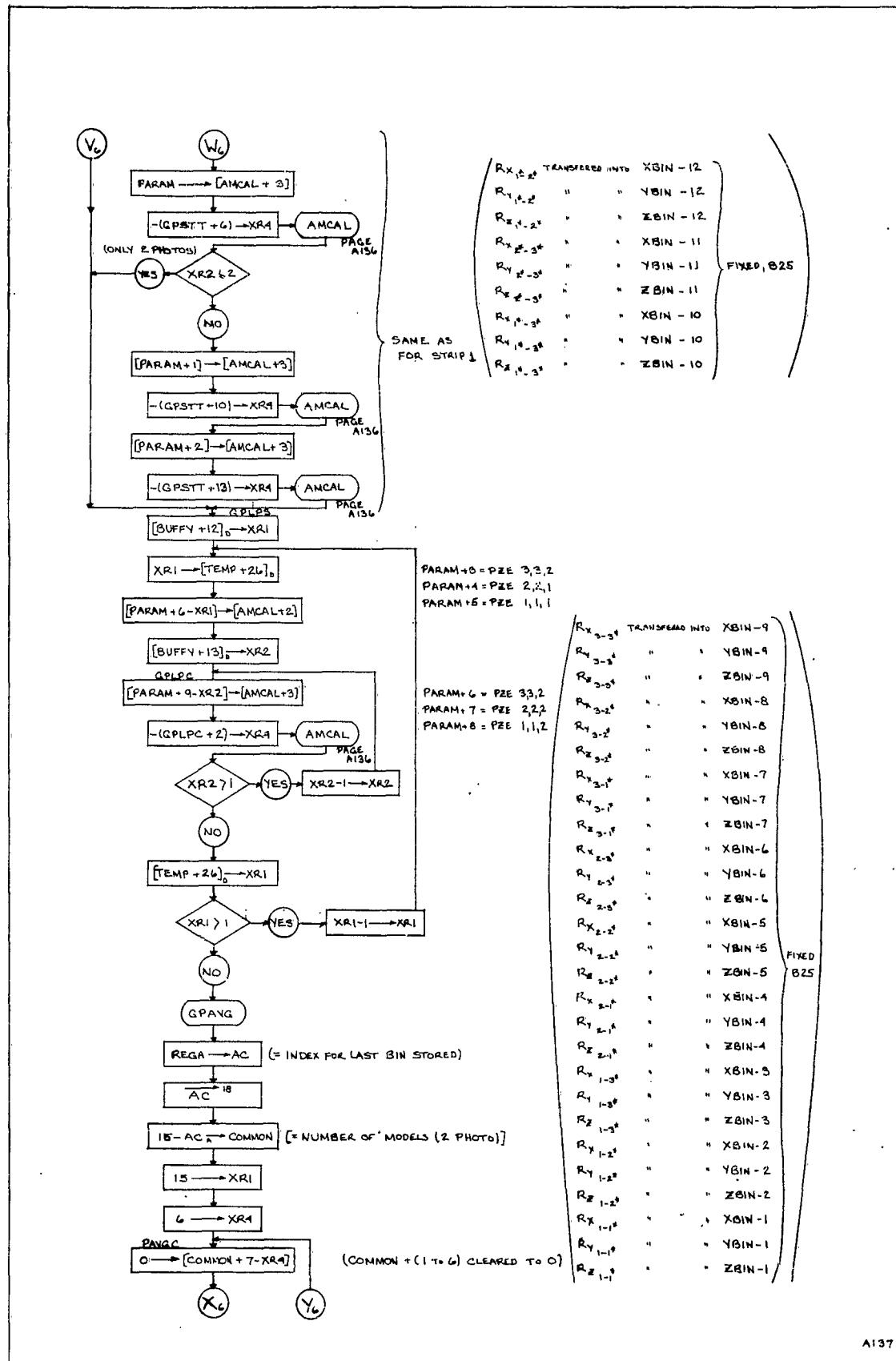


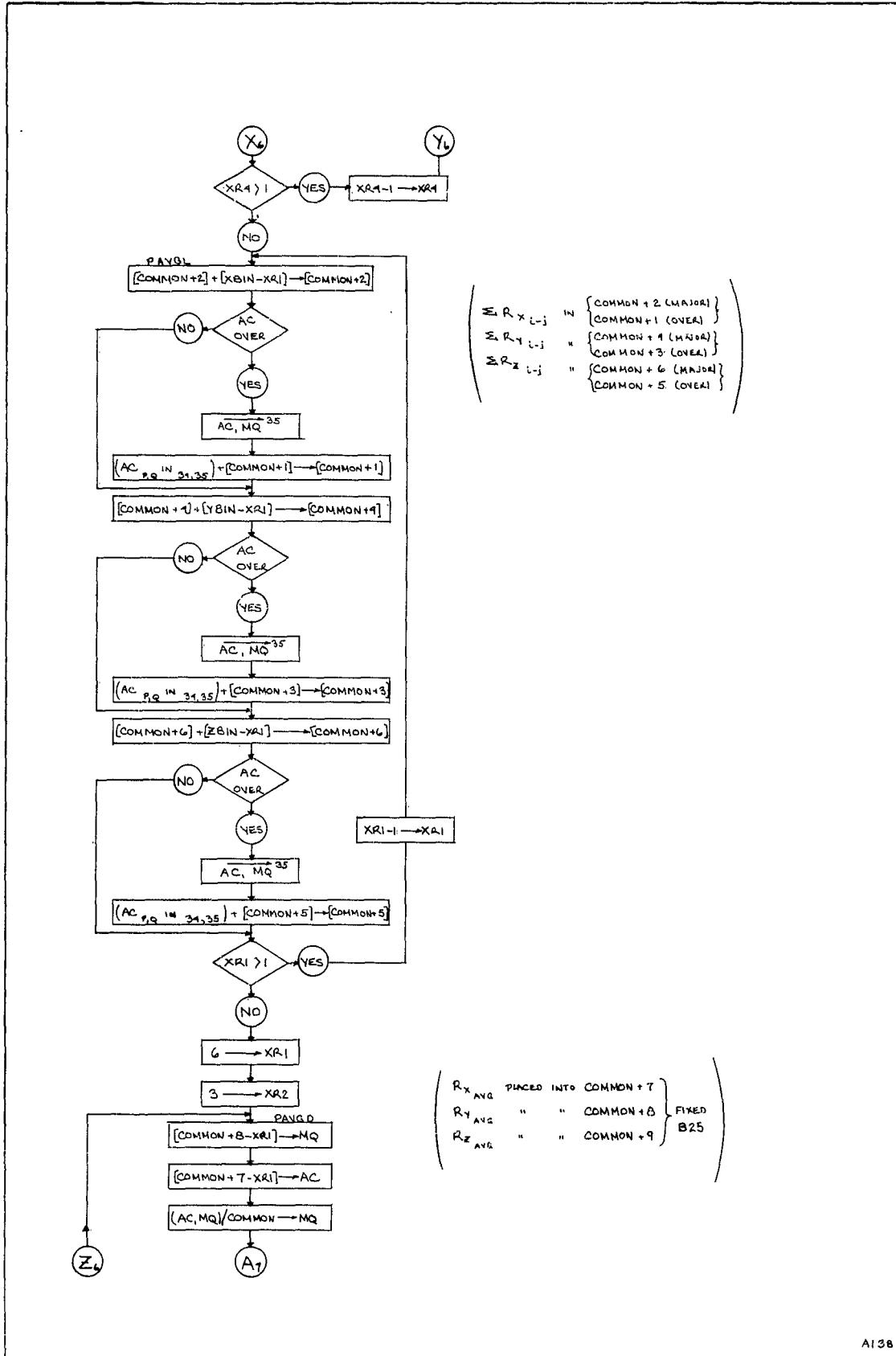


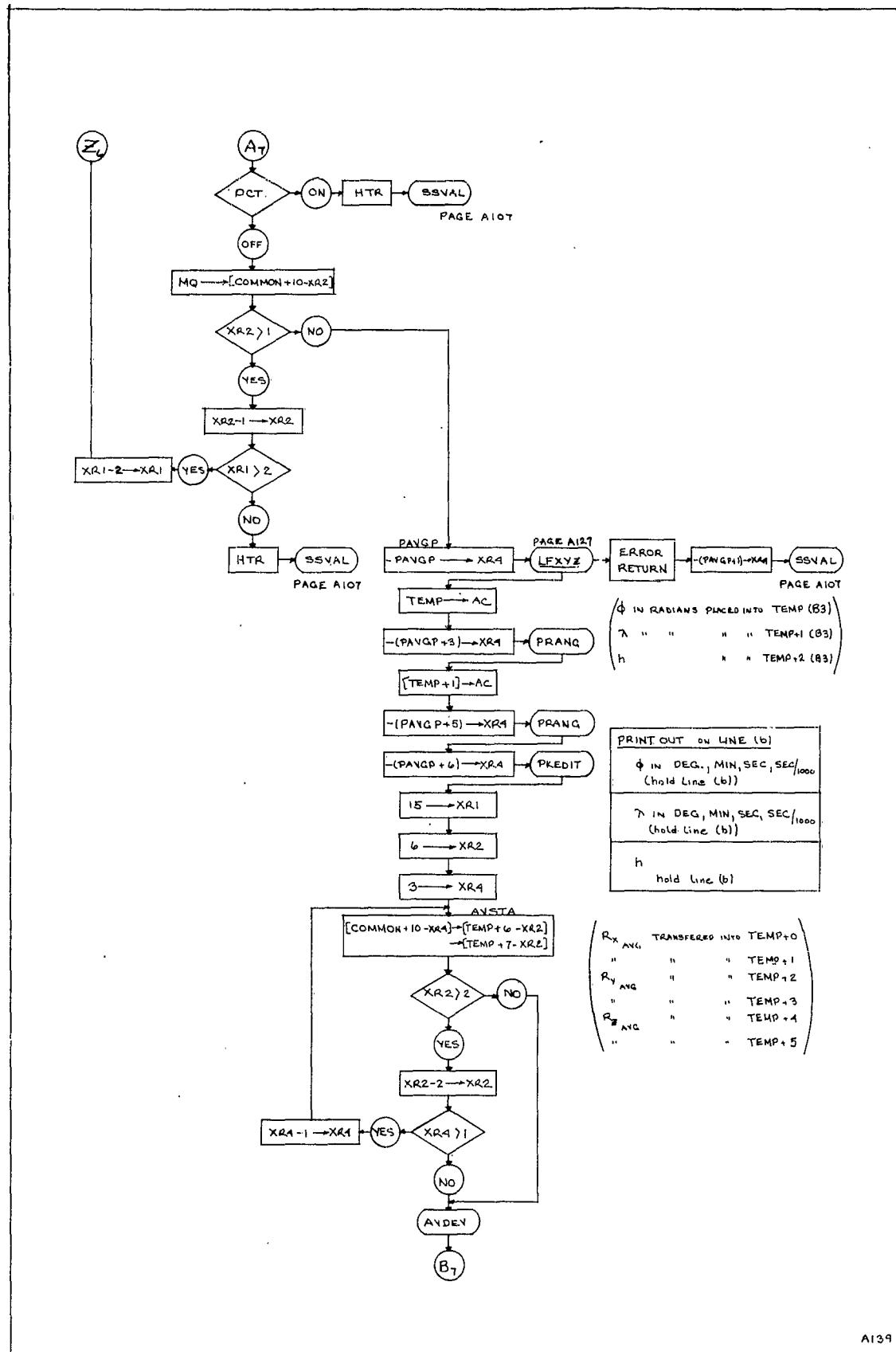


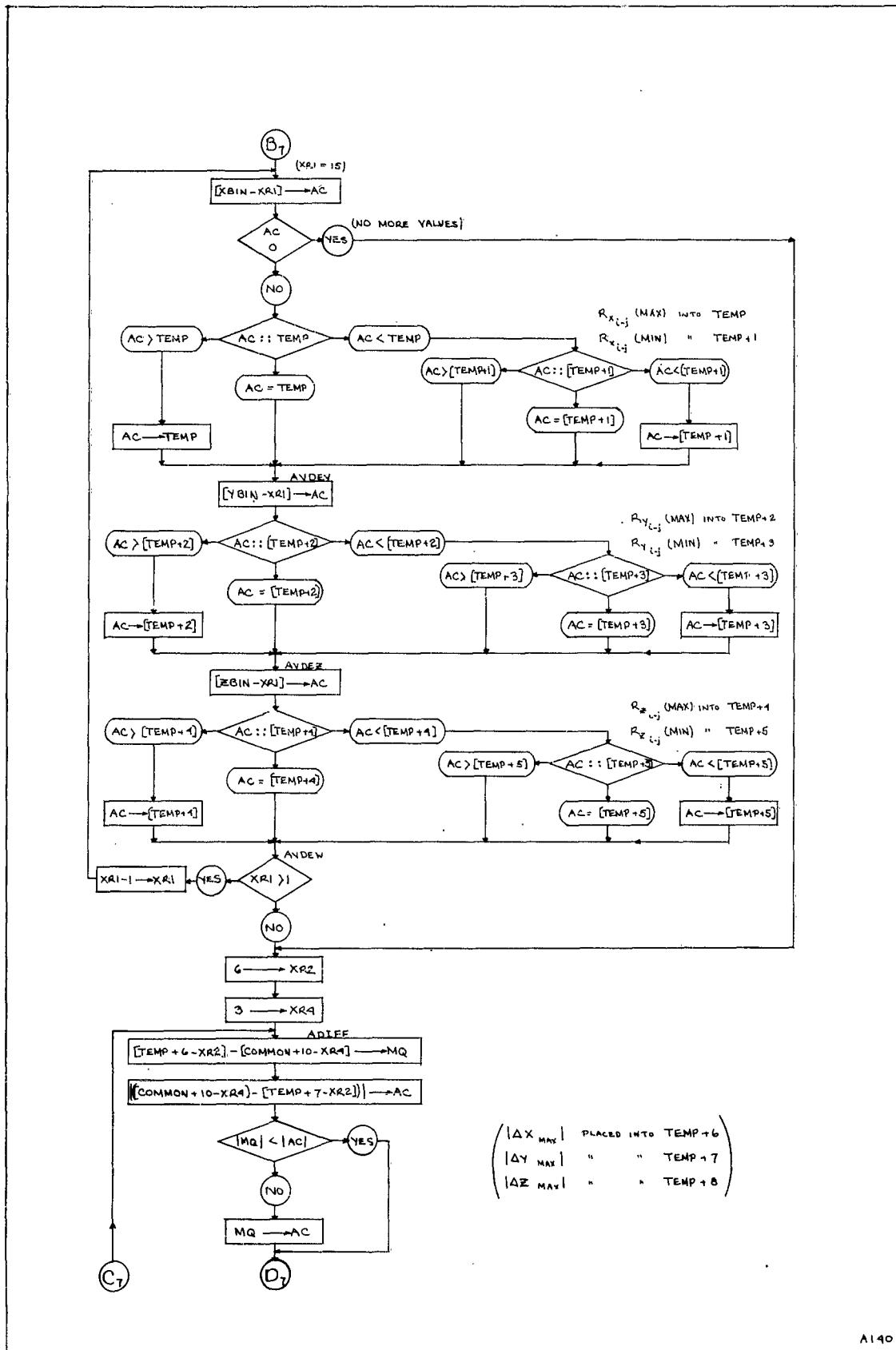








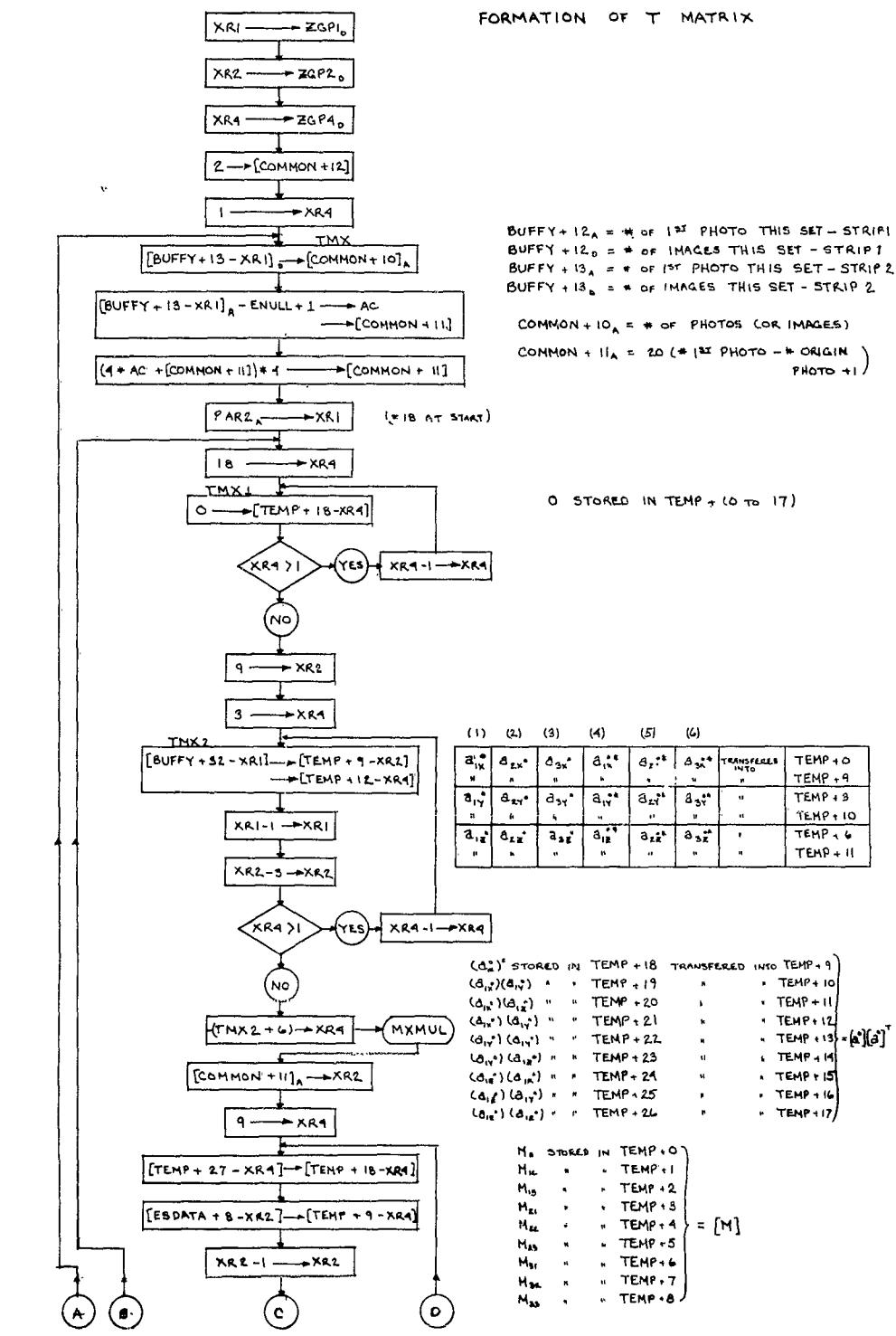


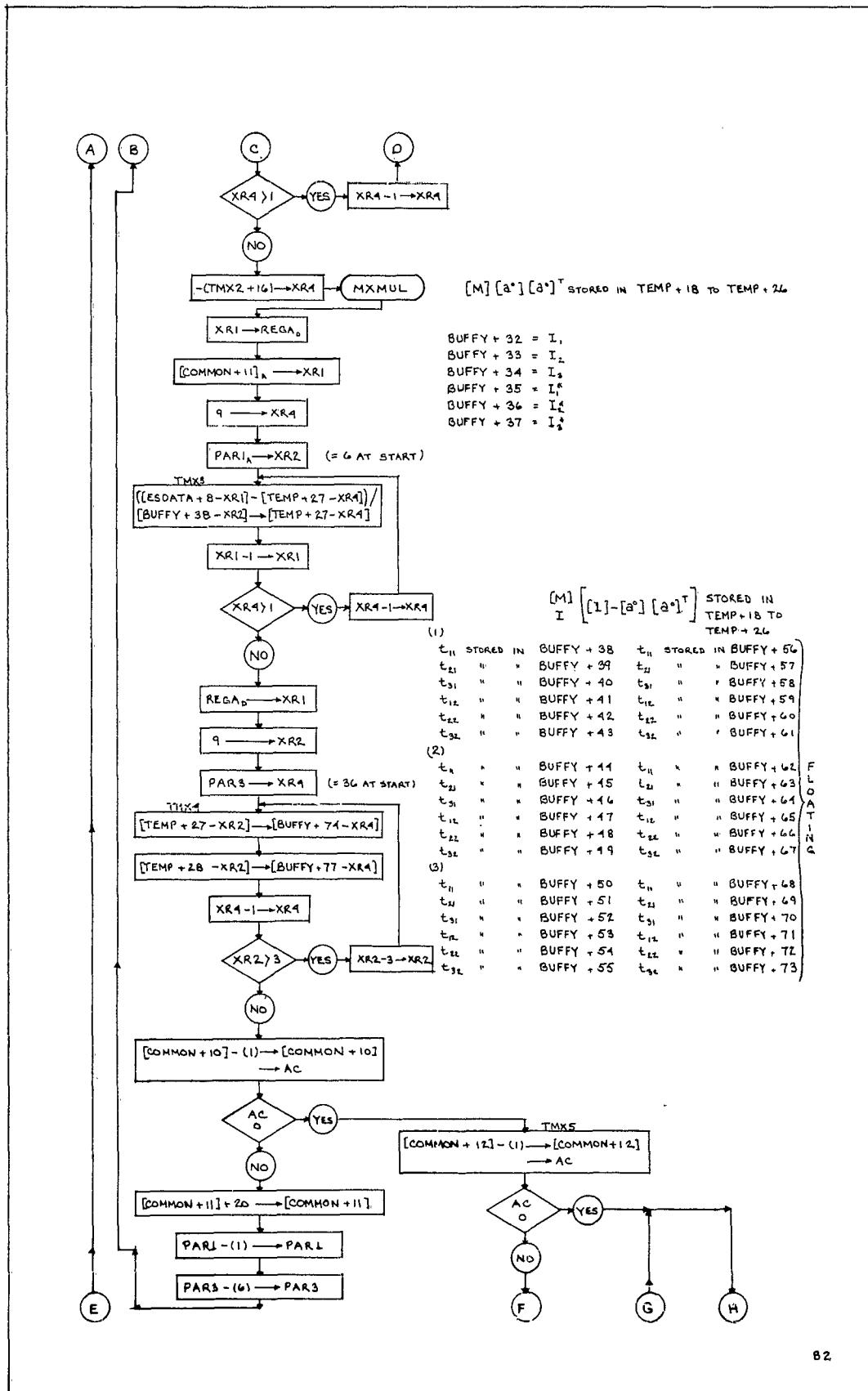


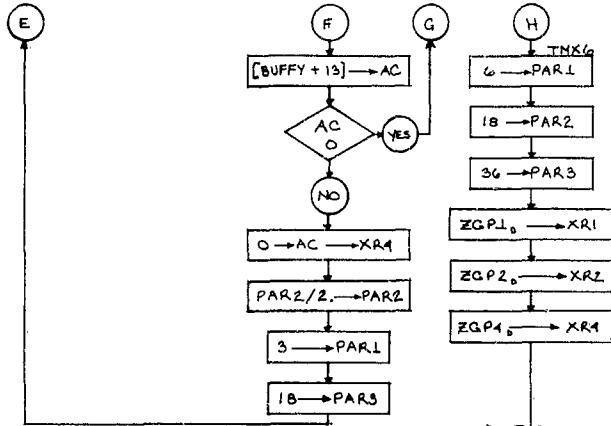
APPENDIX B

ADDITIONS AND MODIFICATIONS TO ORIGINAL PROGRAM - FLOW CHART

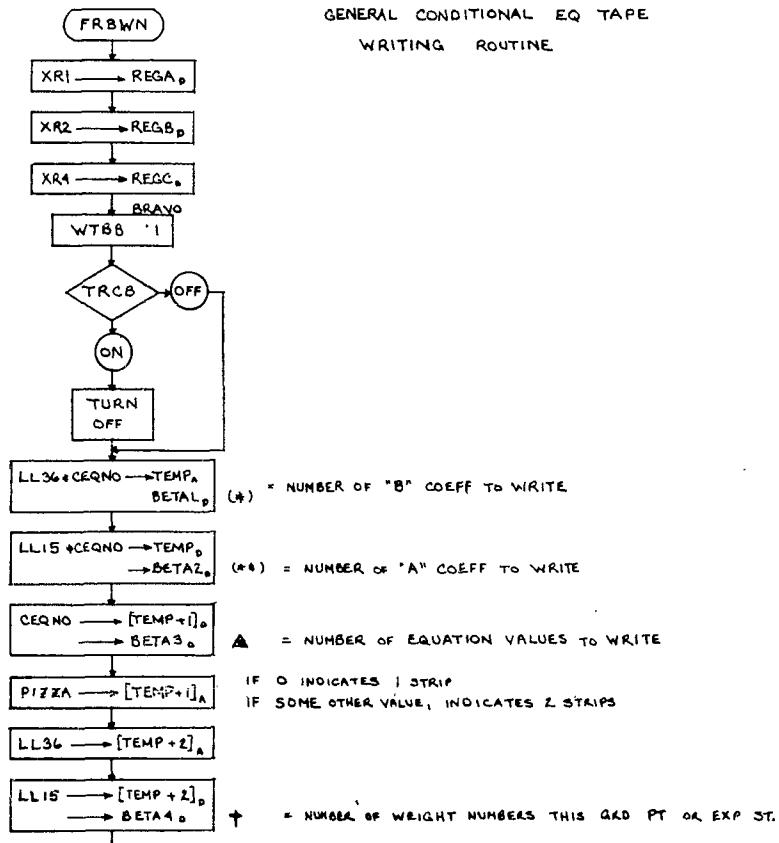
FORMATION OF T MATRIX

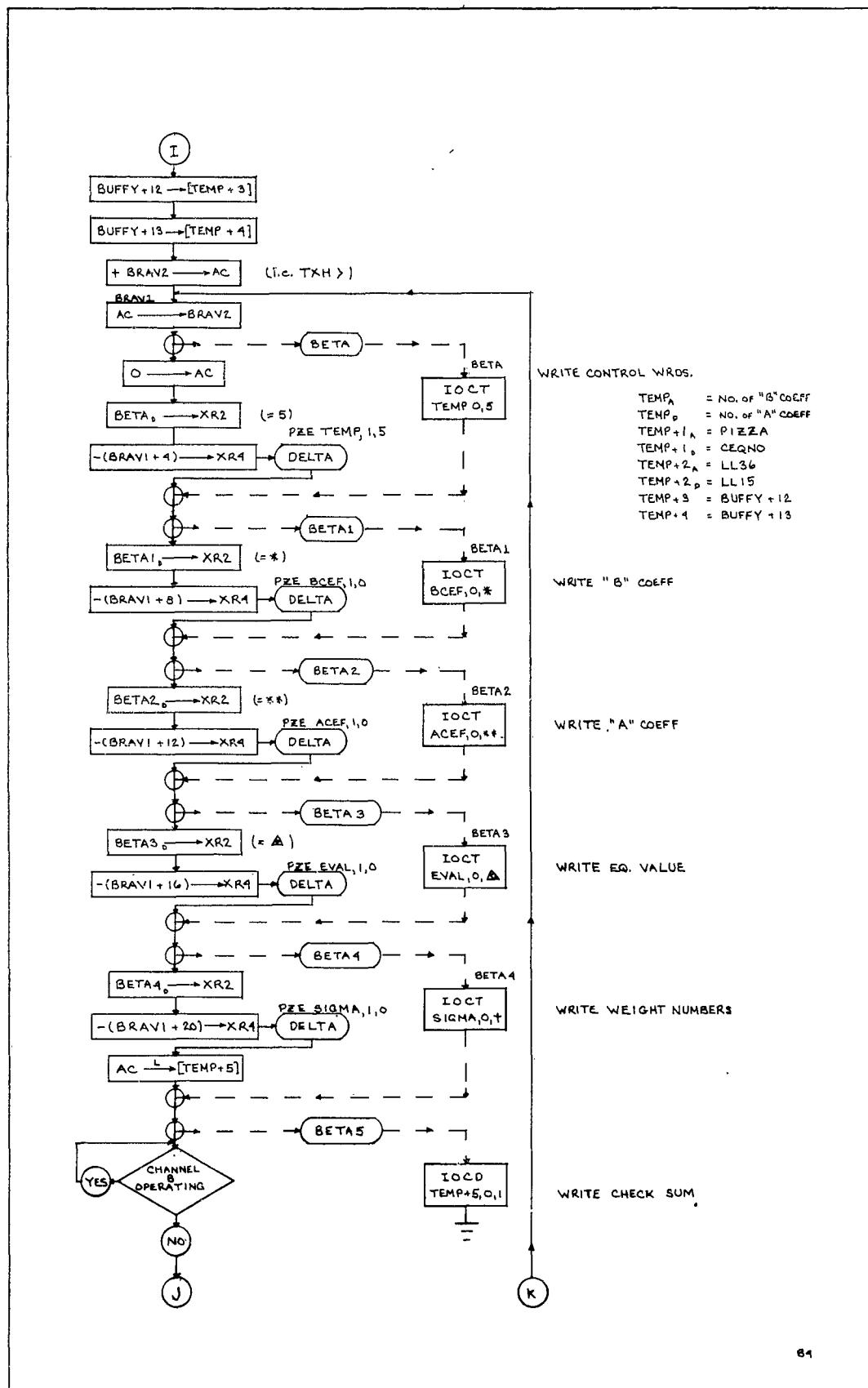


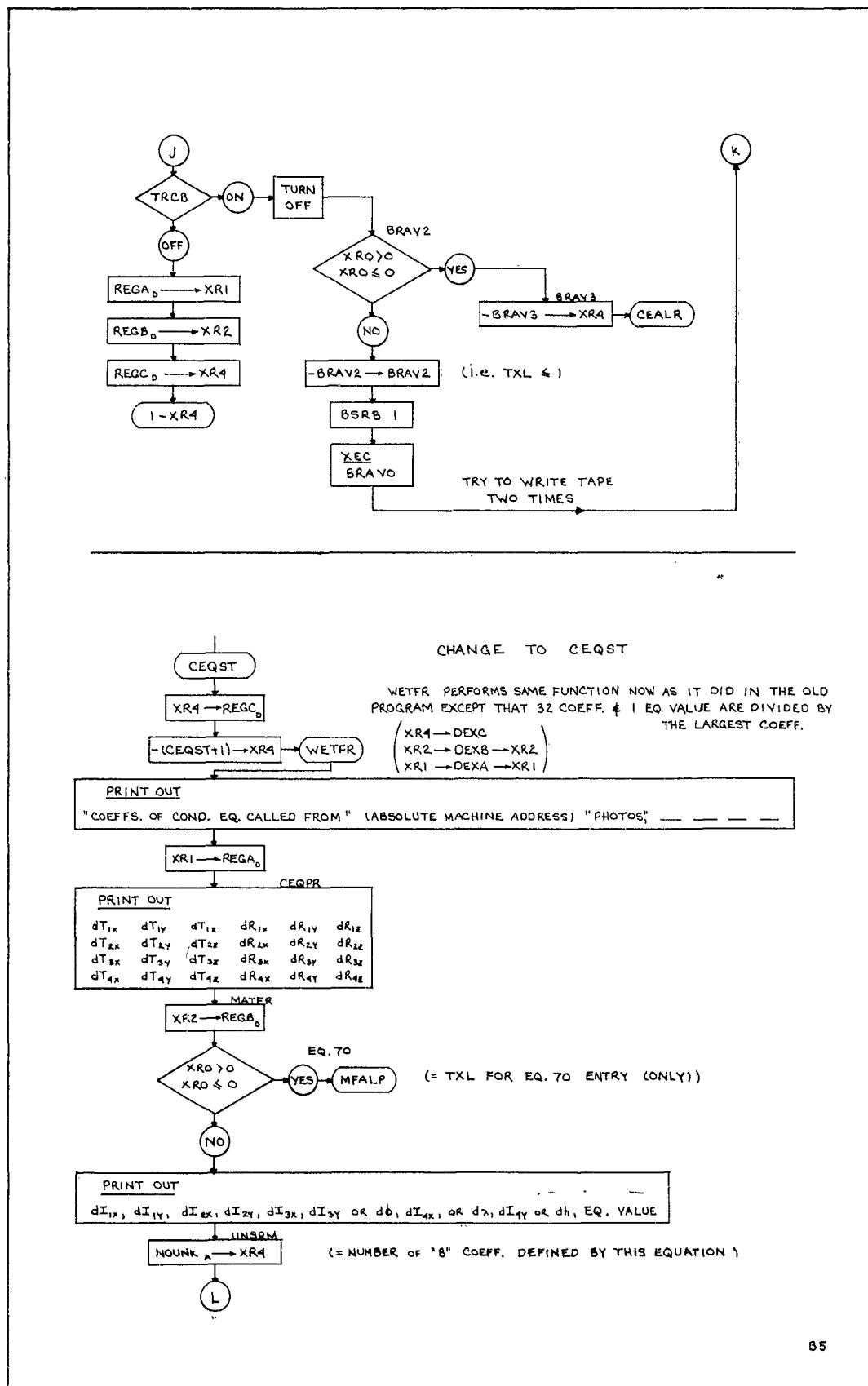


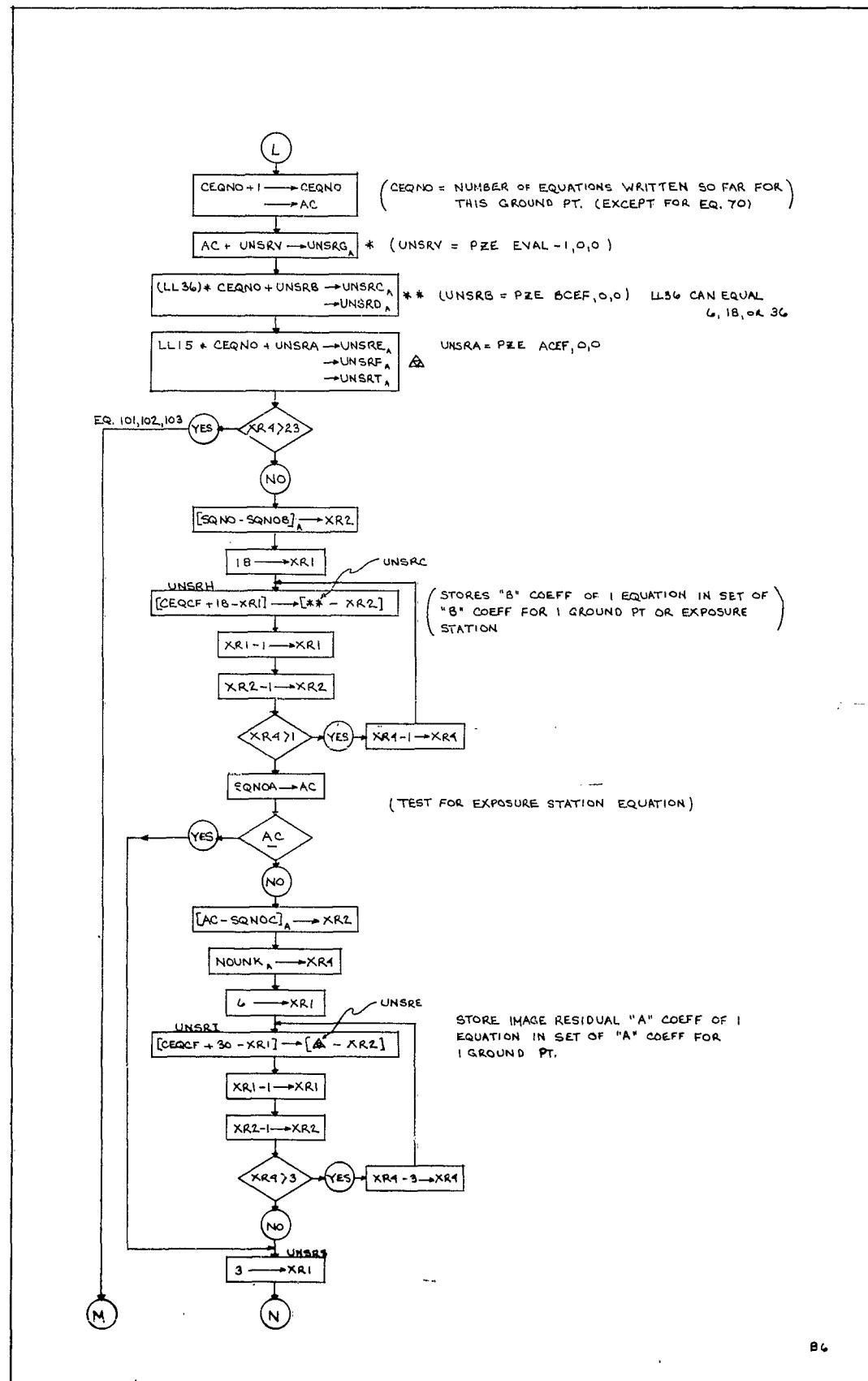


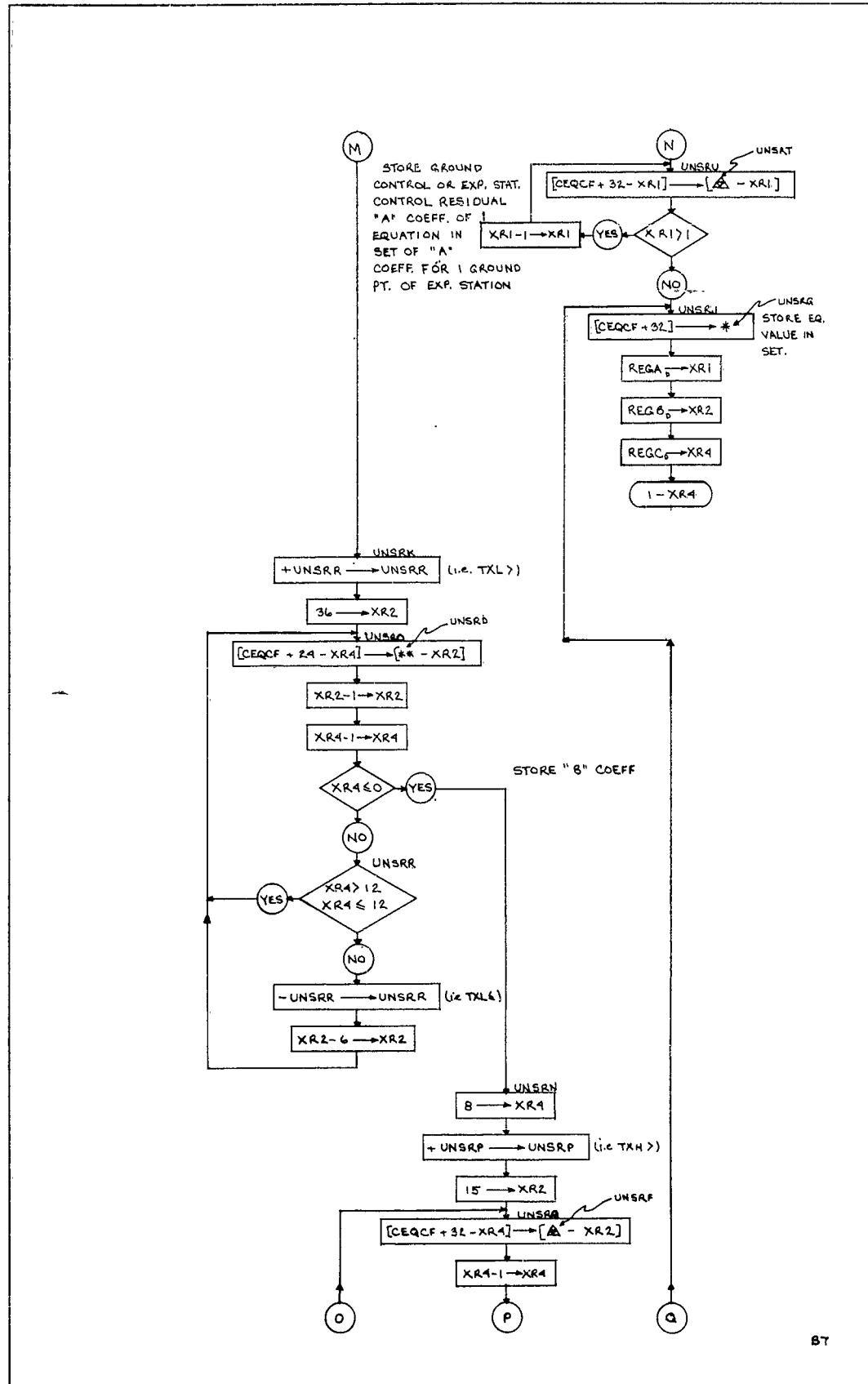
GENERAL CONDITIONAL EQ TAPE
WRITING ROUTINE

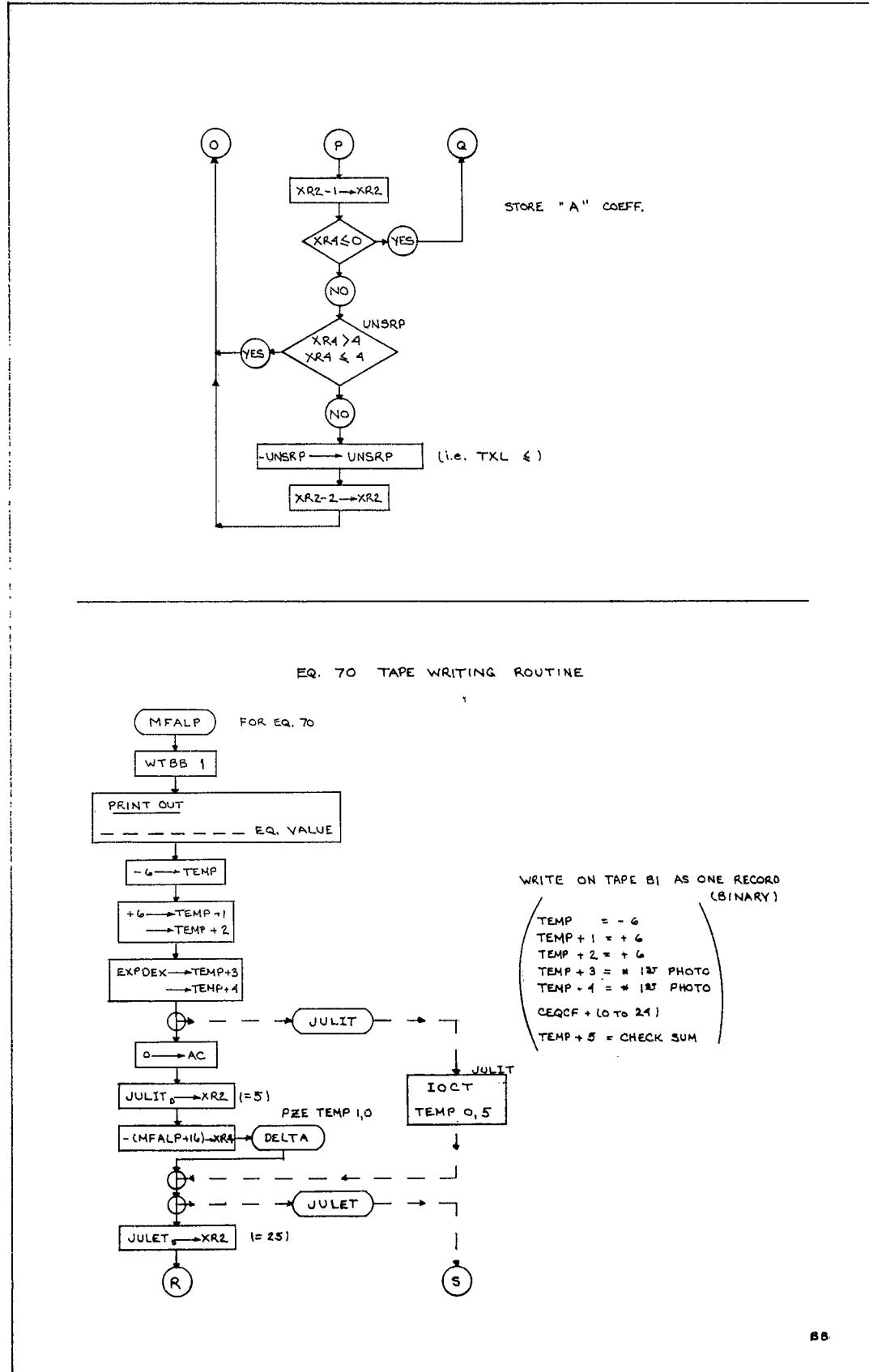


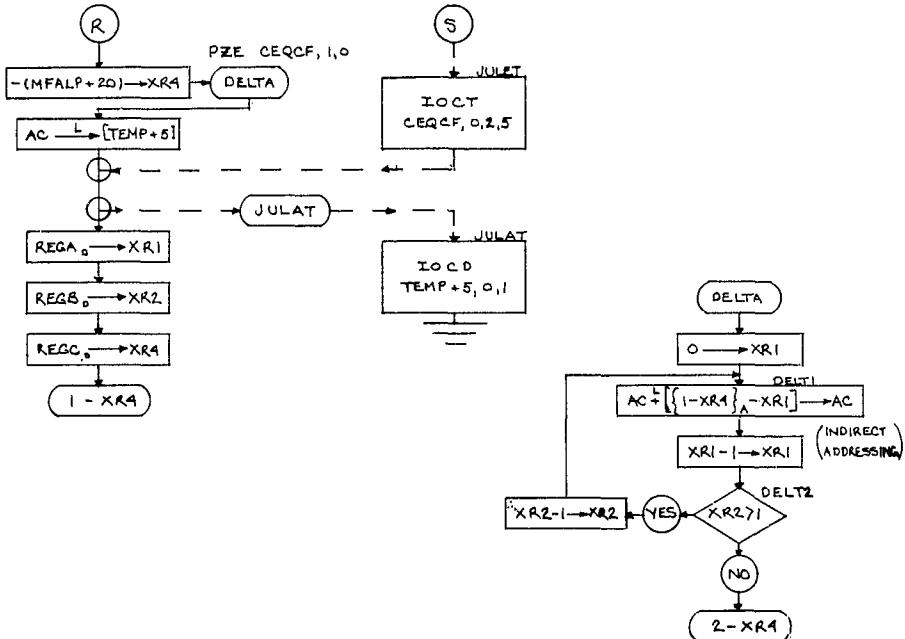




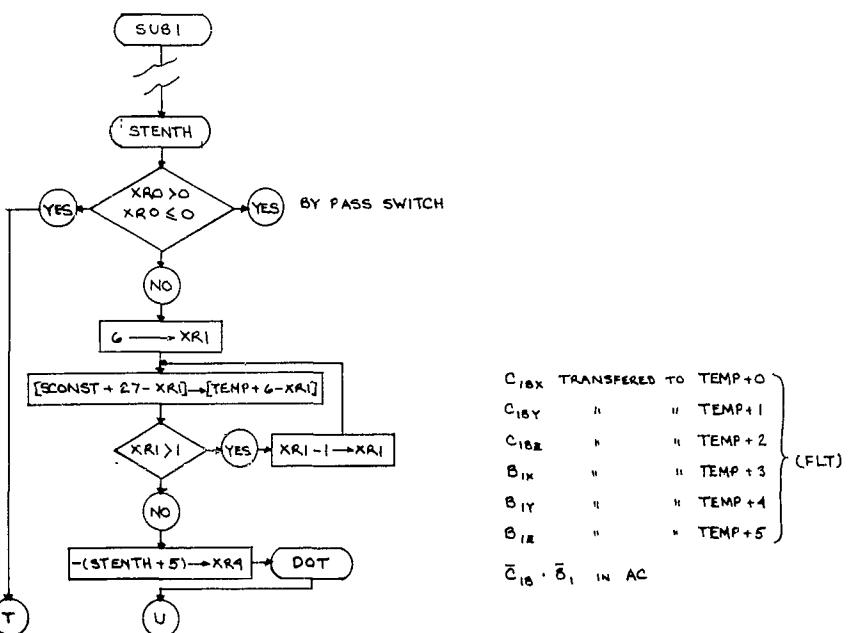


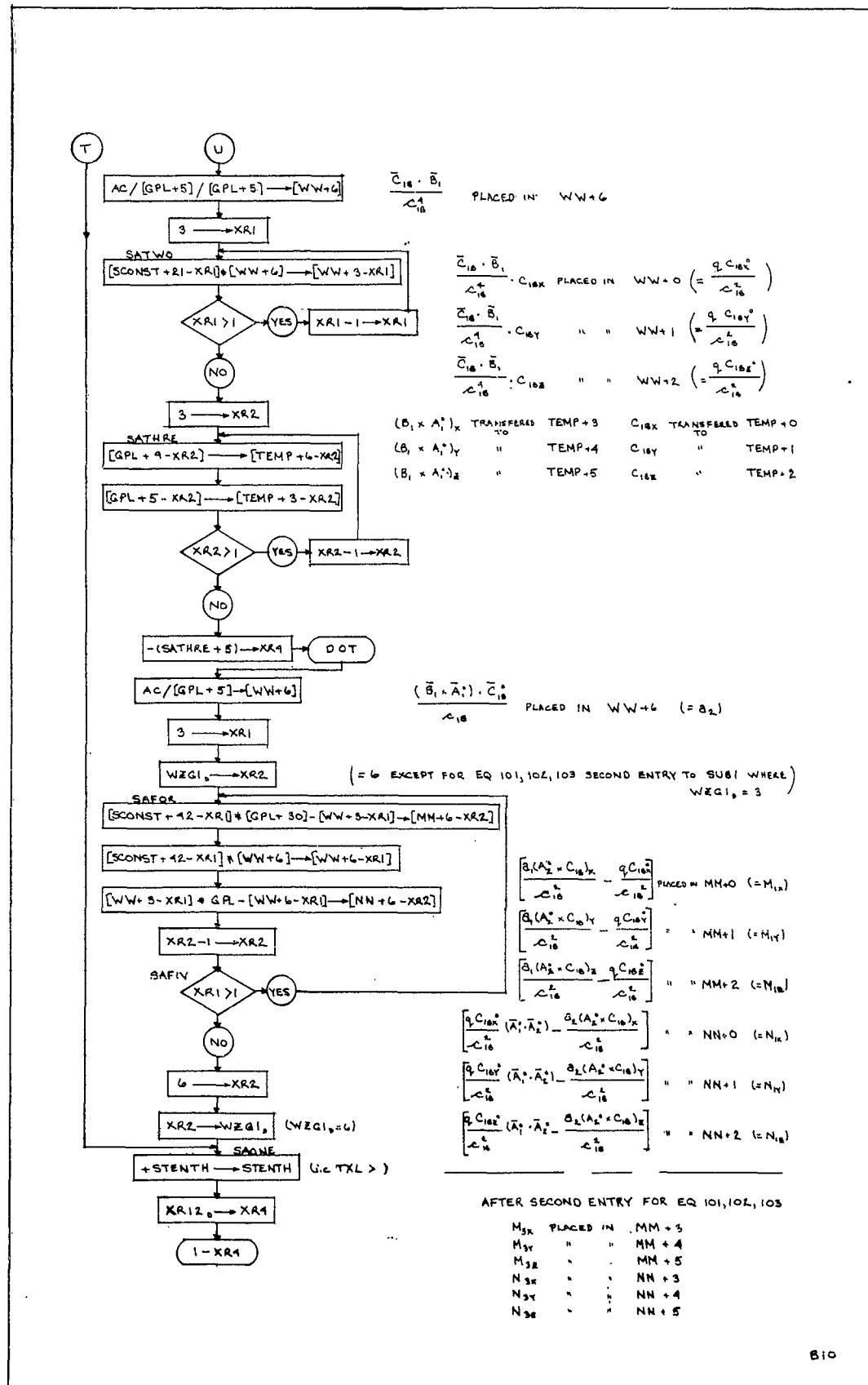






ADDITIONS TO SUB 1



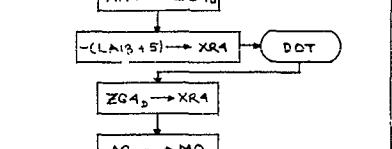
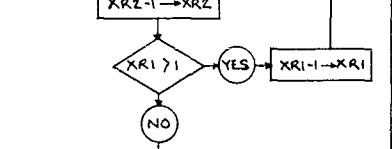
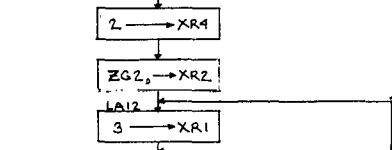
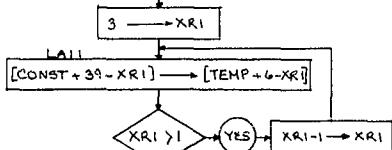


ADDITIONS TO EQ 1

IN CALLING SEQUENCE

	PHOTOS	1,2	2,3	1*,2*	2*,3*
SQNOA	=	36	30	18	12
ZG2 ₀	=	36	30	18	12
SQNOA ₀	=	15	13	9	7

EQ 1



1ST LOOP.

$C_{10X}^{(i)}$ TRANSFERRED TO TEMP + 3
 $C_{10Y}^{(i)}$ " " TEMP + 1
 $C_{10Z}^{(i)}$ " " TEMP + 5

2ND LOOP

$t_{12}^{(i)}$ TRANSFERRED TO TEMP
 $t_{22}^{(i)}$ " " TEMP + 1
 $t_{32}^{(i)}$ " " TEMP + 2

$t_{12}^{(i)}$ TRANSFERRED TO TEMP
 $t_{22}^{(i)}$ " " TEMP + 1
 $t_{32}^{(i)}$ " " TEMP + 2

$$AC = C_{10X}^{(i)} t_{12}^{(i)} + C_{10Y}^{(i)} t_{22}^{(i)} + C_{10Z}^{(i)} t_{32}^{(i)}$$

$$AC = C_{10X}^{(i)} t_{12}^{(i)} + C_{10Y}^{(i)} t_{22}^{(i)} + C_{10Z}^{(i)} t_{32}^{(i)}$$

dI_H STORED IN CEQCF + 24

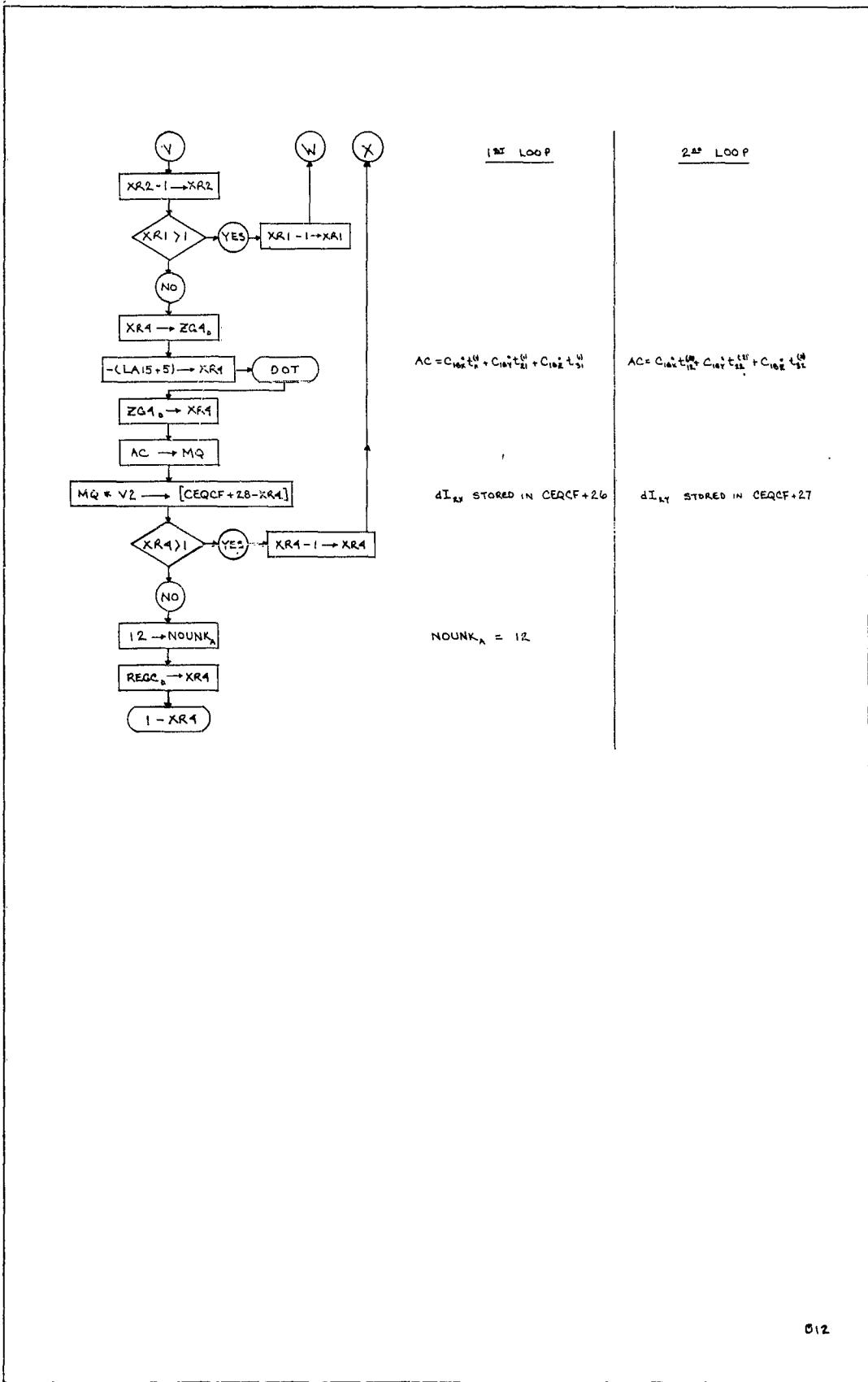
dI_H STORED IN CEQCF + 25

1ST LOOP

$t_{12}^{(i)}$ TRANSFERRED TO TEMP
 $t_{22}^{(i)}$ " " TEMP + 1
 $t_{32}^{(i)}$ " " TEMP + 2

2ND LOOP

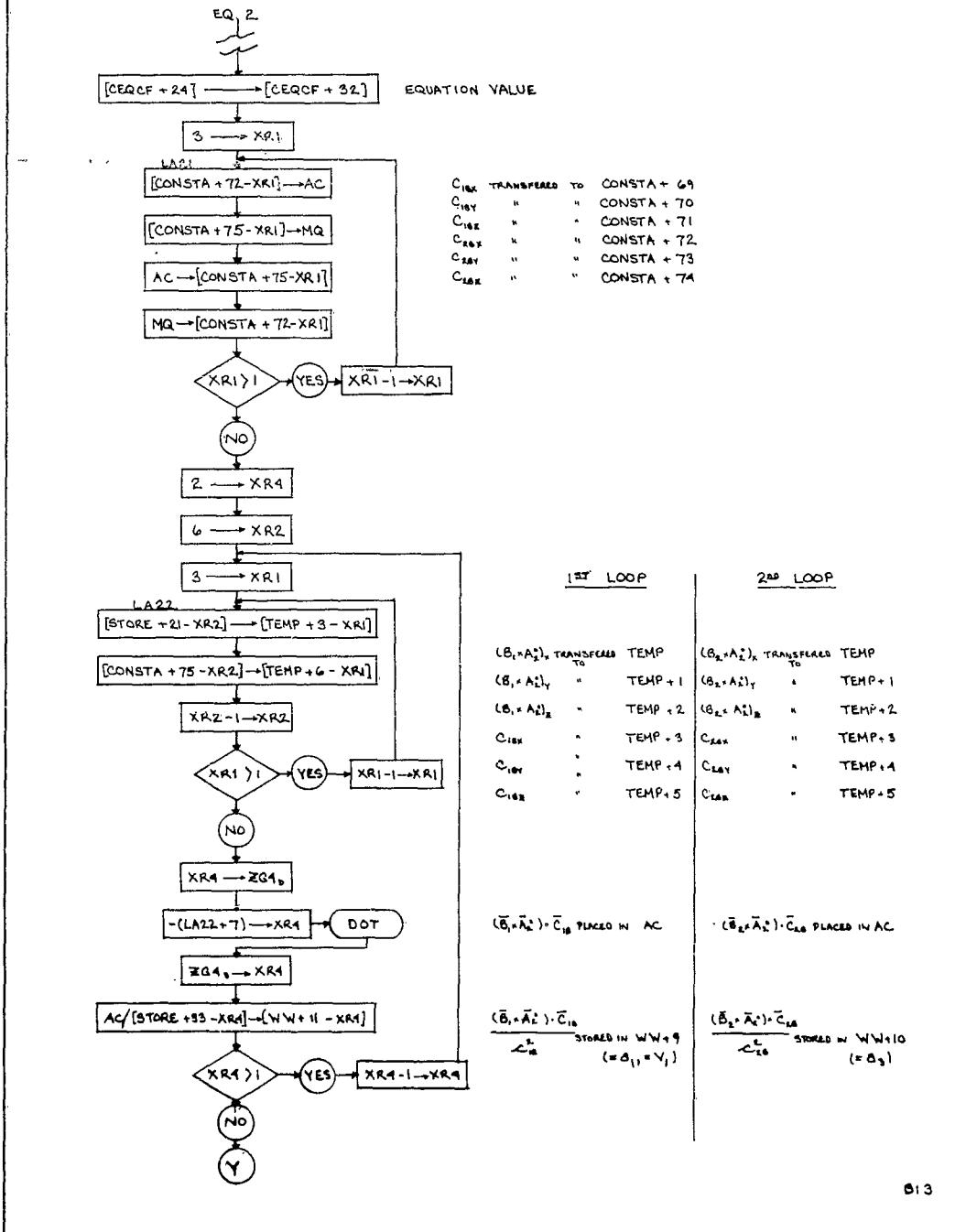
$t_{12}^{(i)}$ TRANSFERRED TO TEMP
 $t_{22}^{(i)}$ " " TEMP + 1
 $t_{32}^{(i)}$ " " TEMP + 2

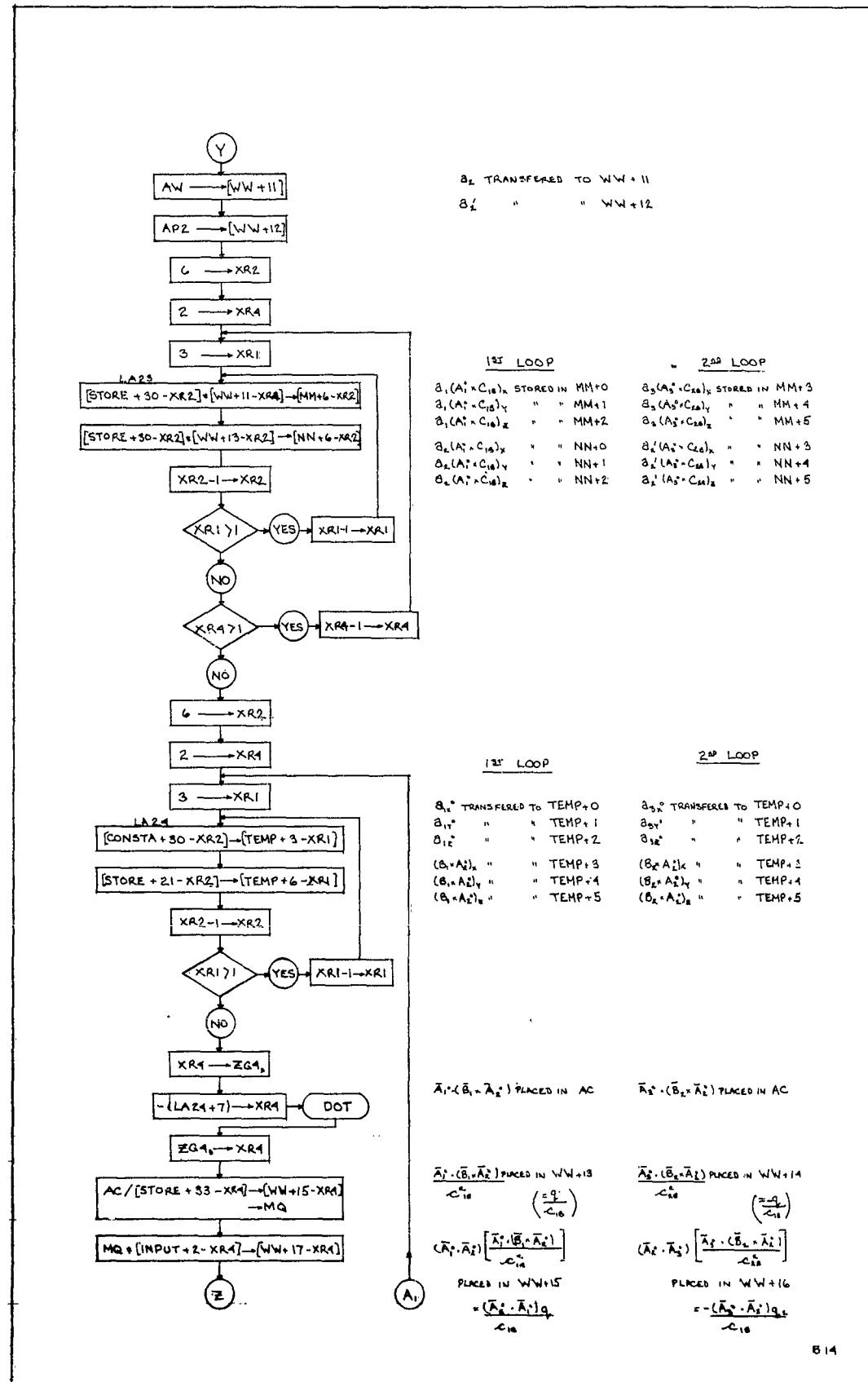


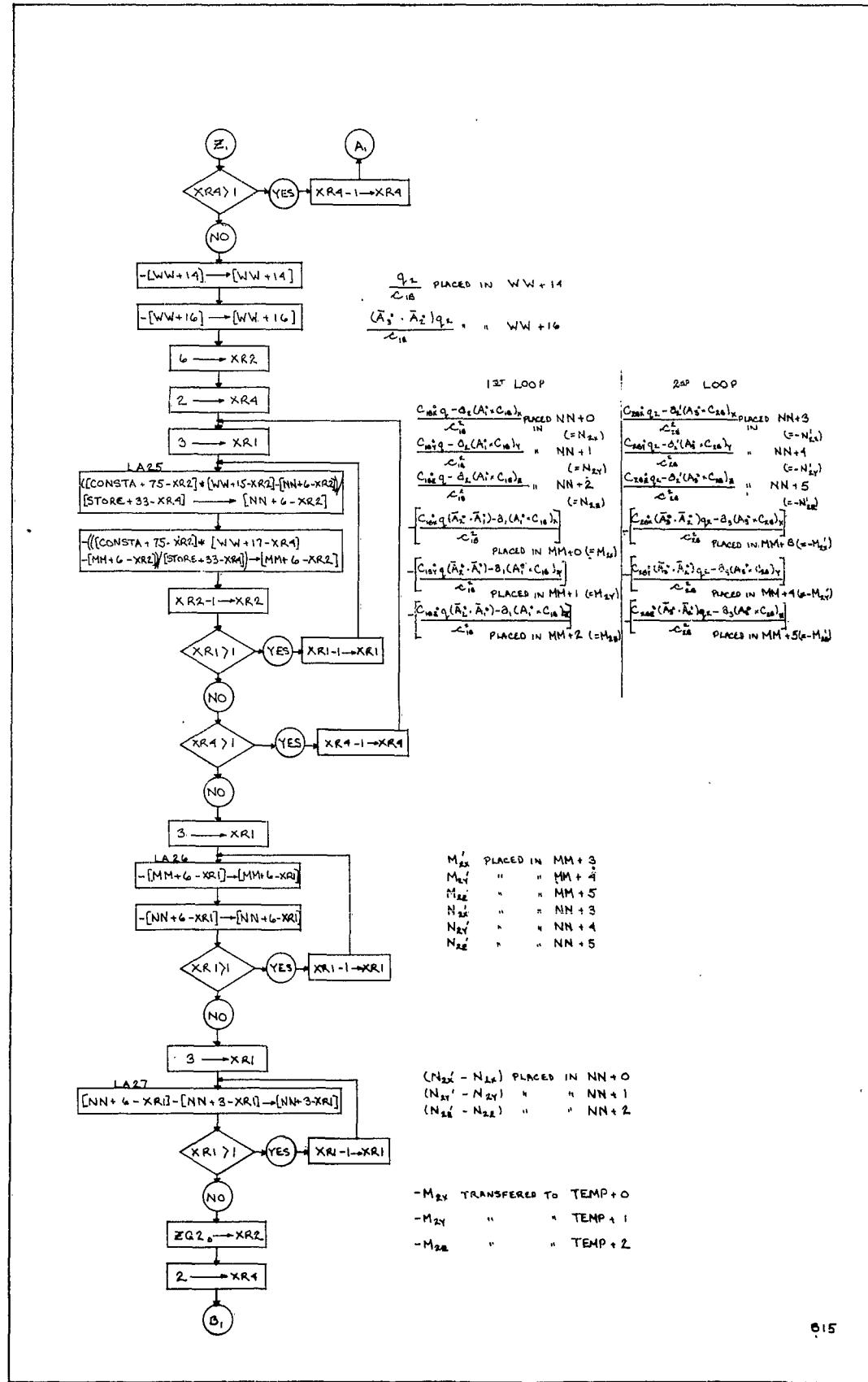
ADDITIONS TO EQ 2

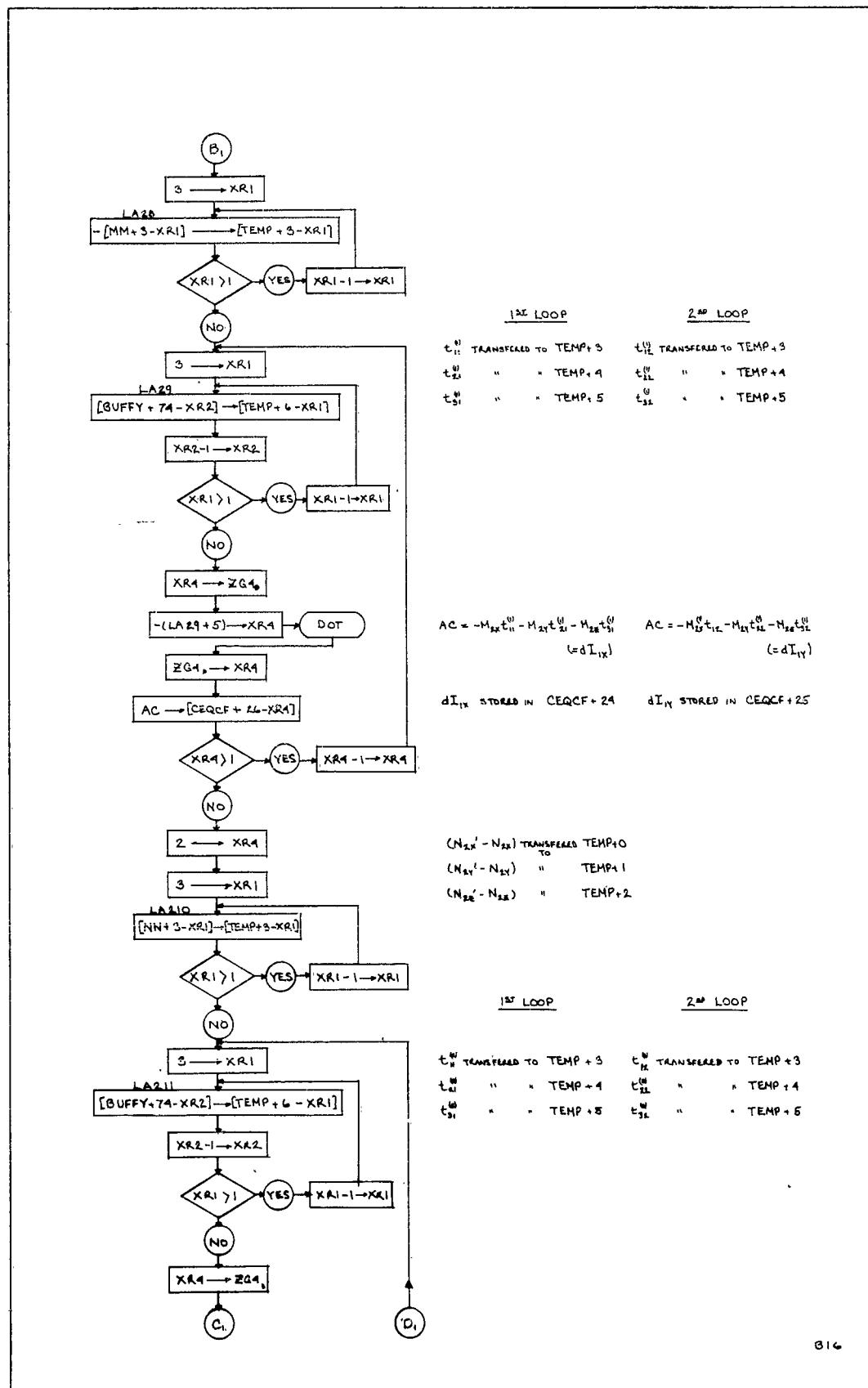
SQNO	1,3	1,2,3,5*
ZG2 ₀	36	18
SQNOA	15	9

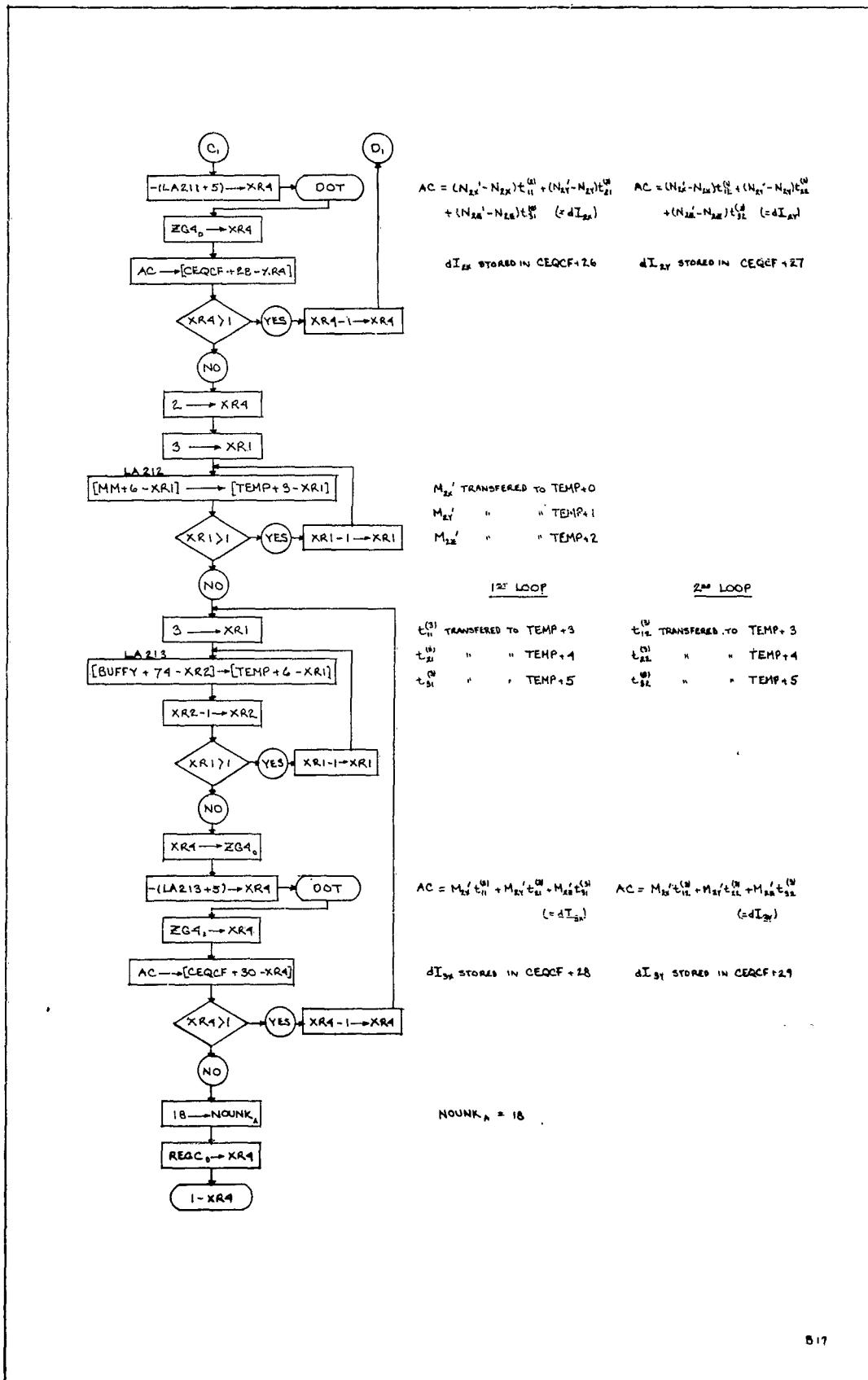
} FROM CALLING SEQUENCE FOR EQ 1 (1ST PAIRS)





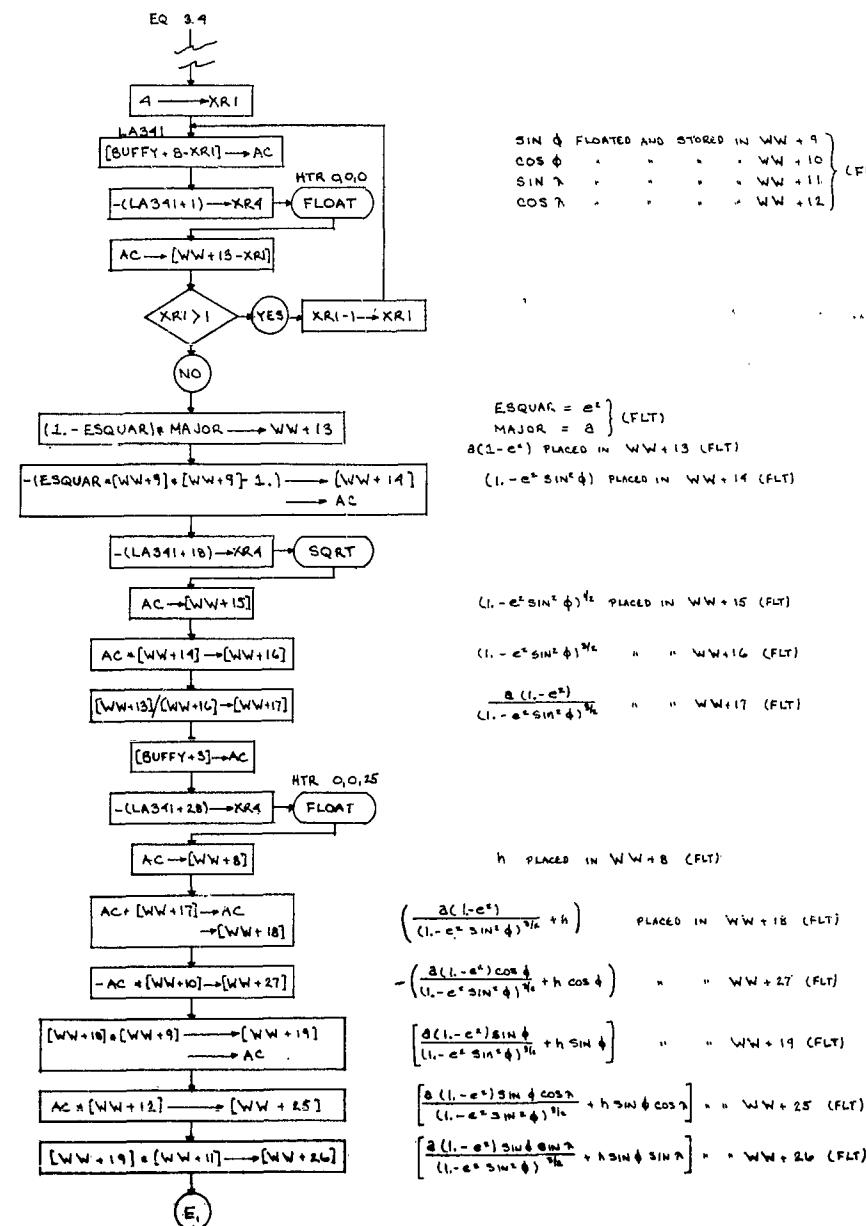


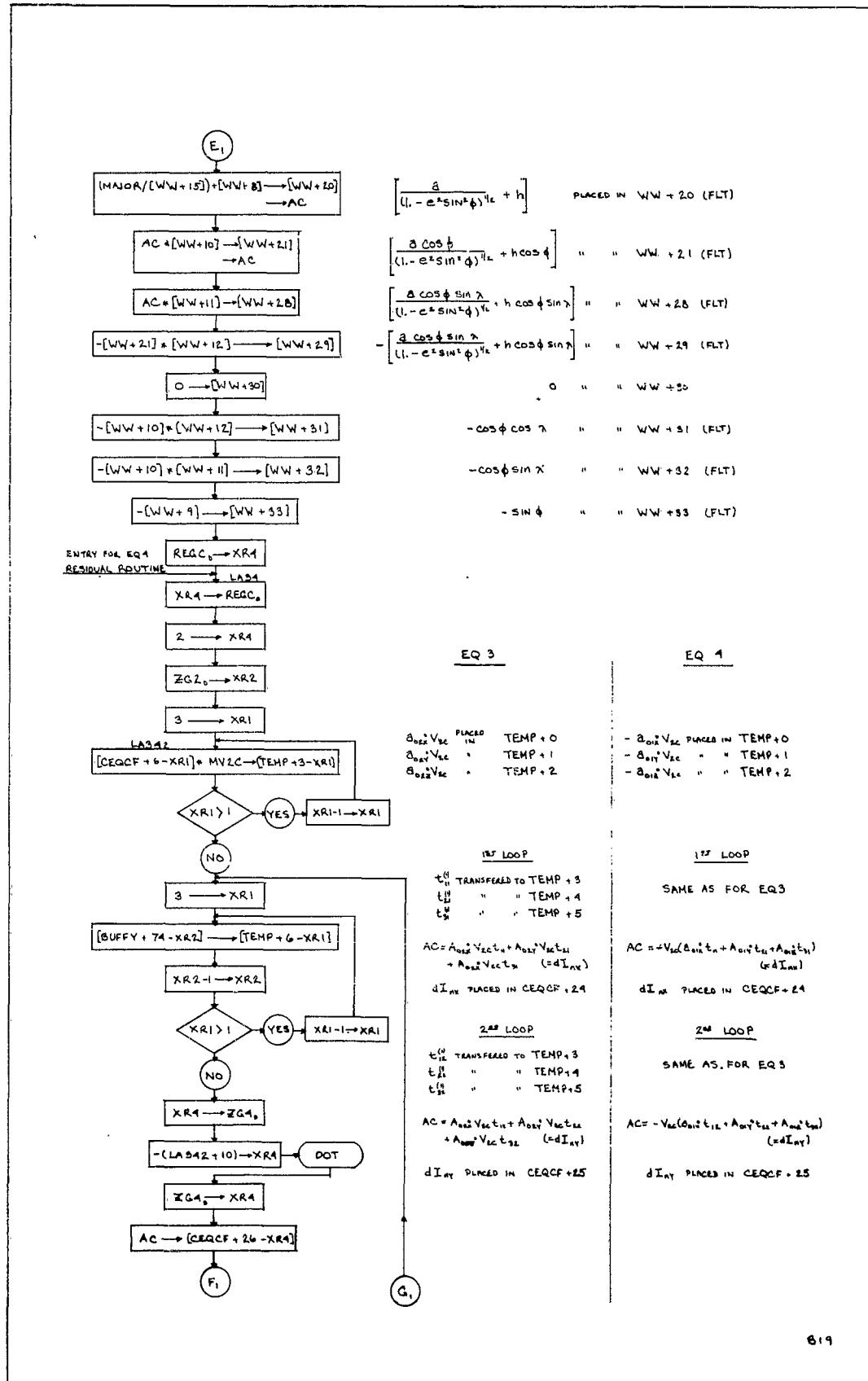


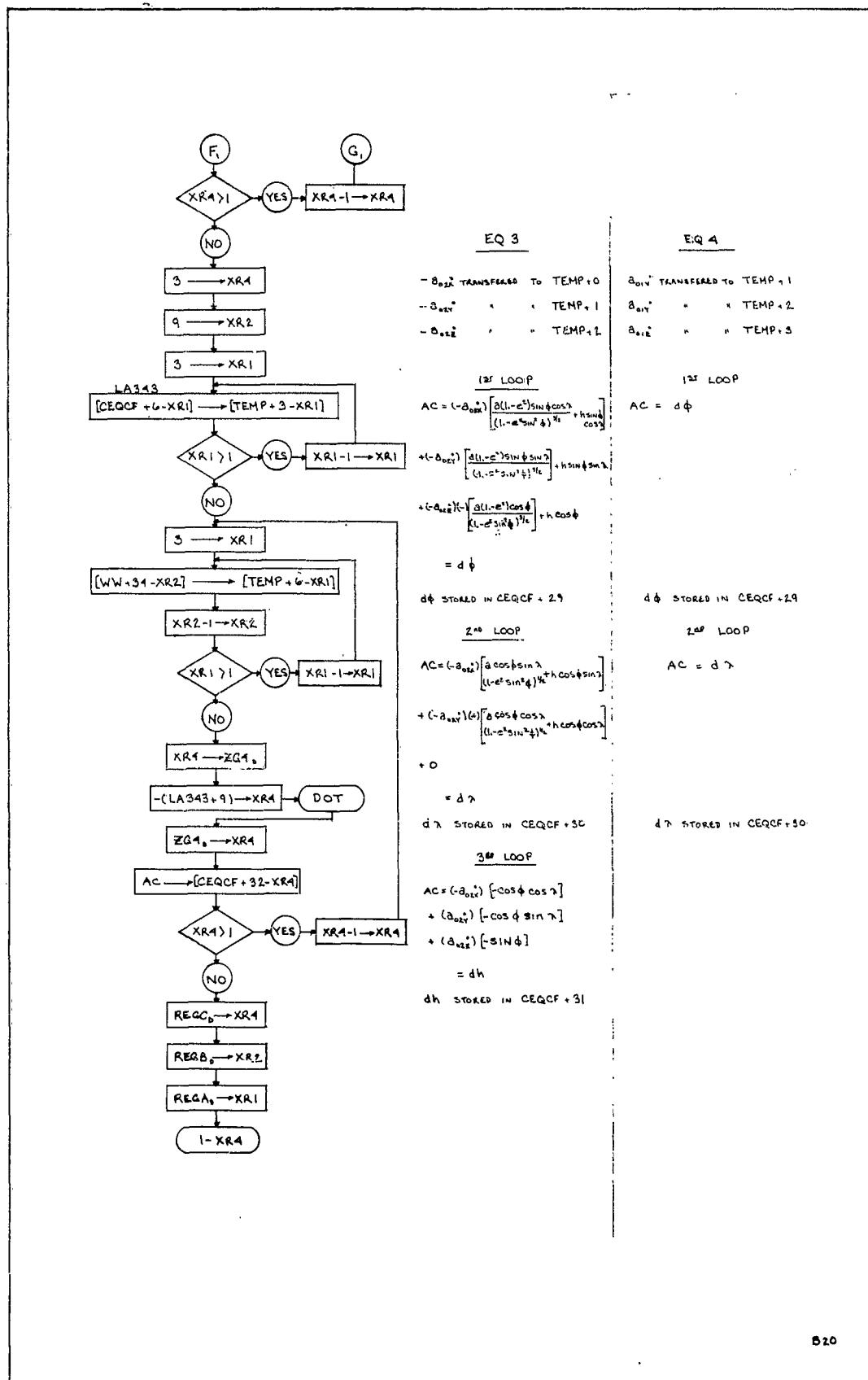


ADDITIONS TO EQ3 & EQ4

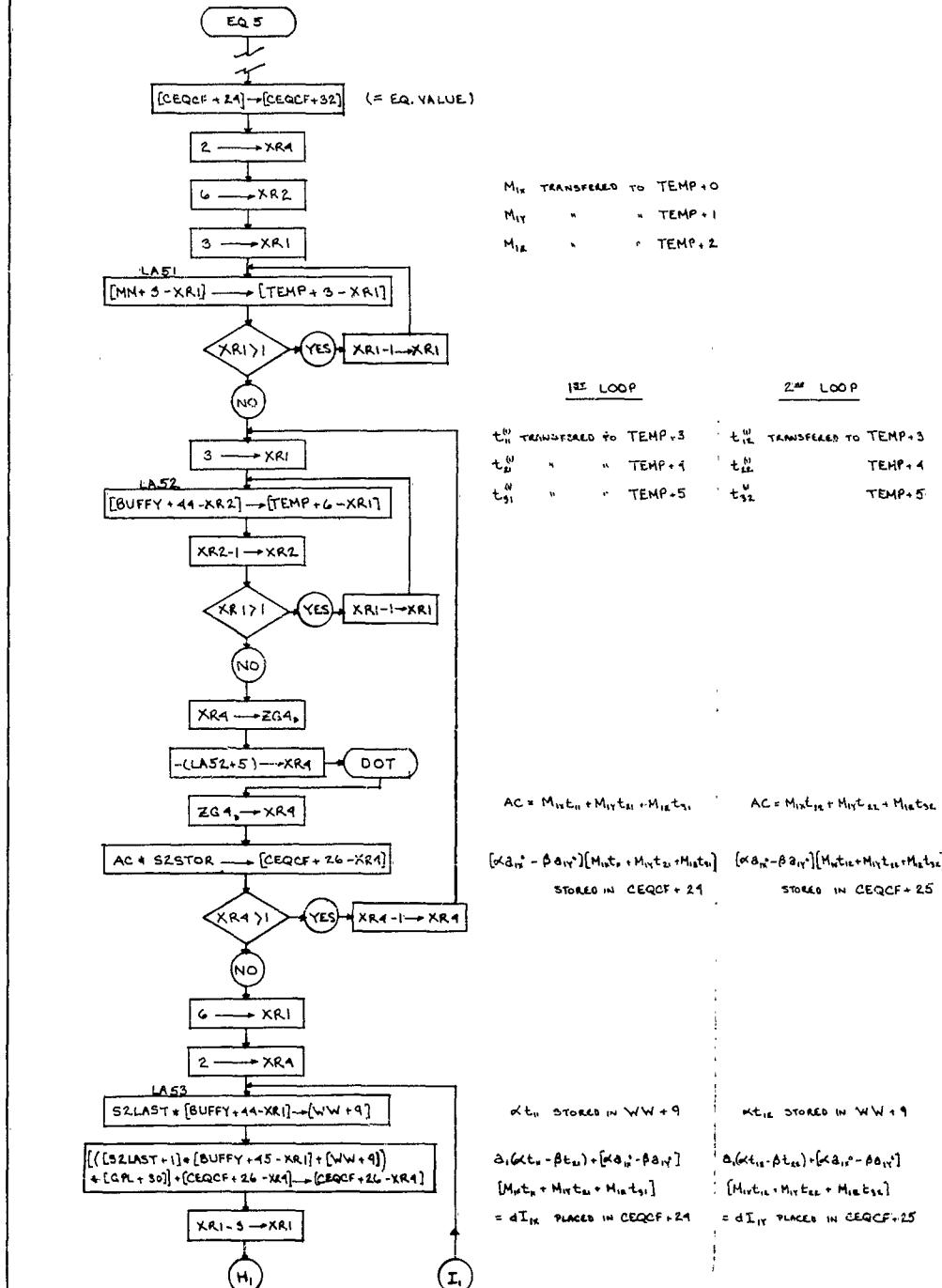
IN CALLING SEQUENCE						
PHOTO	1	2	3	1*	2*	3*
SQNO	36	30	24	18	12	6
EG2	36	30	24	18	12	6
SQNOA	15	13	11	9	7	5
NOUNK	6	6	6	6	6	6

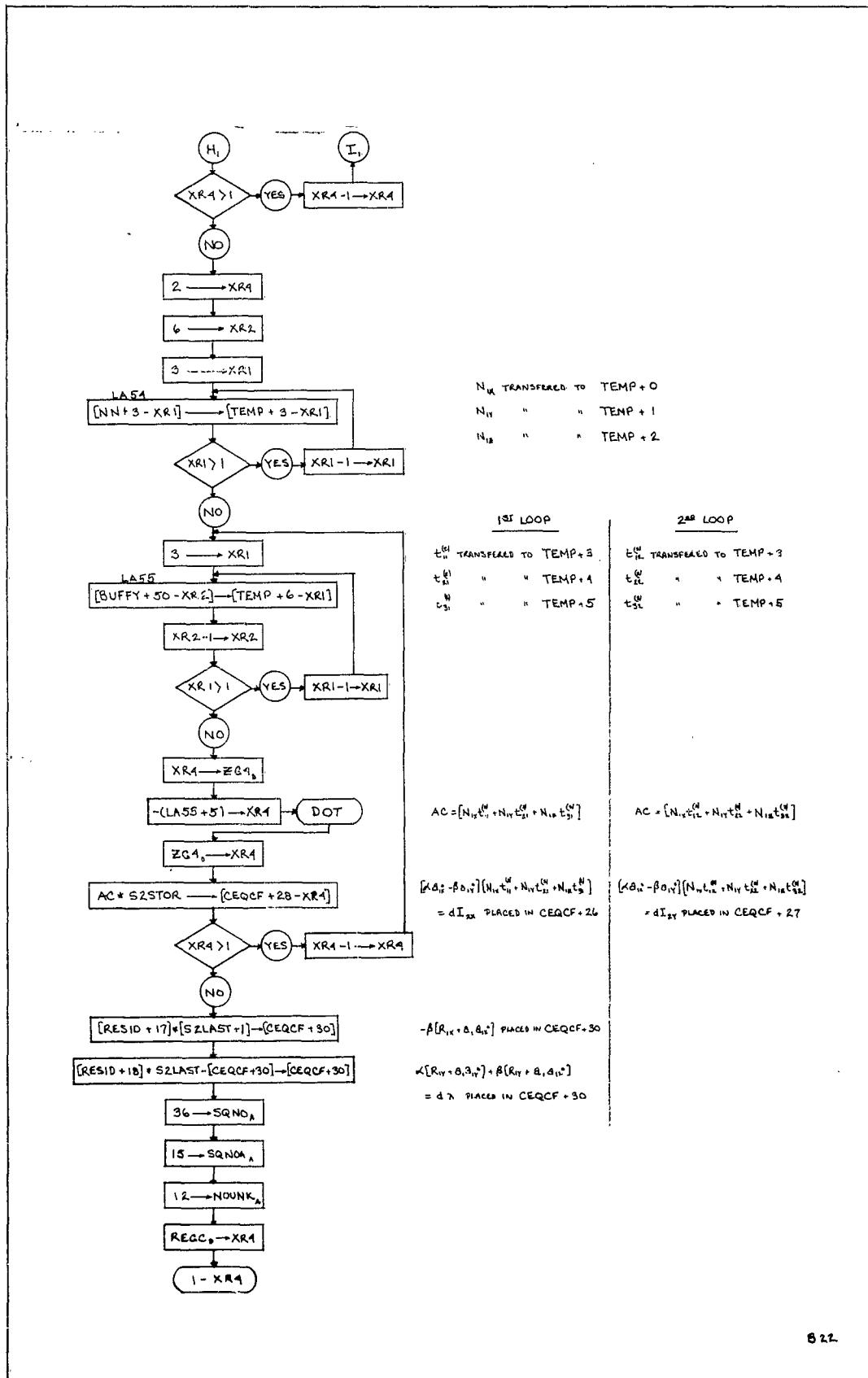




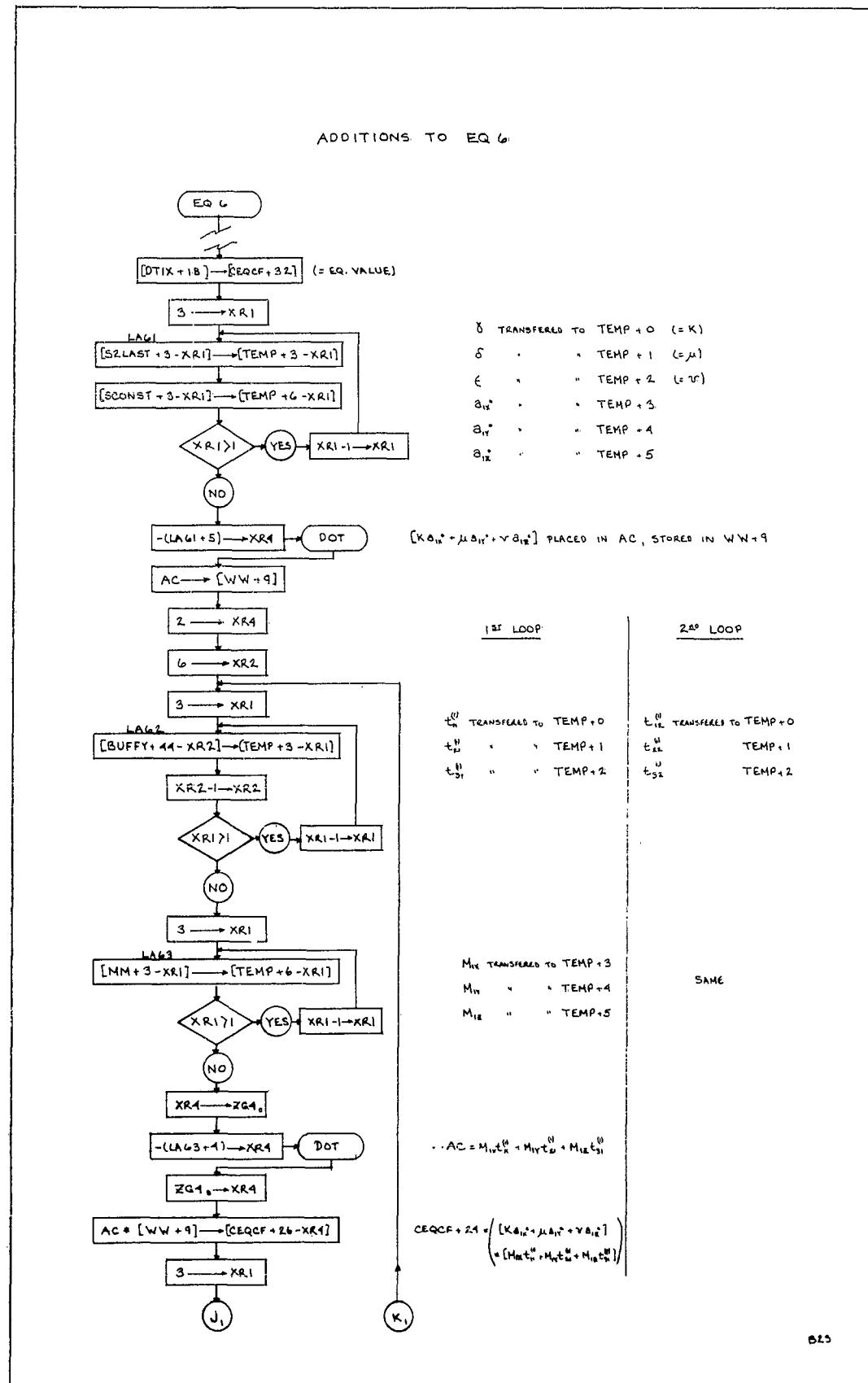


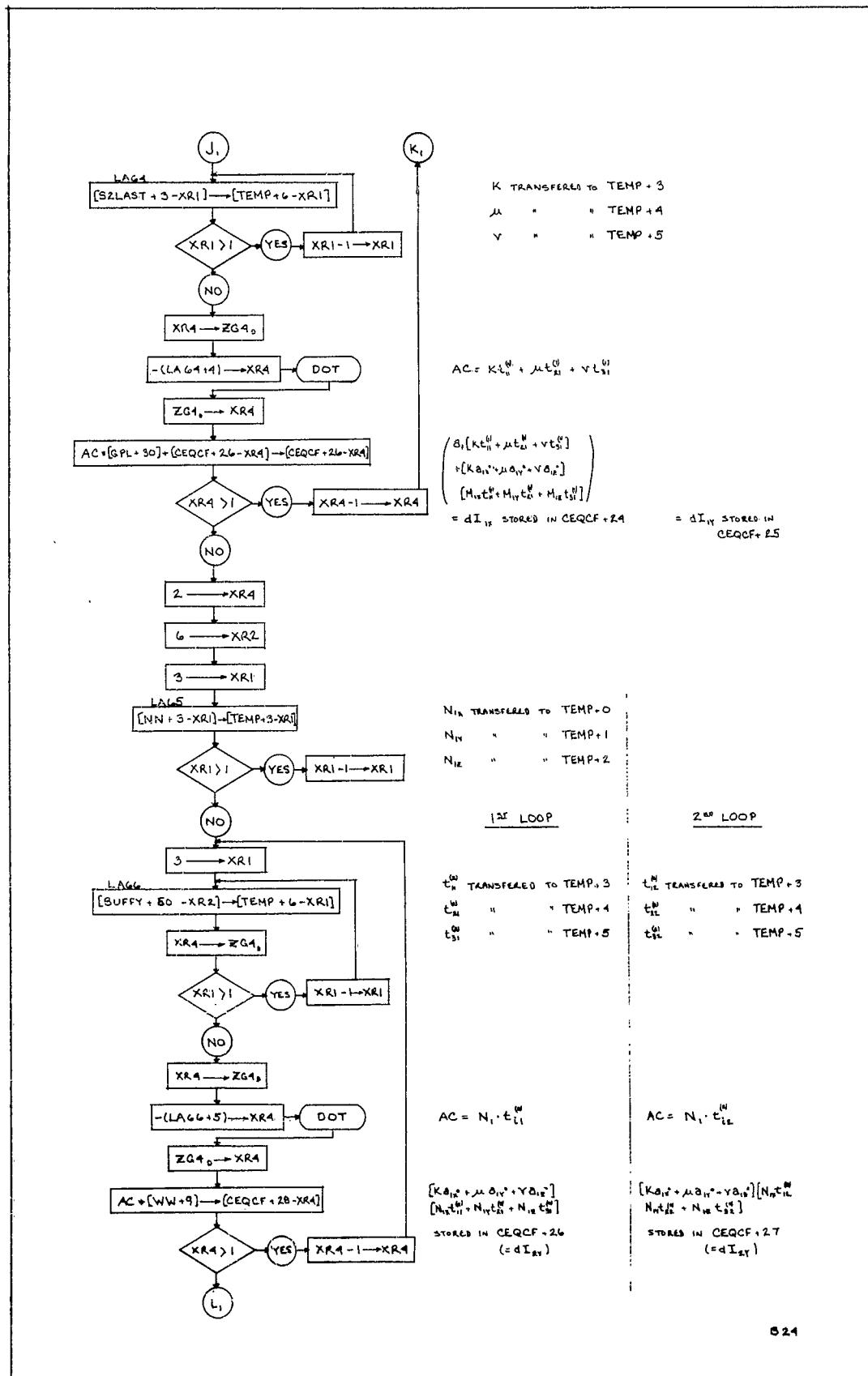
ADDITIONS TO EQ5

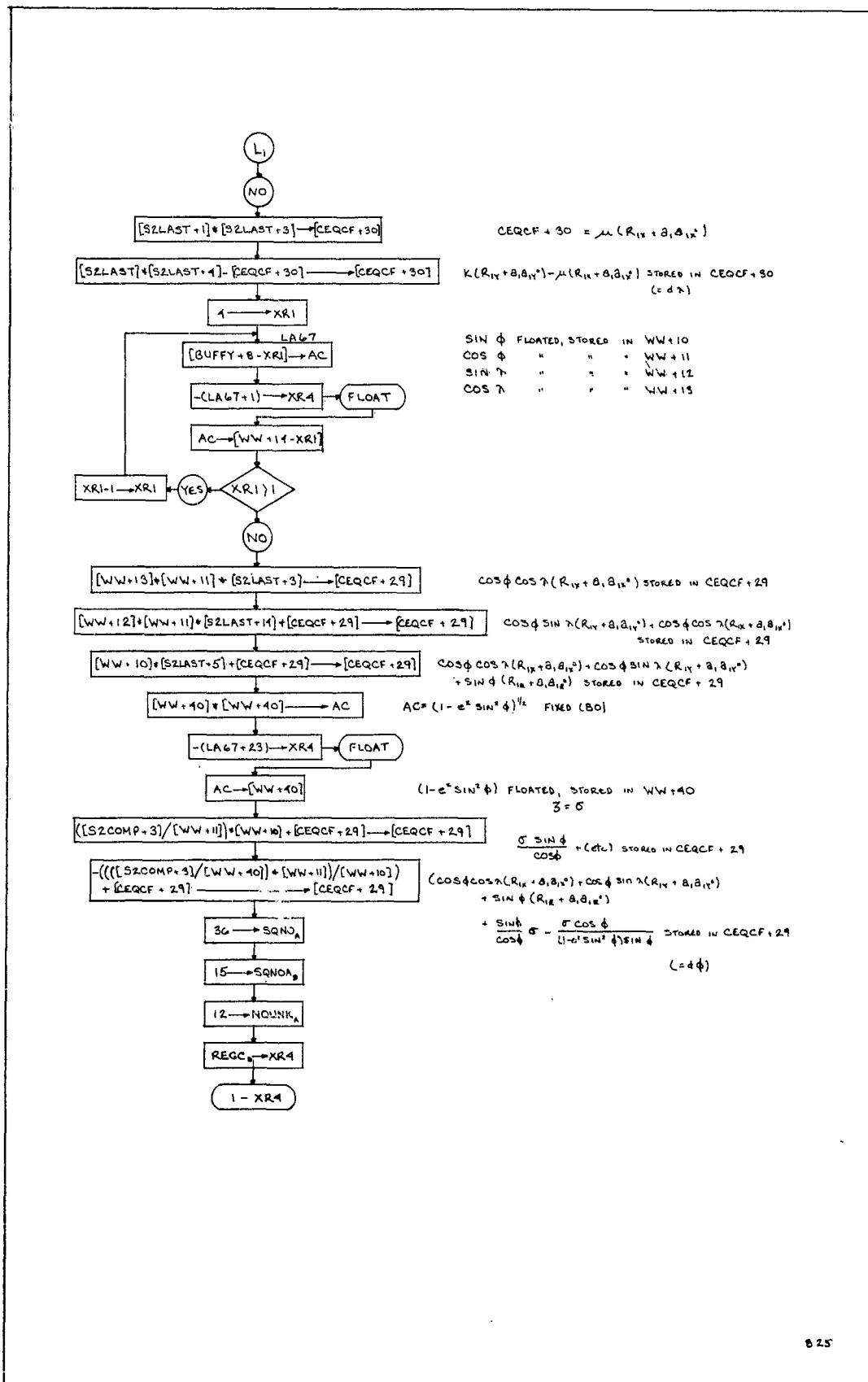


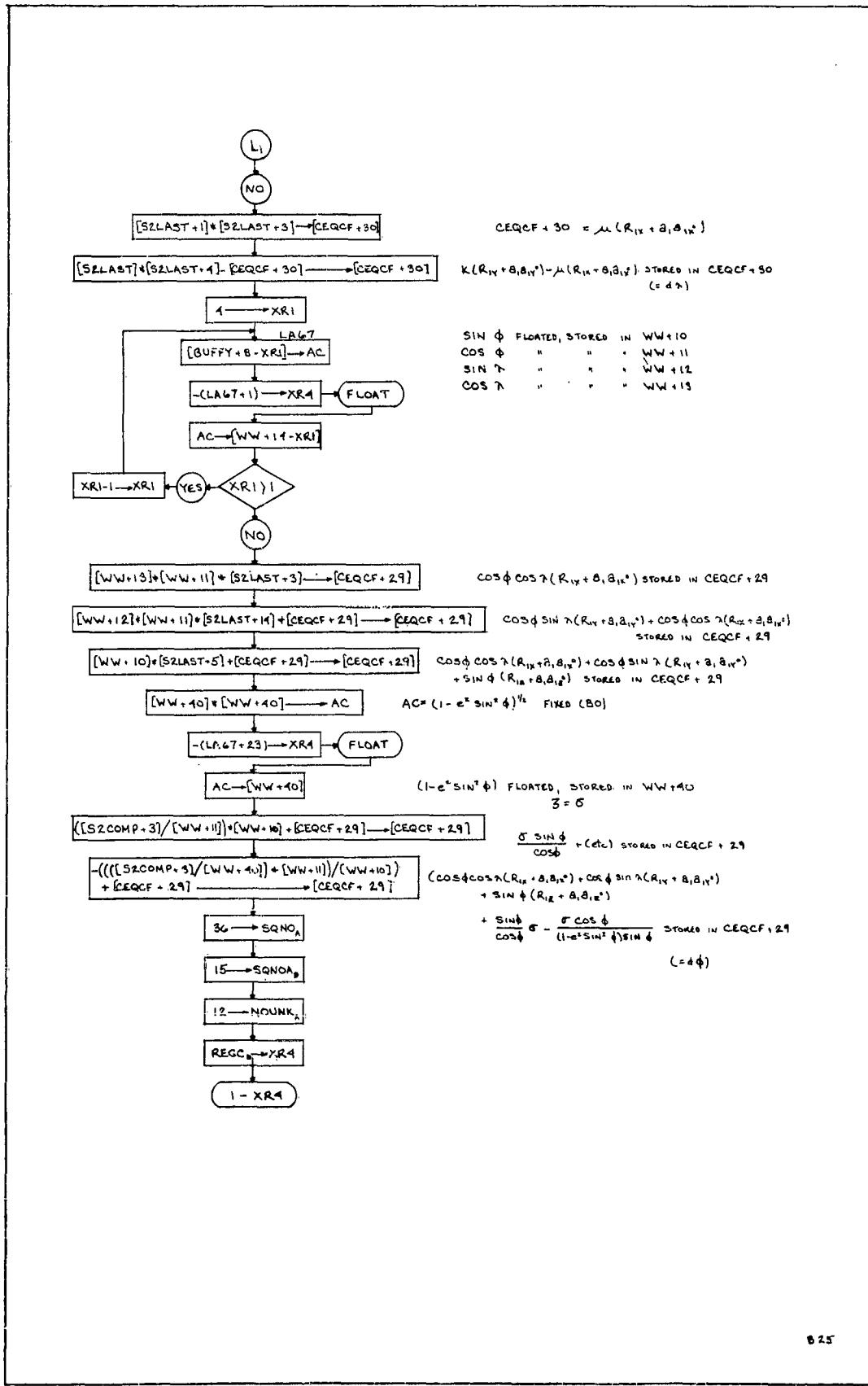


ADDITIONS TO EQ 6

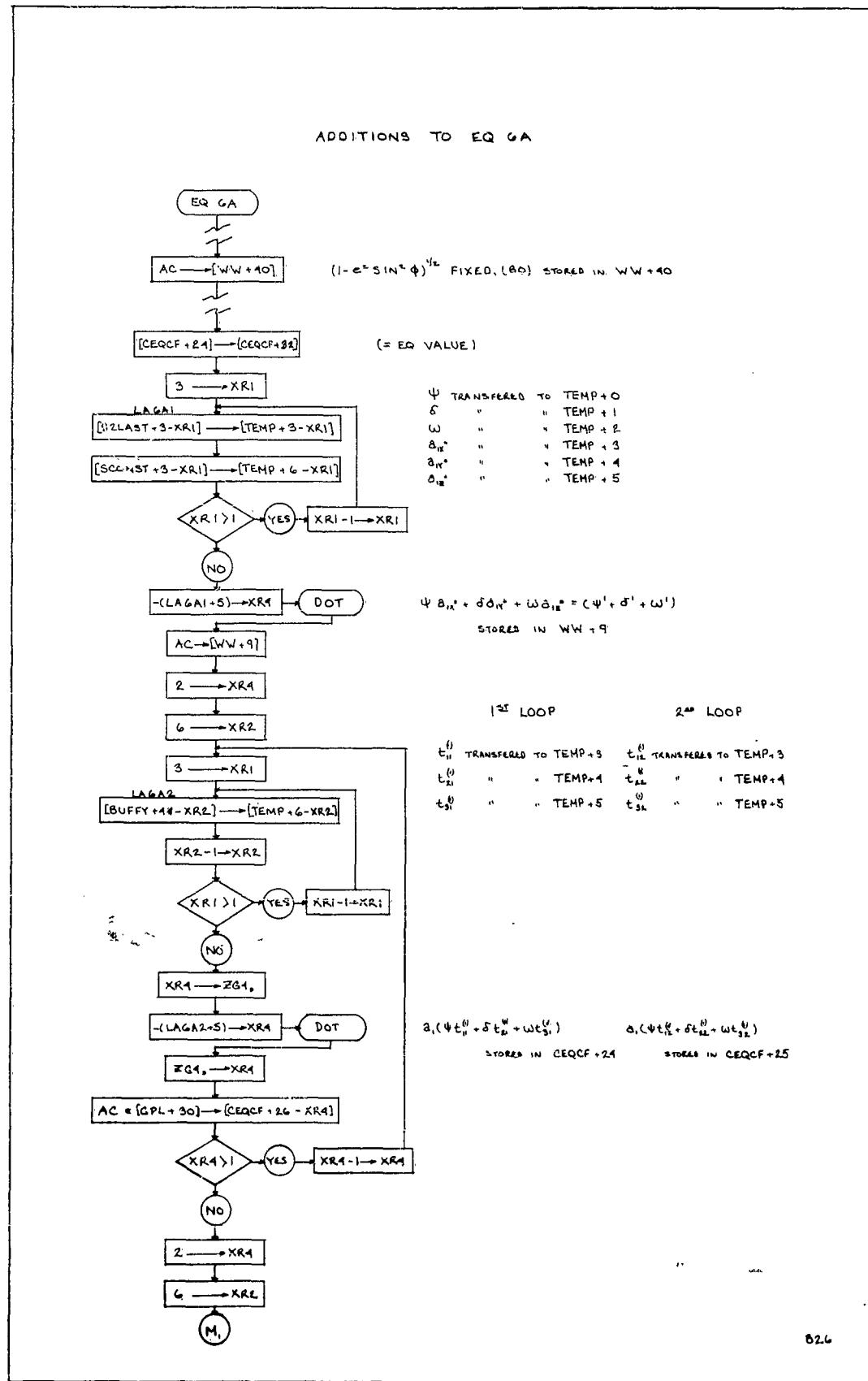


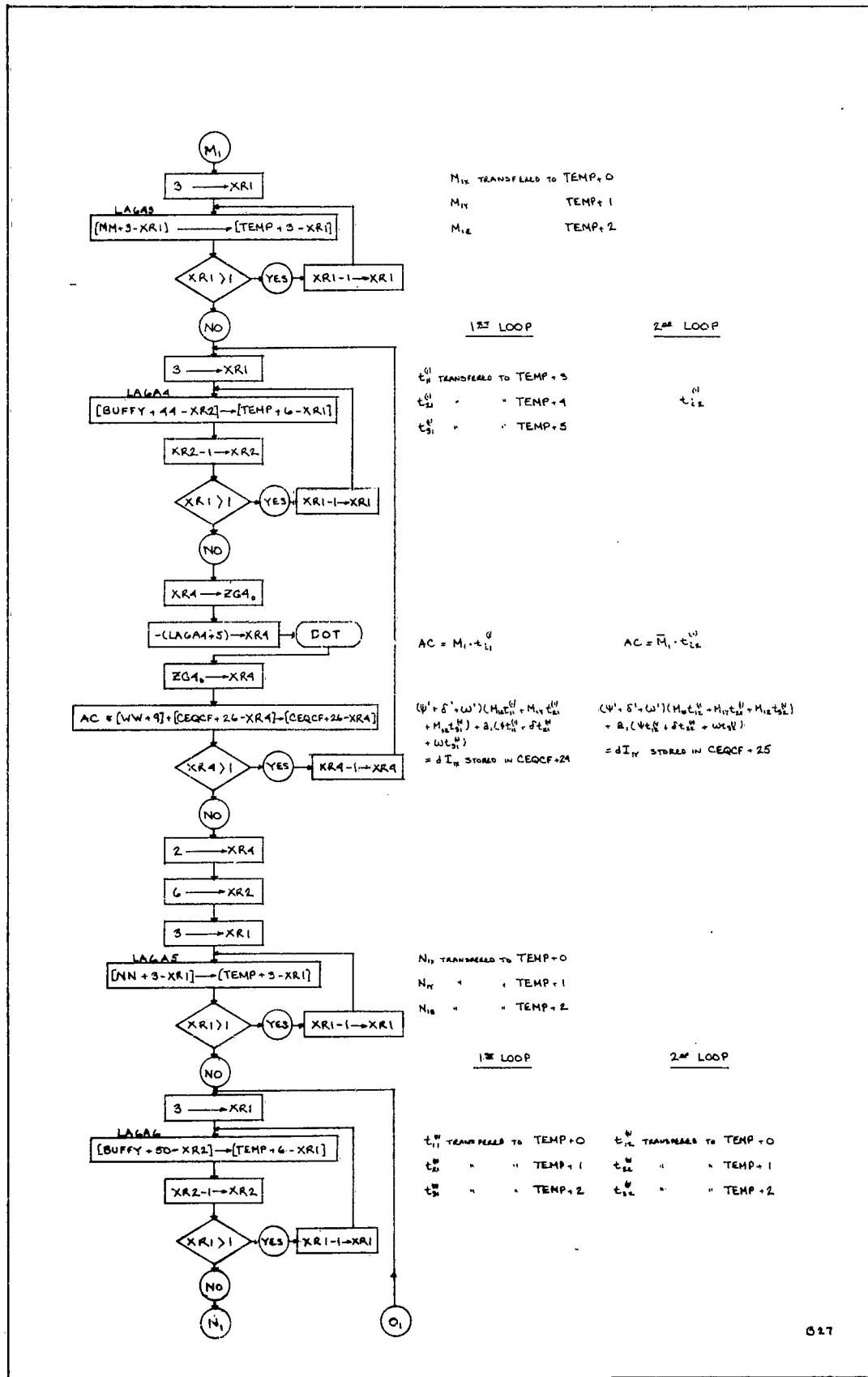


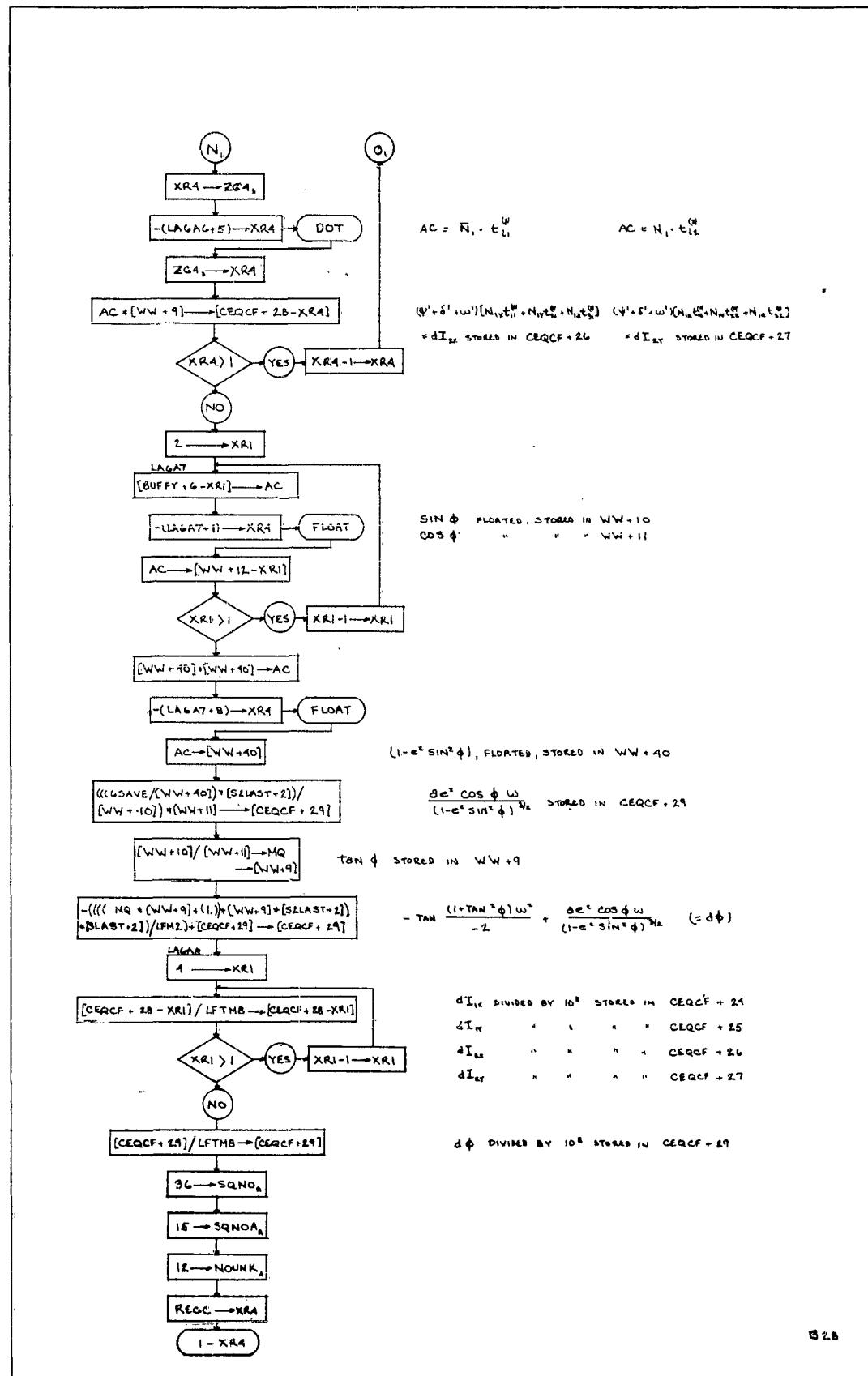




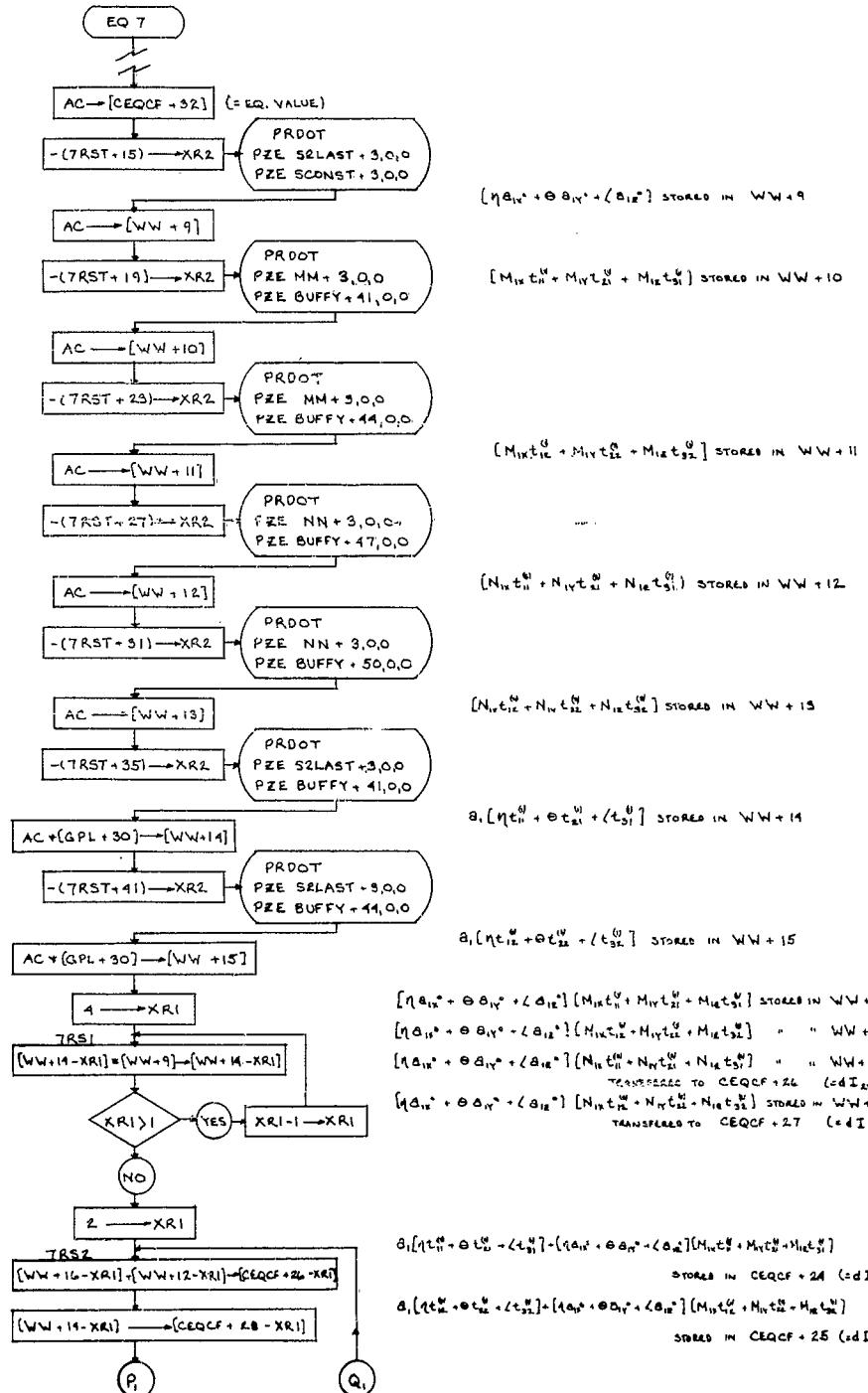
ADDITIONS TO EQ GA

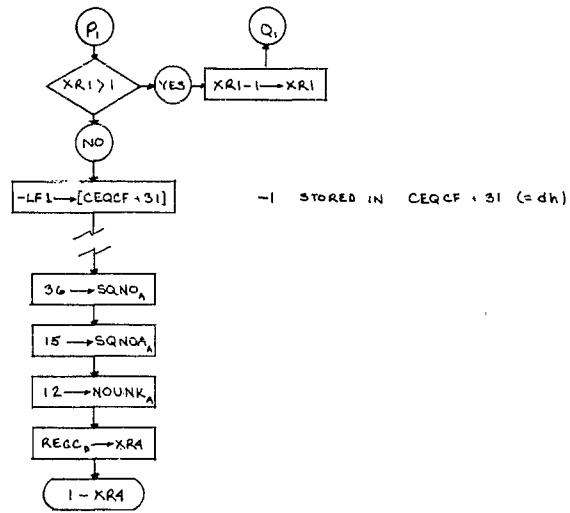




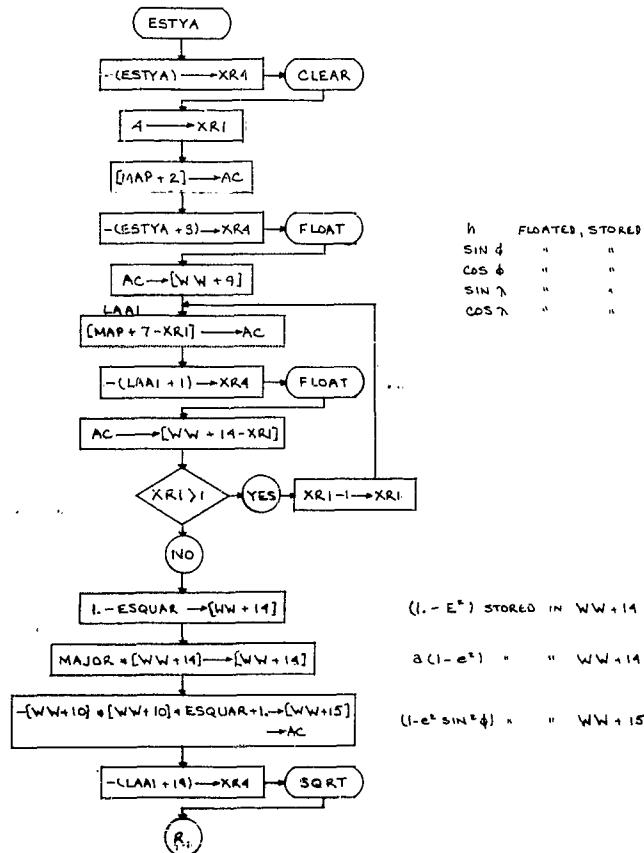


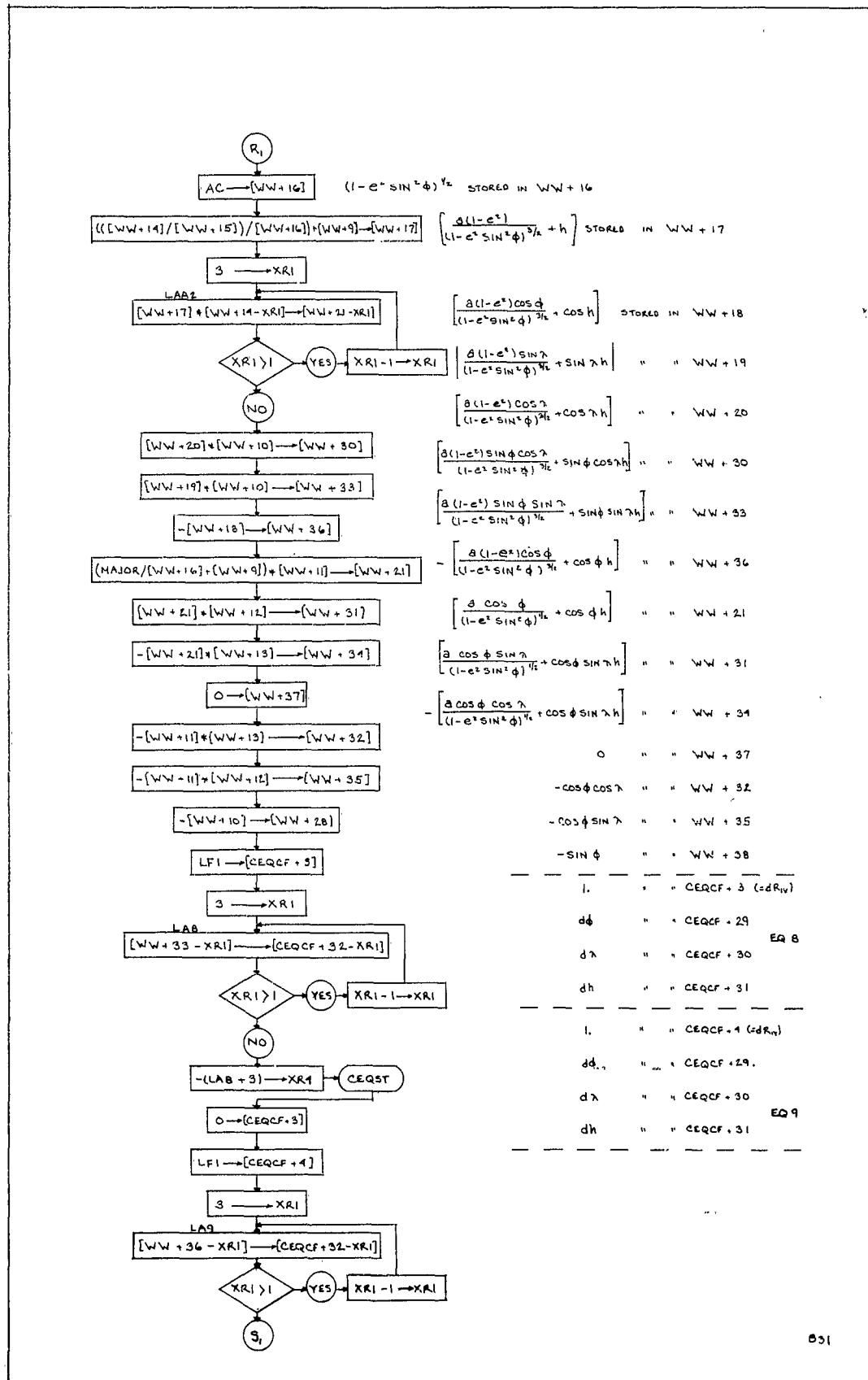
ADDITIONS TO EQ 7

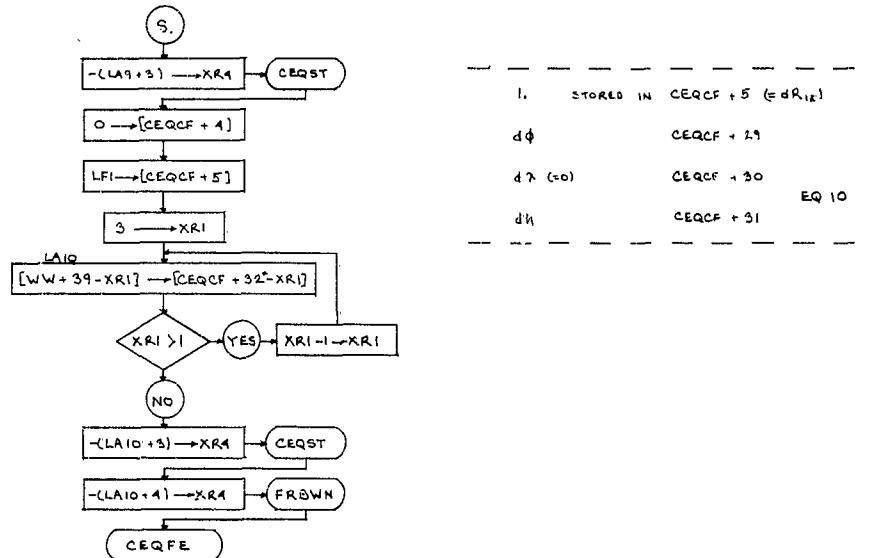




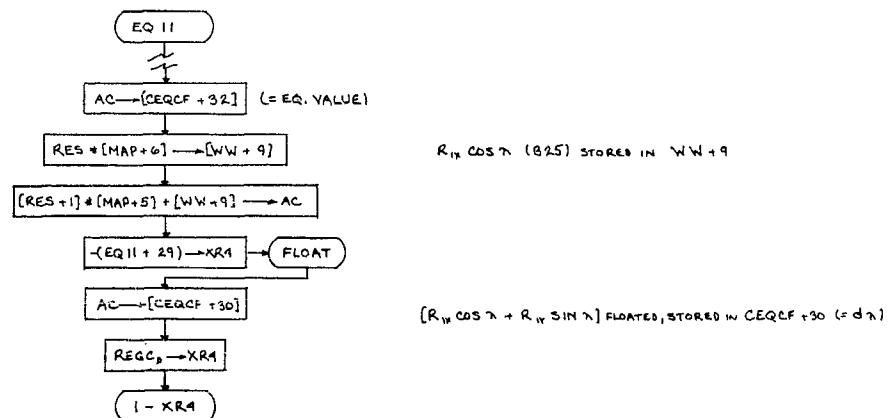
EQ 8, 9, 10



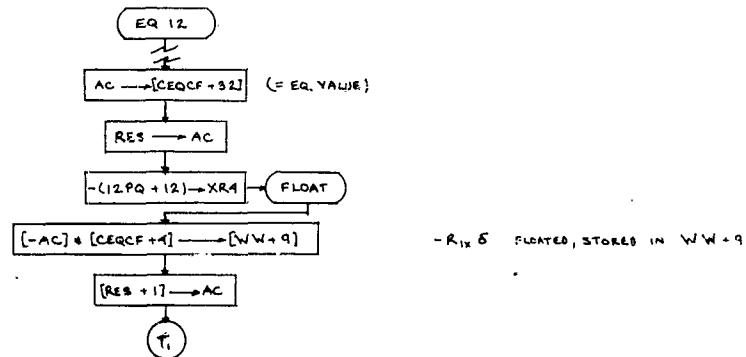


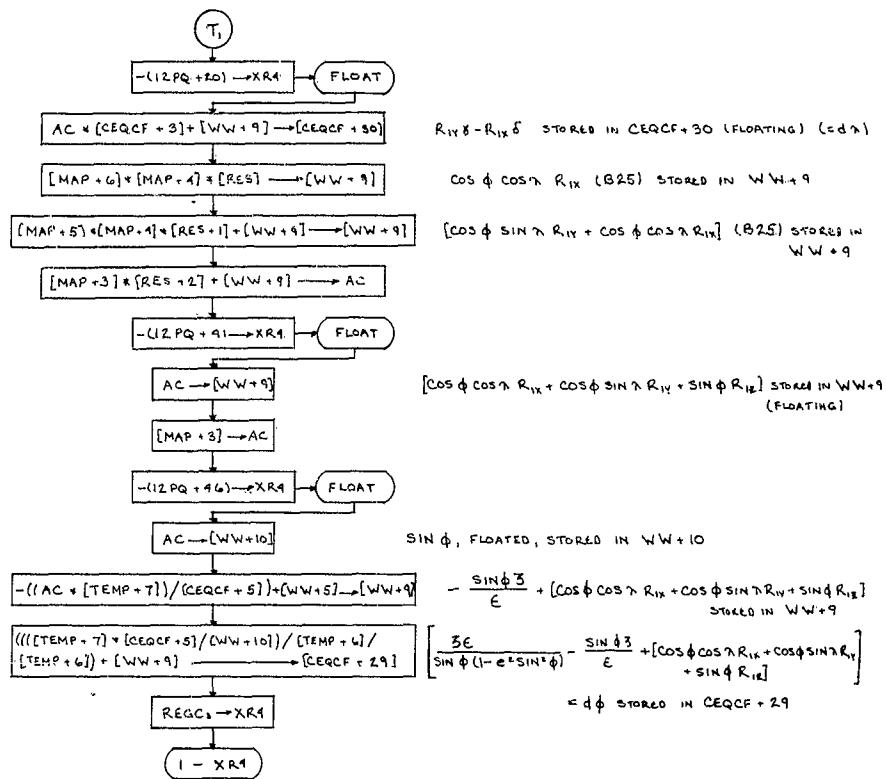


ADDITIONS TO EQ 11

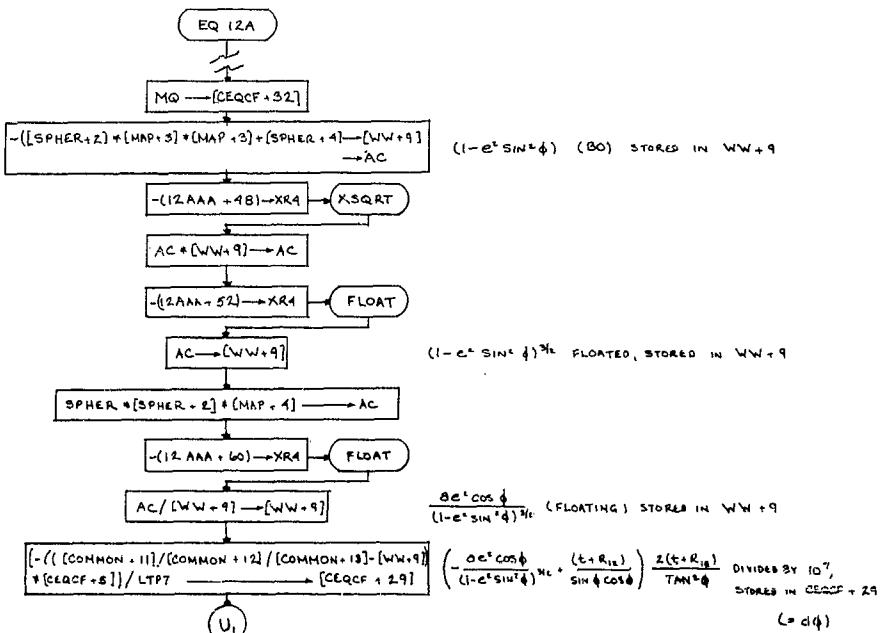


ADDITIONS TO EQ 12



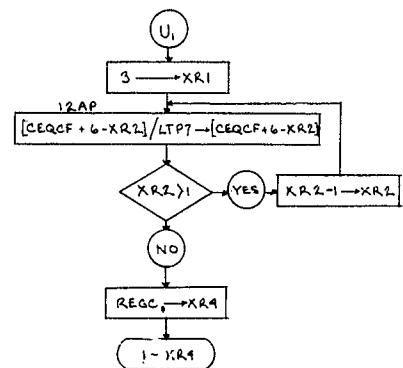


ADDITIONS TO EQ 12A



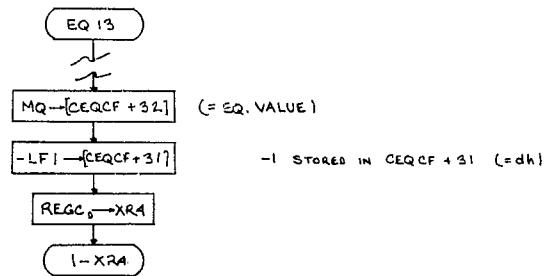
$(= d\phi)$

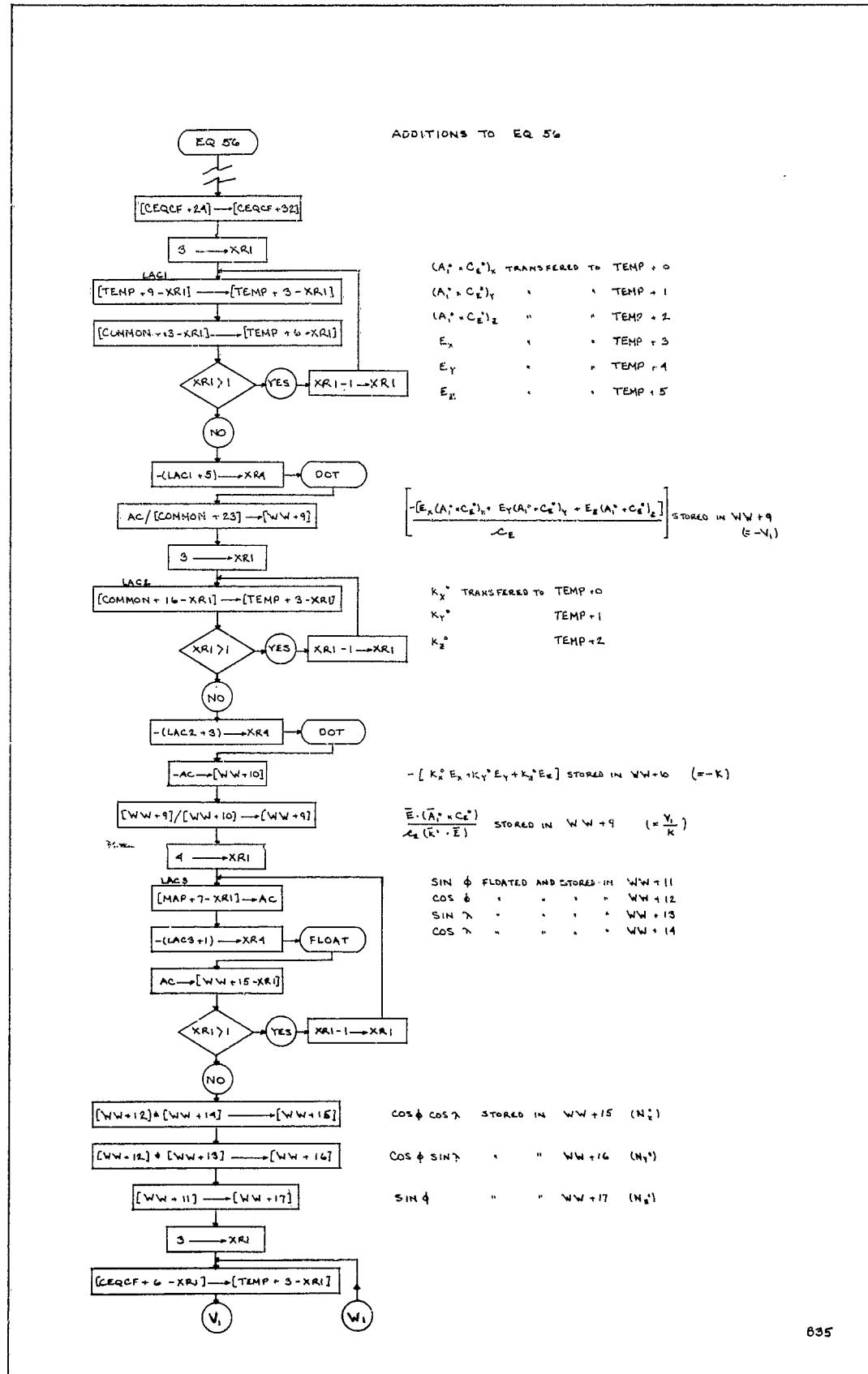
833

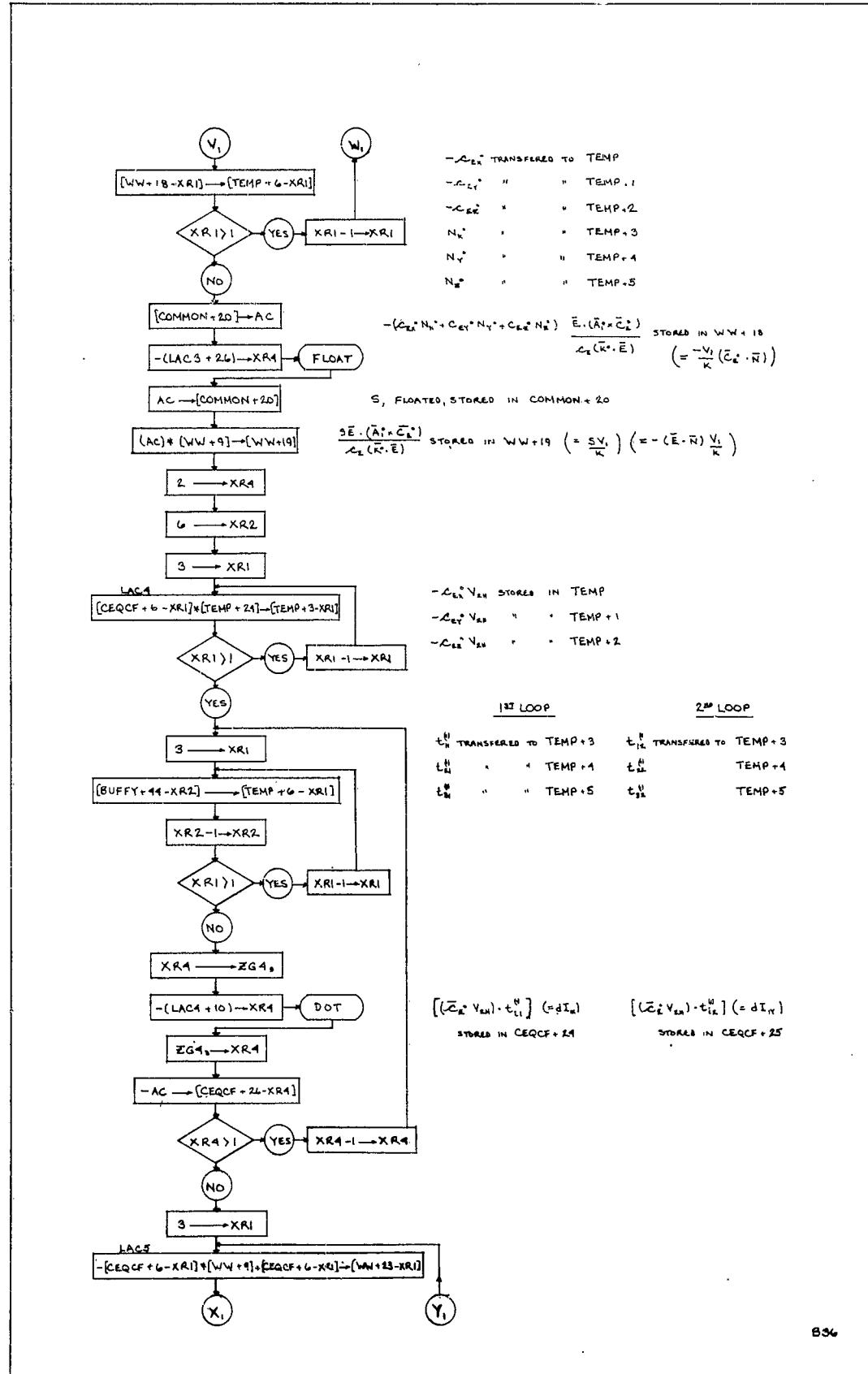


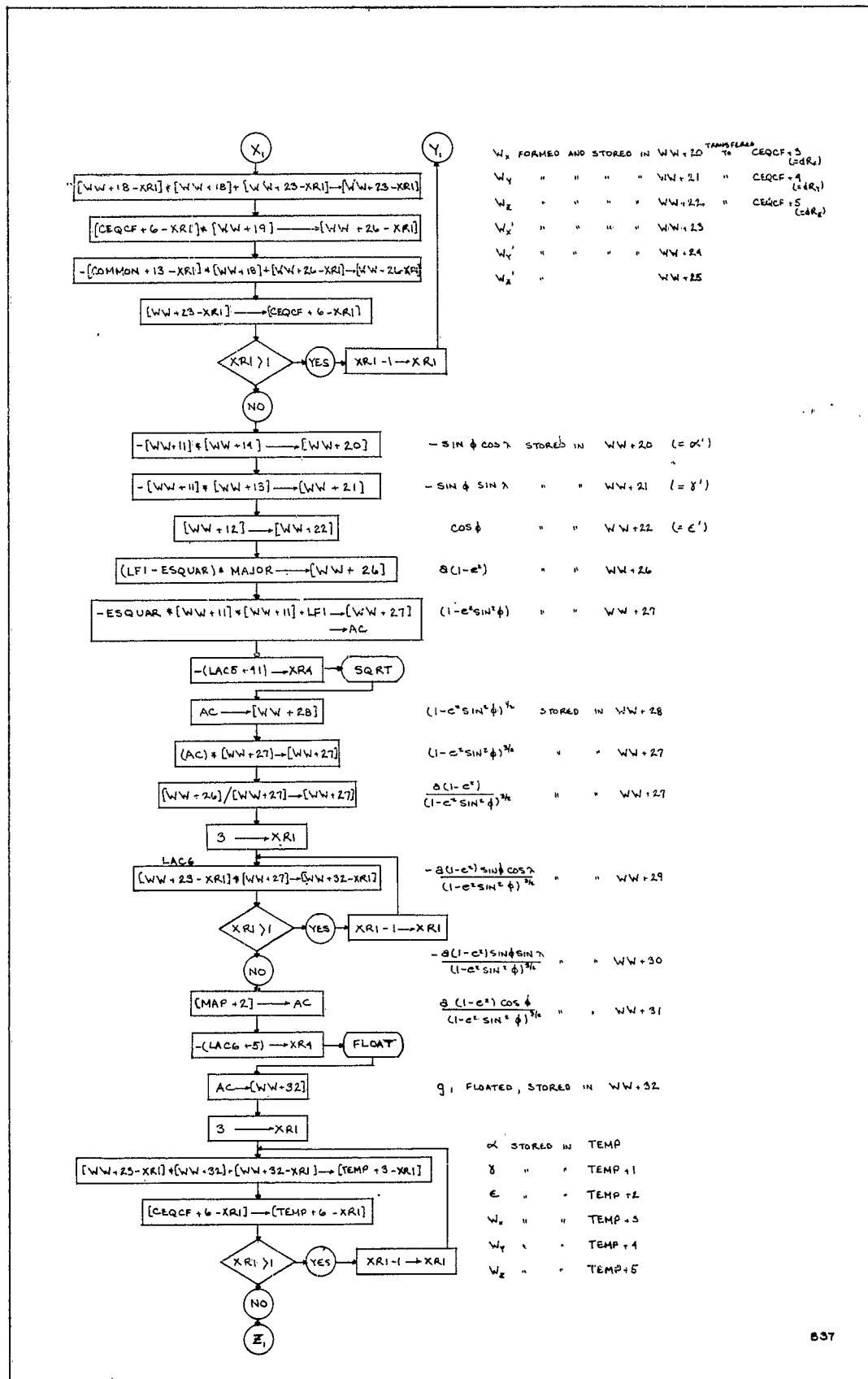
dR_{1x} DIVIDED BY 10^7 , STORED IN CEQCF + 3
 dR_{1y} " " " " CEQCF + 4
 dR_{1z} " " " " CEQCF + 5

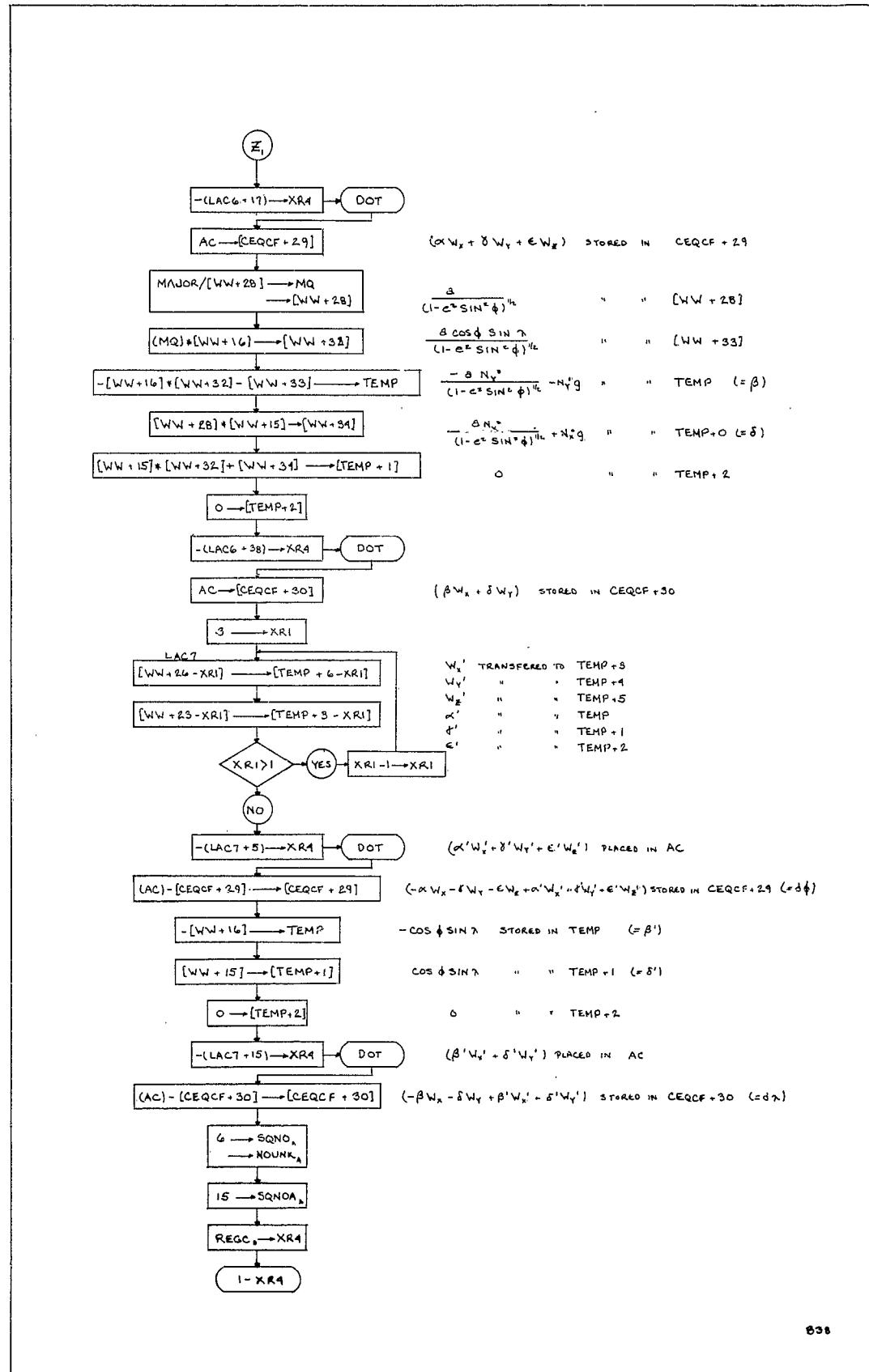
ADDITIONS TO EQ 13

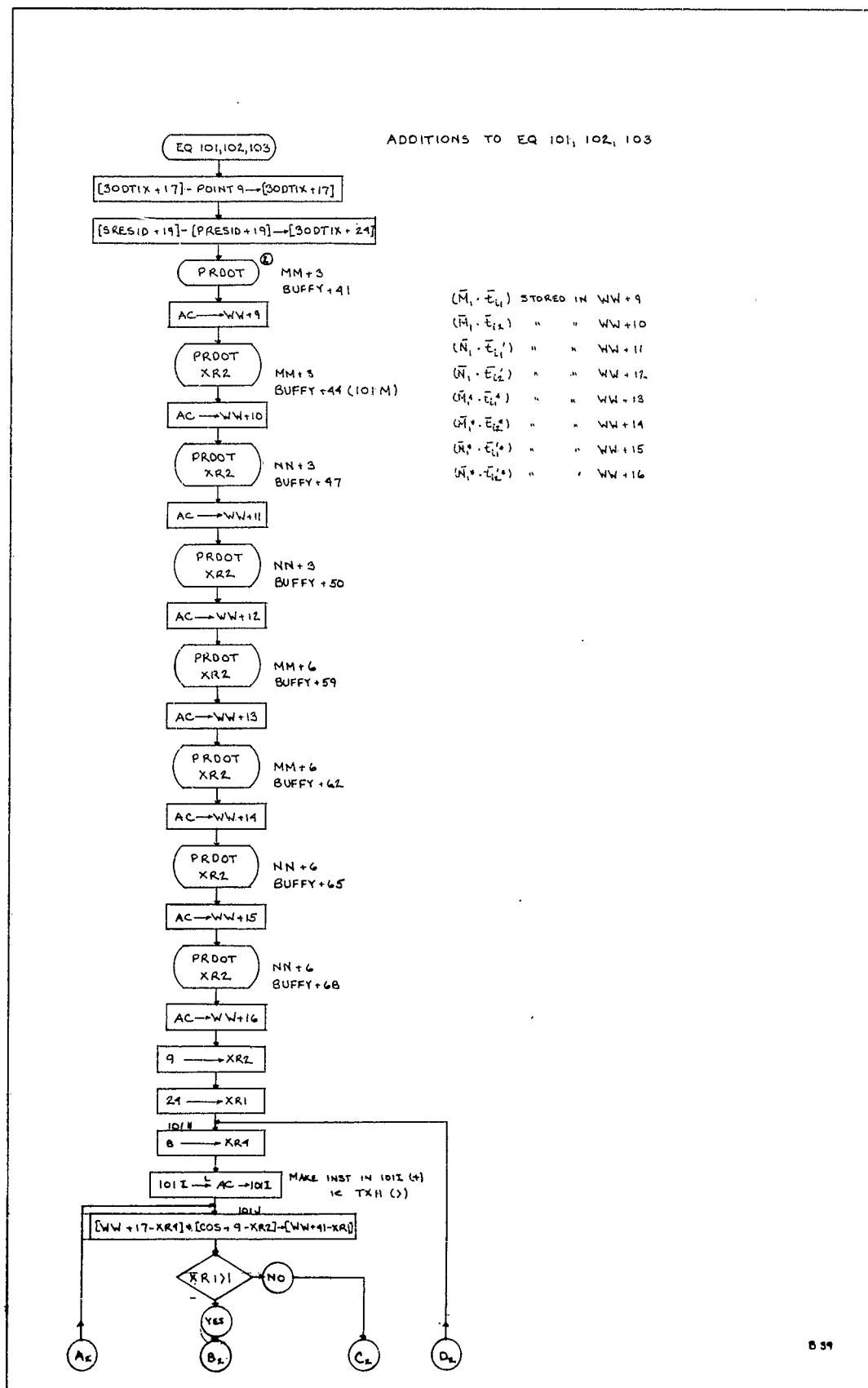


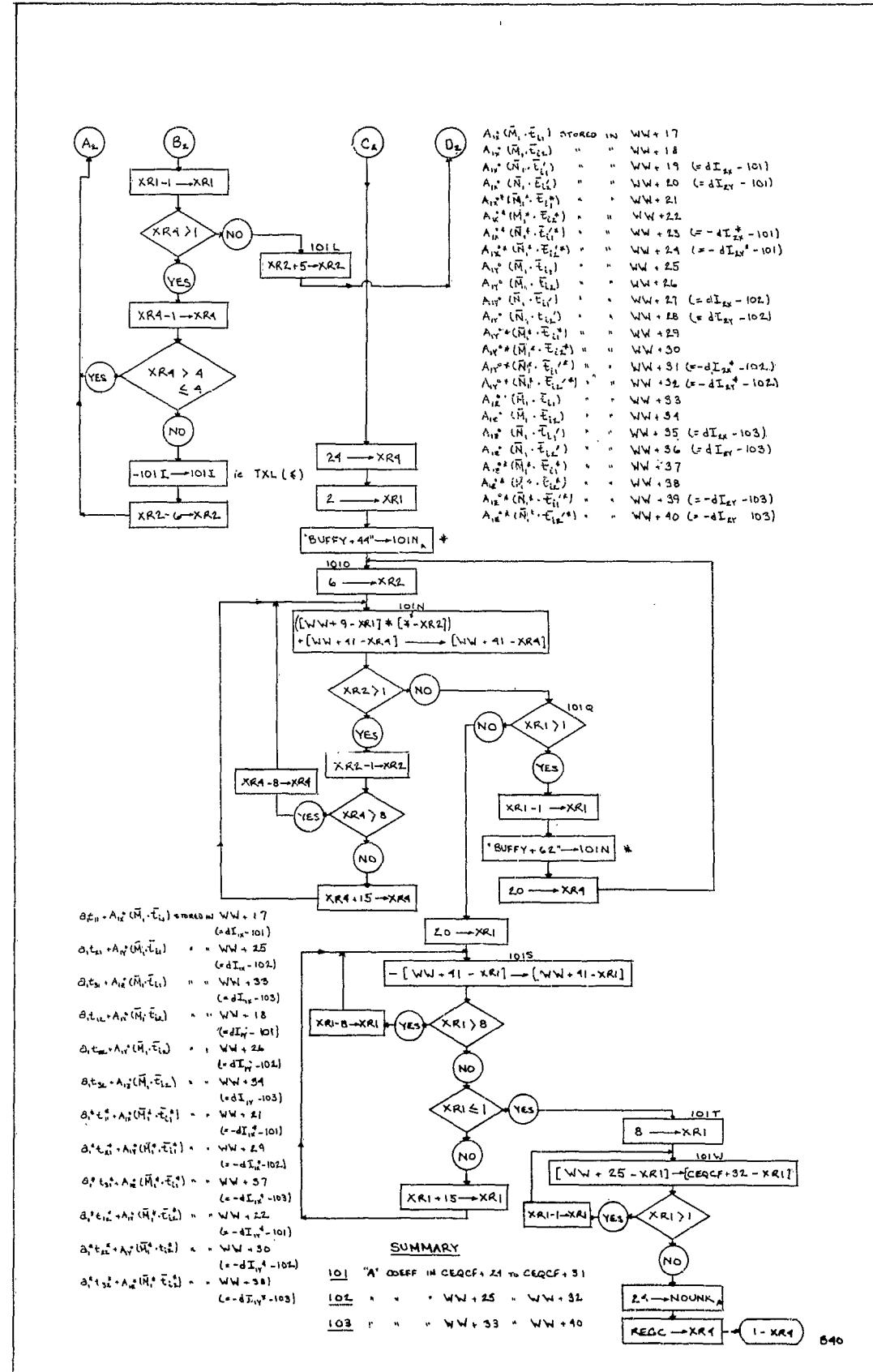


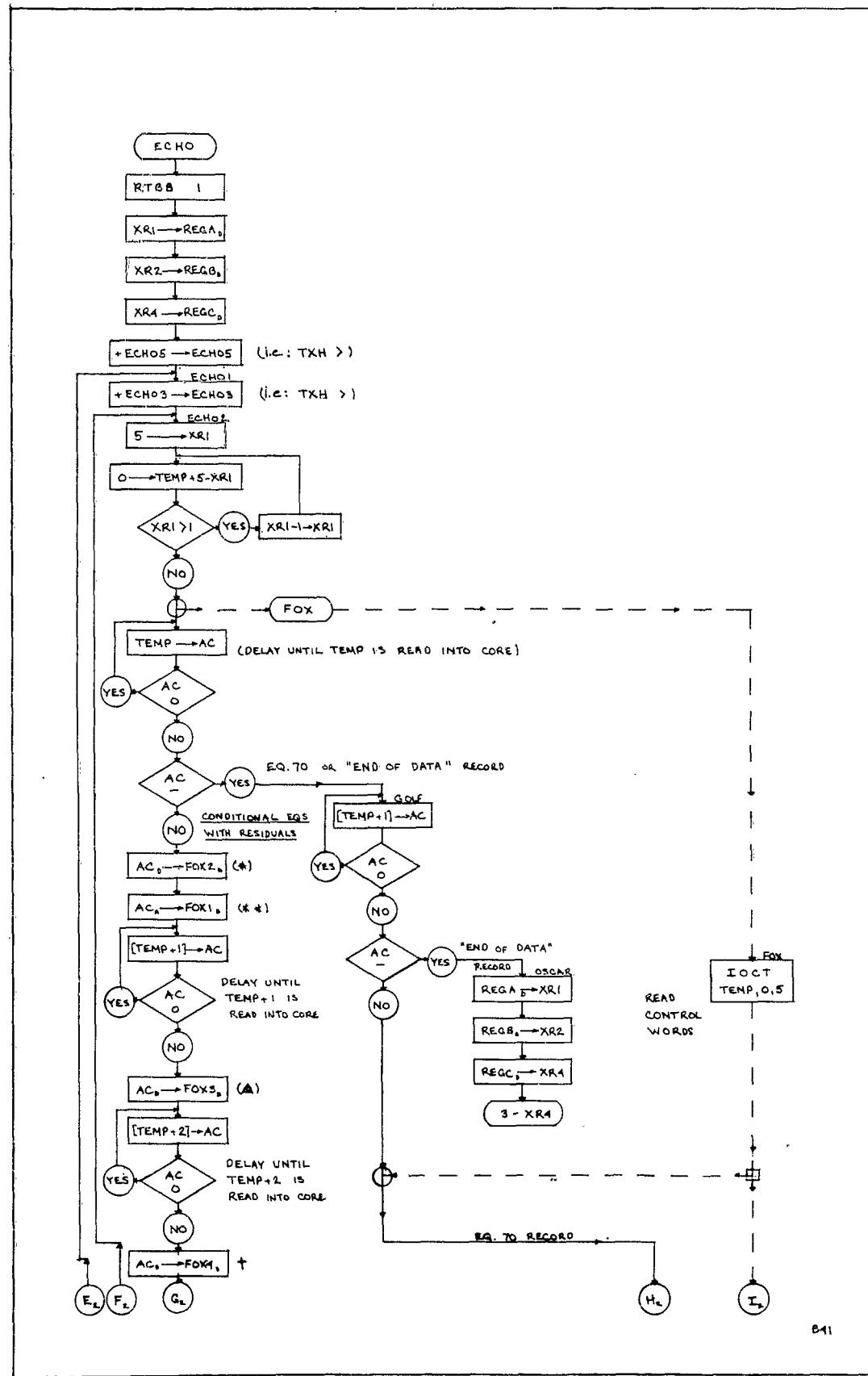


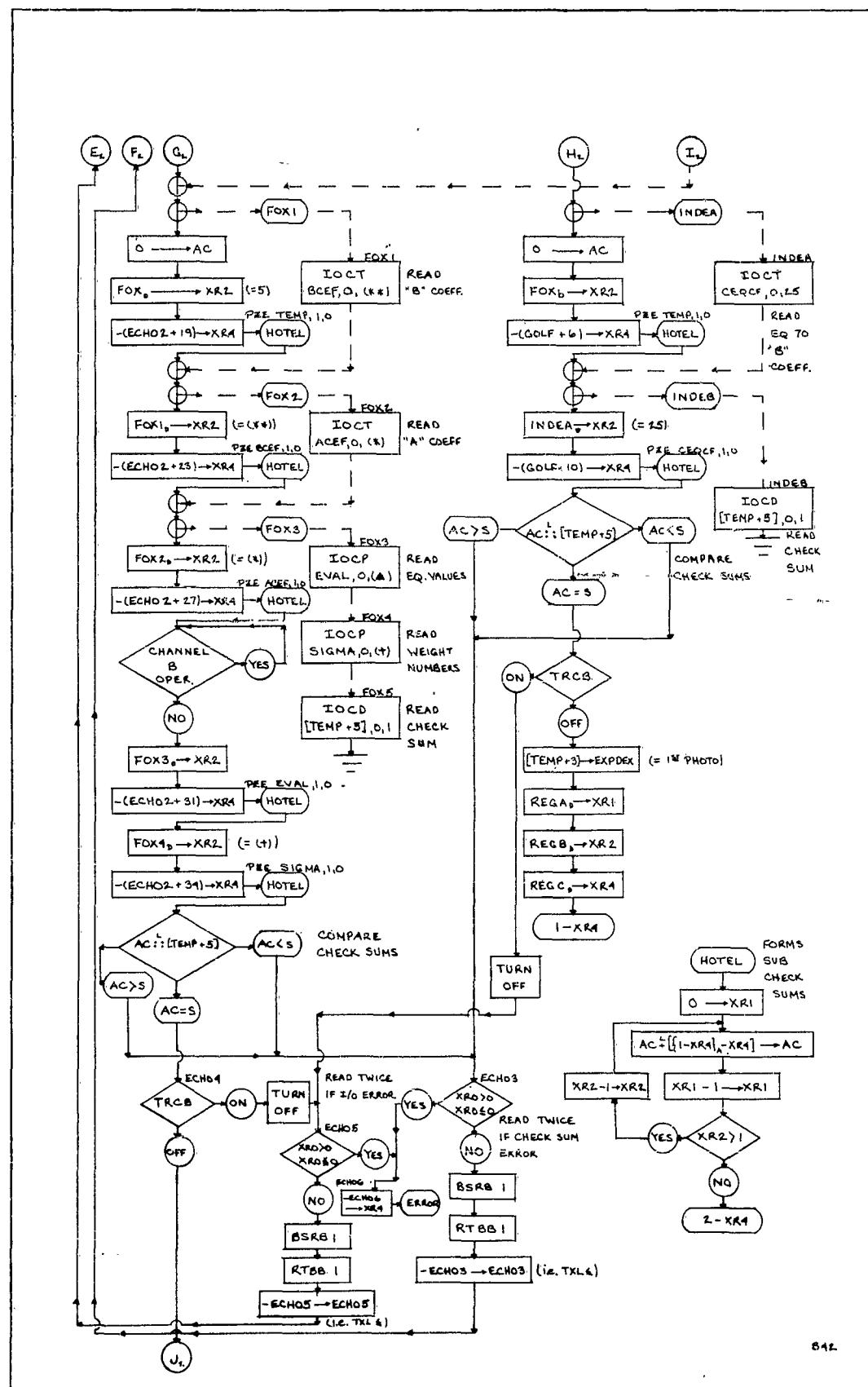


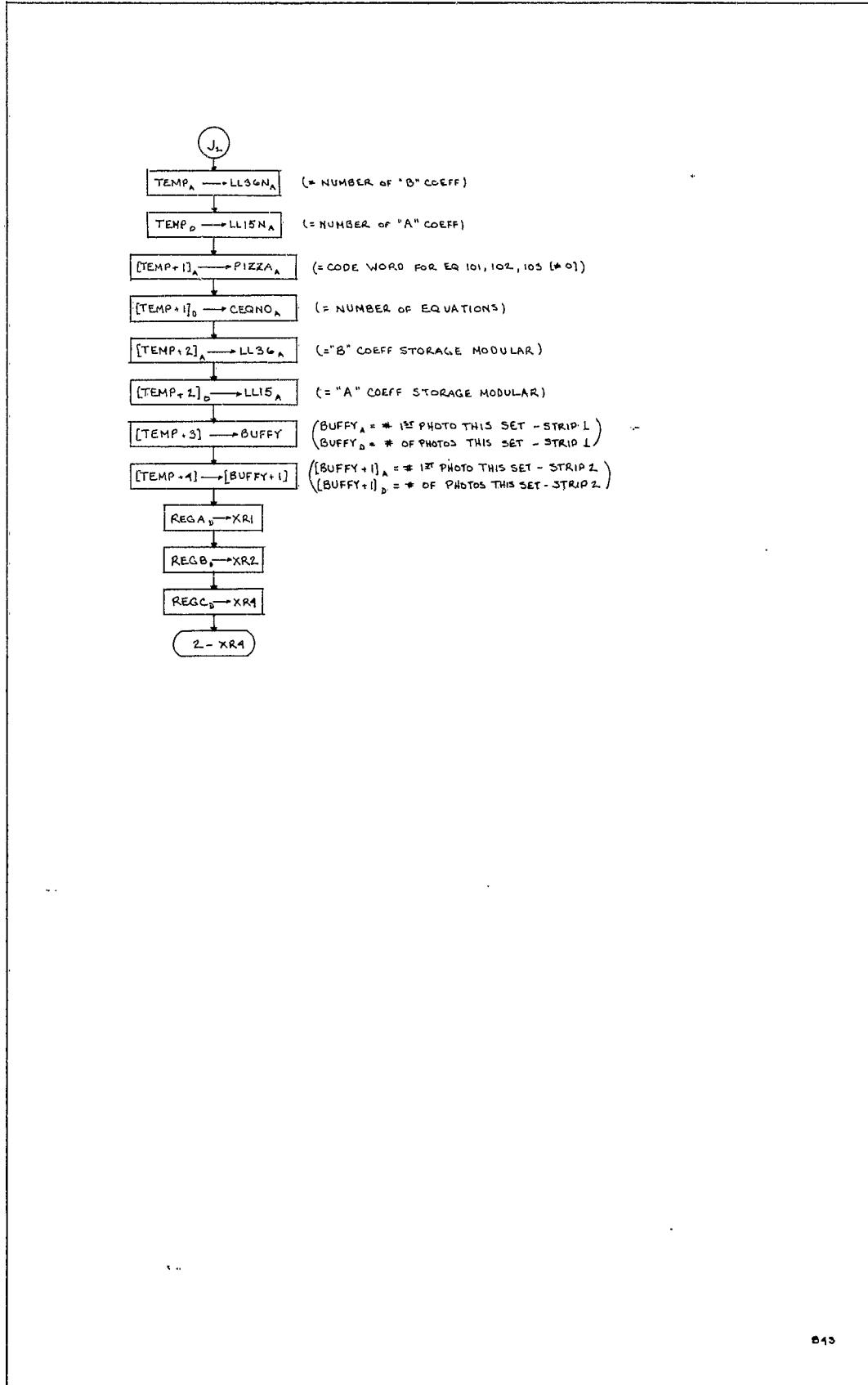


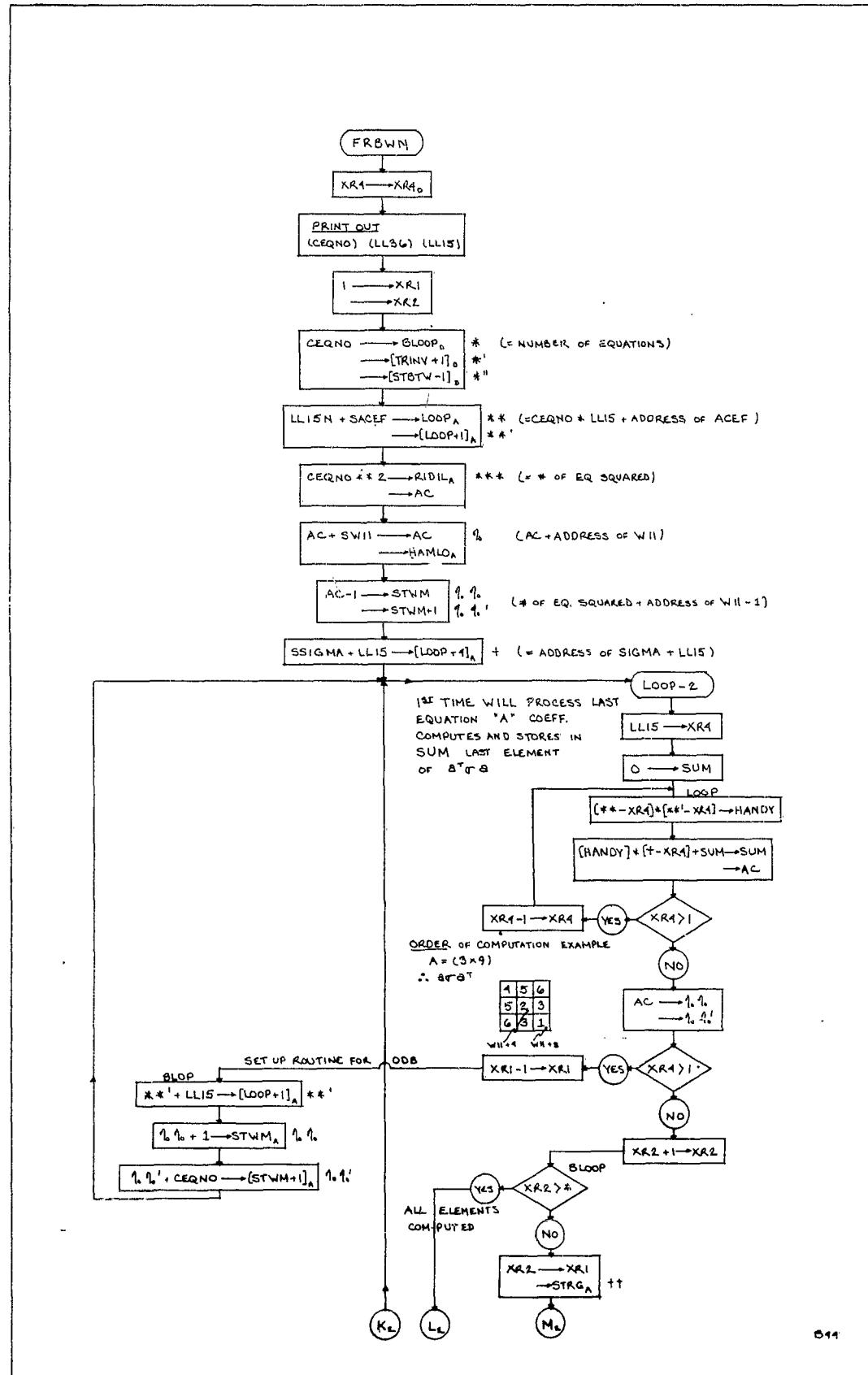


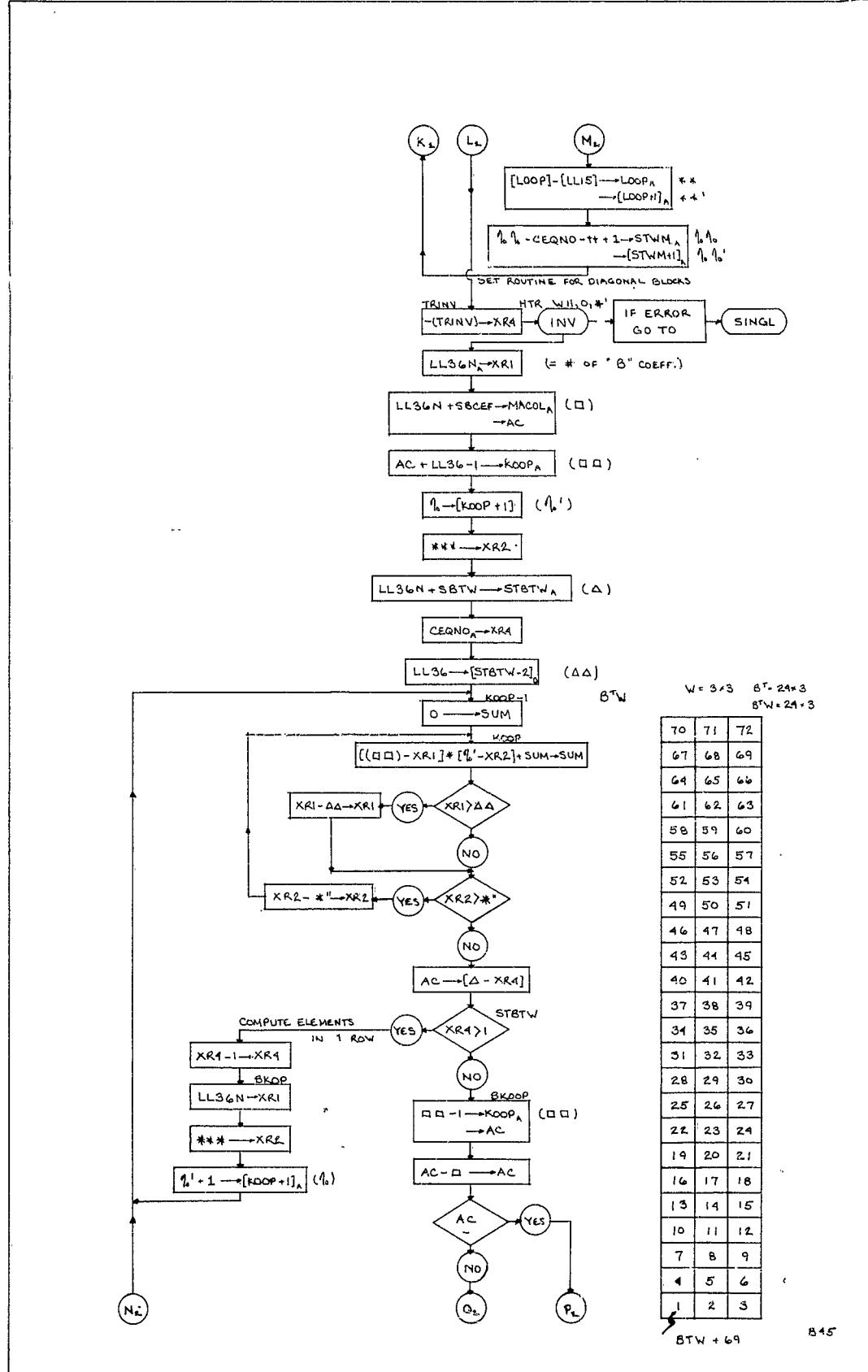


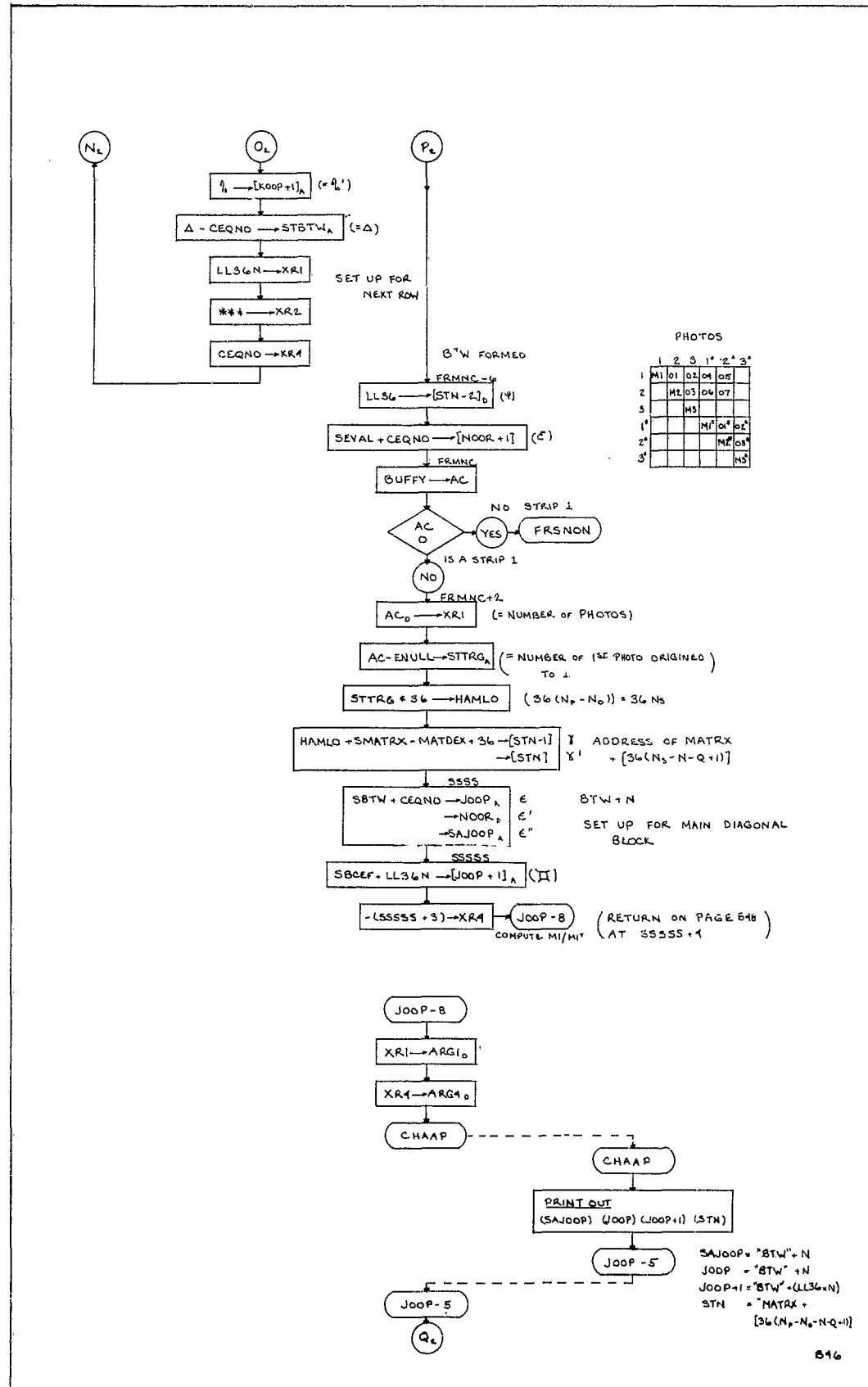


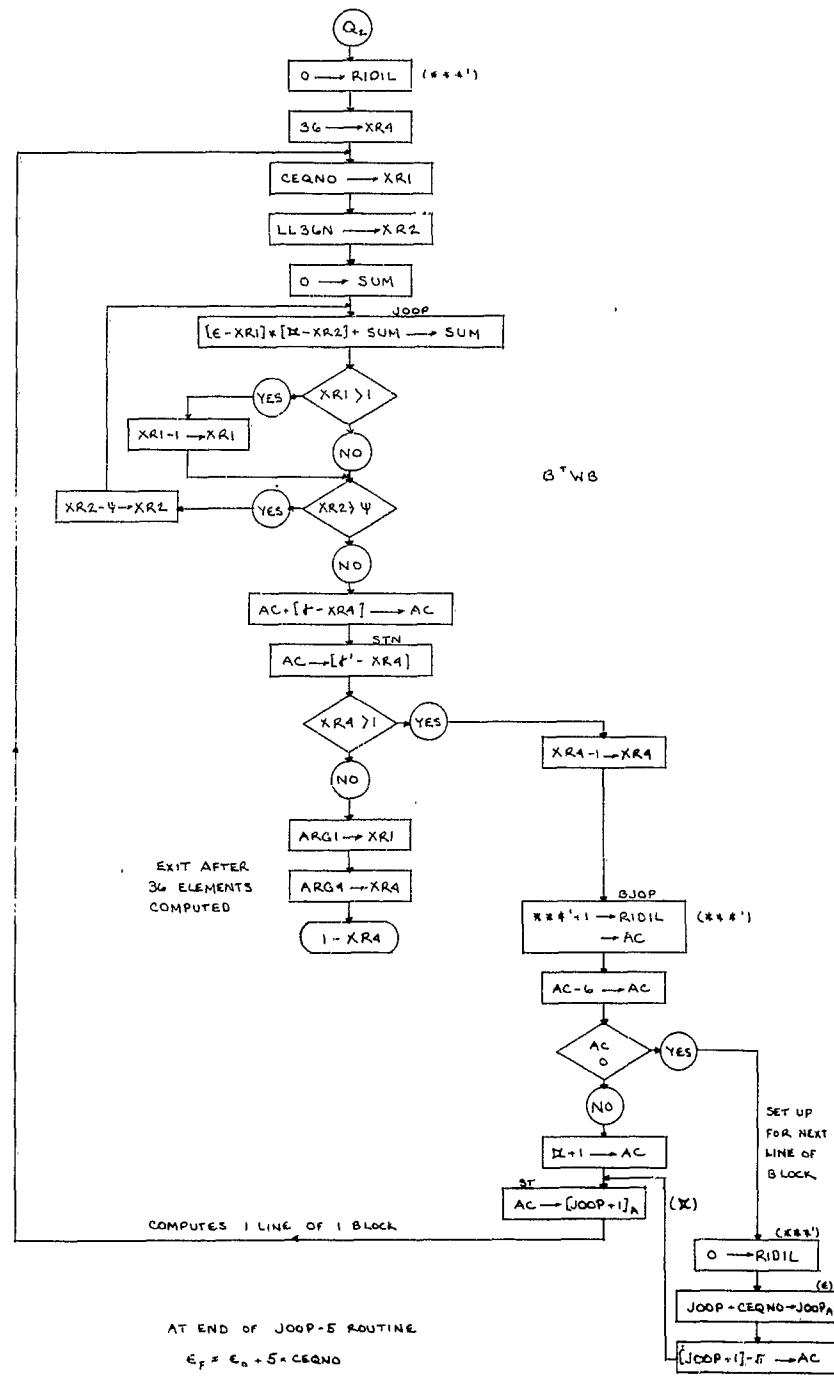




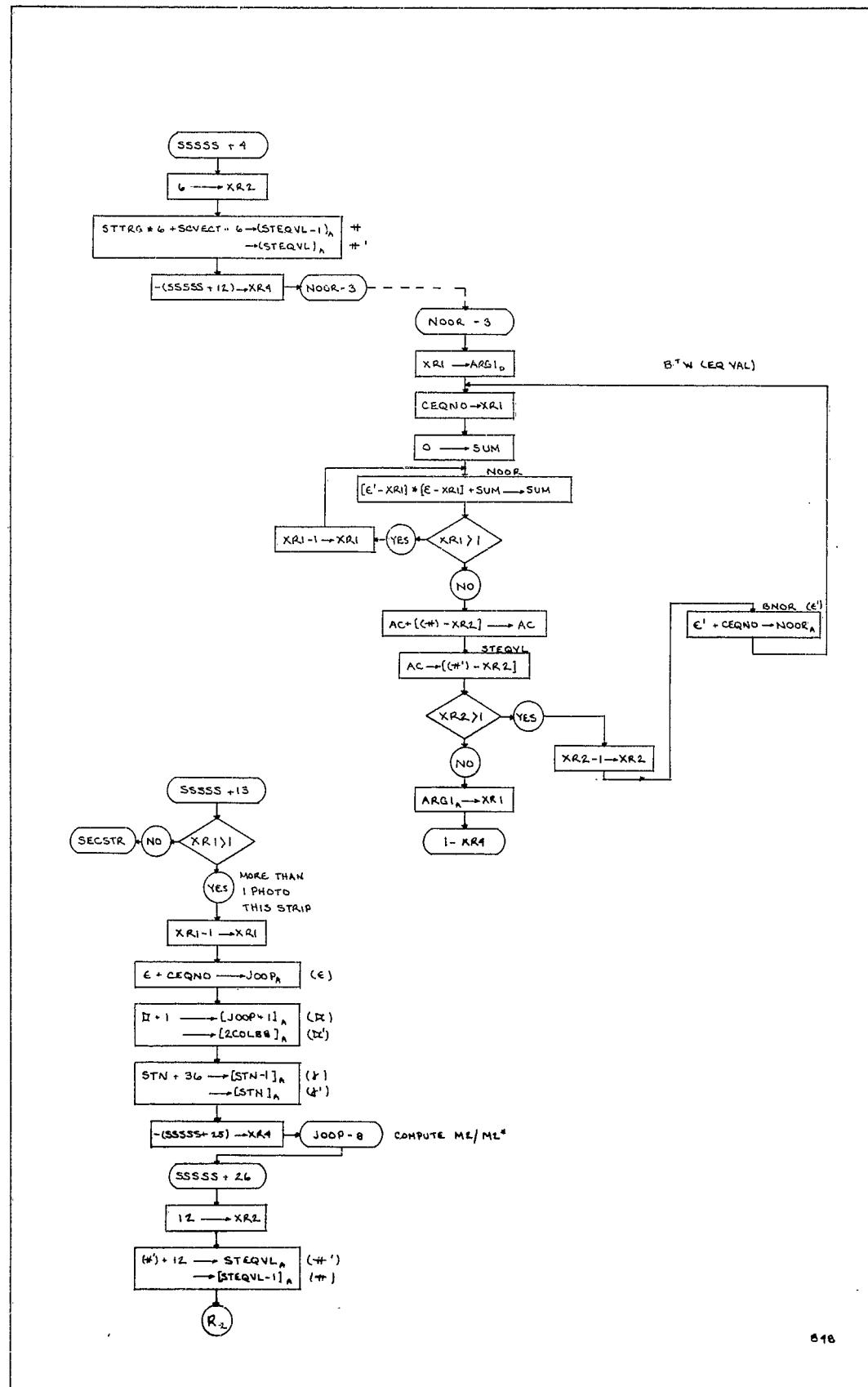


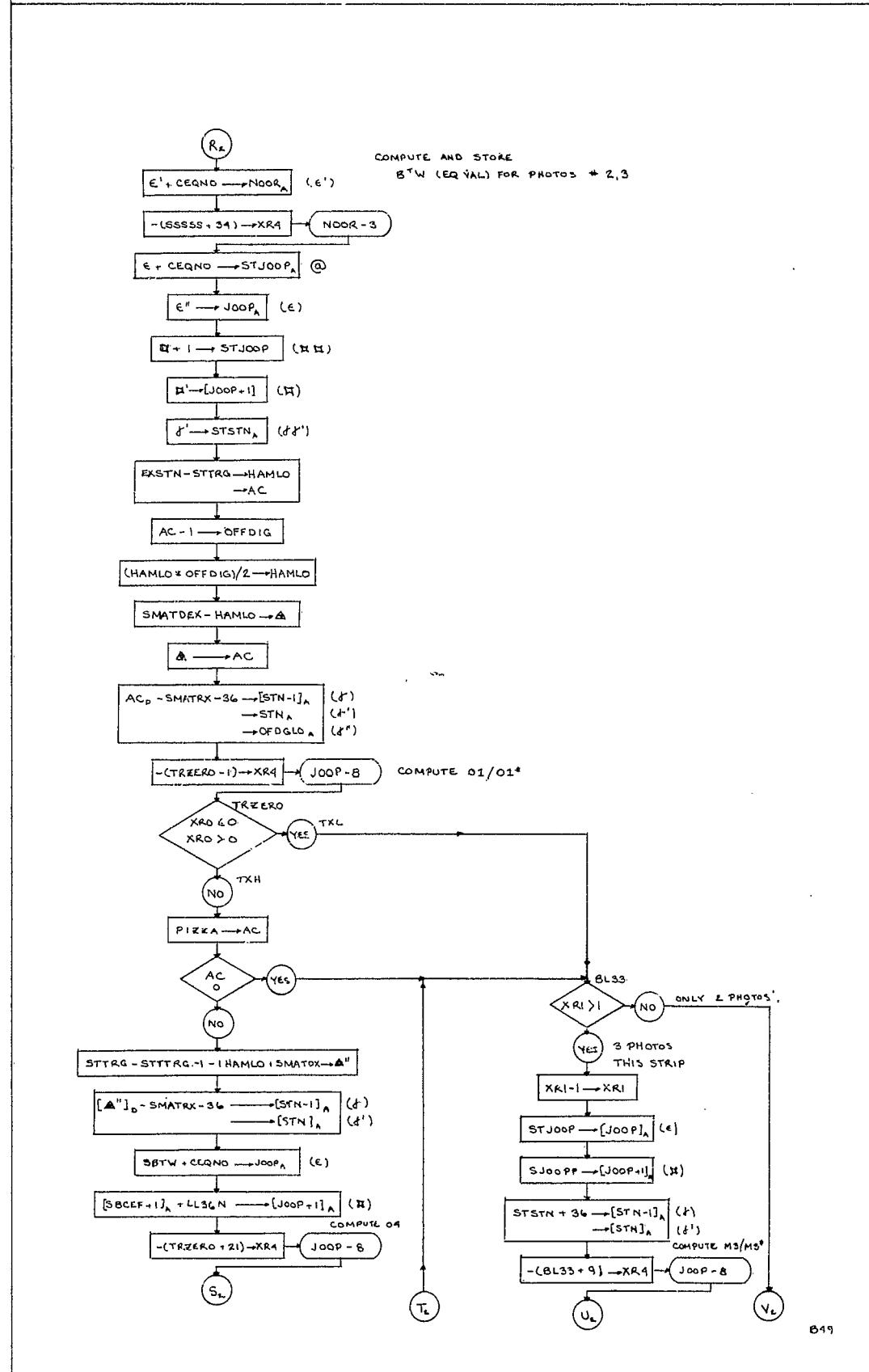


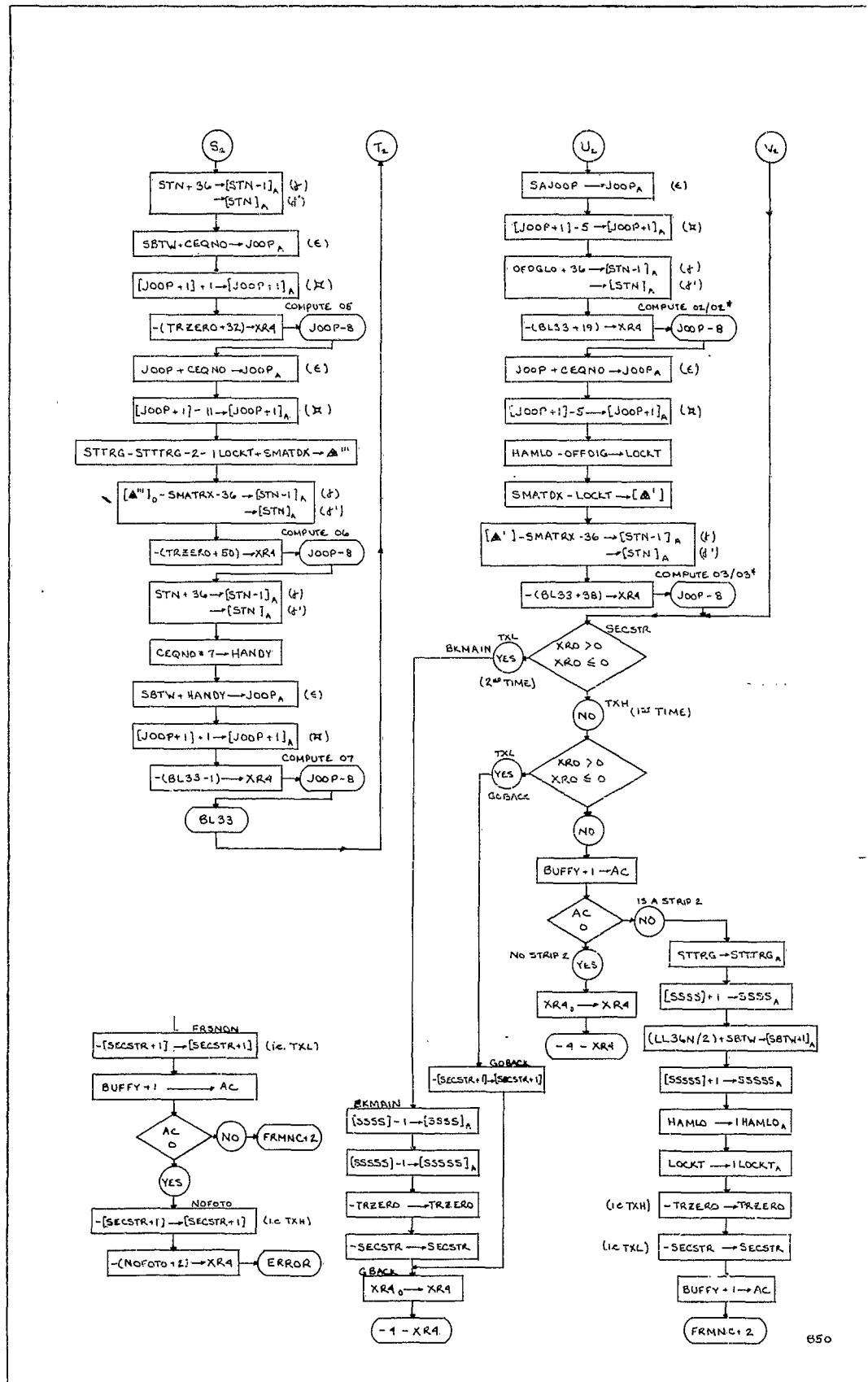




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ANALYTICAL AERIAL TRIANGULATION ERROR ANALYSIS AND
APPLICATION OF COMPENSATING EQUATIONS TO
THE GENERAL BLOCK TRIANGULATION AND ADJUSTMENT PROGRAM

FINAL TECHNICAL REPORT
VOLUME 2

Civil Engineering Systems Laboratory
Department of Civil Engineering
Massachusetts Institute of Technology
Cambridge, Massachusetts

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Further information concerning this project may be obtained from Mr. R. D. Esten, Chief, Photogrammetry Division, U. S. Army Engineer Geodesy, Intelligence and Mapping Research and Development Agency, Fort Belvoir, Virginia, telephone EDgewater 9-5500, ext. 62140.

AD	Accession No.	AD	Accession No.
Civil Engineering Systems Laboratory, Department of Civil Engineering, Massachusetts Institute of Technology, Cambridge, Massachusetts - ANALYTICAL AERIAL TRIANGULATION ERROR ANALYSIS AND APPLICATION OF COMPENSATING EQUATIONS TO THE GENERAL BLOCK TRIANGULATION AND ADJUSTMENT PROGRAM - L. Andrew R., Z. H. Elias, F. S. Greatorox	Final Technical Report - Appendix I, 1 August 1962, 200 pages, Corps of Engineers, GINMADA, Contract No. DA-44-009 ENG 4420, Task No. 8735-11-001-05, Unclassified Report	UNCLASSIFIED	UNCLASSIFIED
The objective of the activities reported is to effect improved accuracy through incorporation in the program means of error adjustment and compensation. The first volume of the report presents:	1. the nature of random and systematic errors and the basic techniques for treating their effects as applicable to the analytical photogrammetric problem; 2. the basic least squares method and its incorporation in the computer program; 3. complete mathematical description of the program; 4. studies of the nature and effects of the important error sources: lens and camera errors, atmospheric refraction, film distortion; 5. the study of various techniques for the solution of simultaneous equations; 6. operating instructions; 7. the results, conclusions, and resulting recommendations of test runs of the final computer program.	In the supplied General Block Triangulation digital computer program, through incorporation in the program means of error adjustment and compensation. The first volume of the report presents:	1. the nature of random and systematic errors and the basic techniques for treating their effects as applicable to the analytical photogrammetric problem; 2. the basic least squares method and its incorporation in the computer program; 3. complete mathematical description of the program; 4. studies of the nature and effects of the important error sources: lens and camera errors, atmospheric refraction, film distortion; 5. the study of various techniques for the solution of simultaneous equations; 6. operating instructions; 7. the results, conclusions, and resulting recommendations of test runs of the final computer program.
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